

Source inversion in seismology

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Outline

Source inversion in seismology

Goals and inversion structure

Source model and inversion method, a multi-step inversion approach

Source inversion using the Kiwi tools

Inversion tips: frequency vs. time domain, bodywaves vs. full waveforms, ...

Example of applications

Point source inversion using full waveforms, regional applications

Extended source inversion, an overview on different approaches

Point source inversion using bodywaves, a deep earthquake case

Microseismicity application, source inversion in mining environments

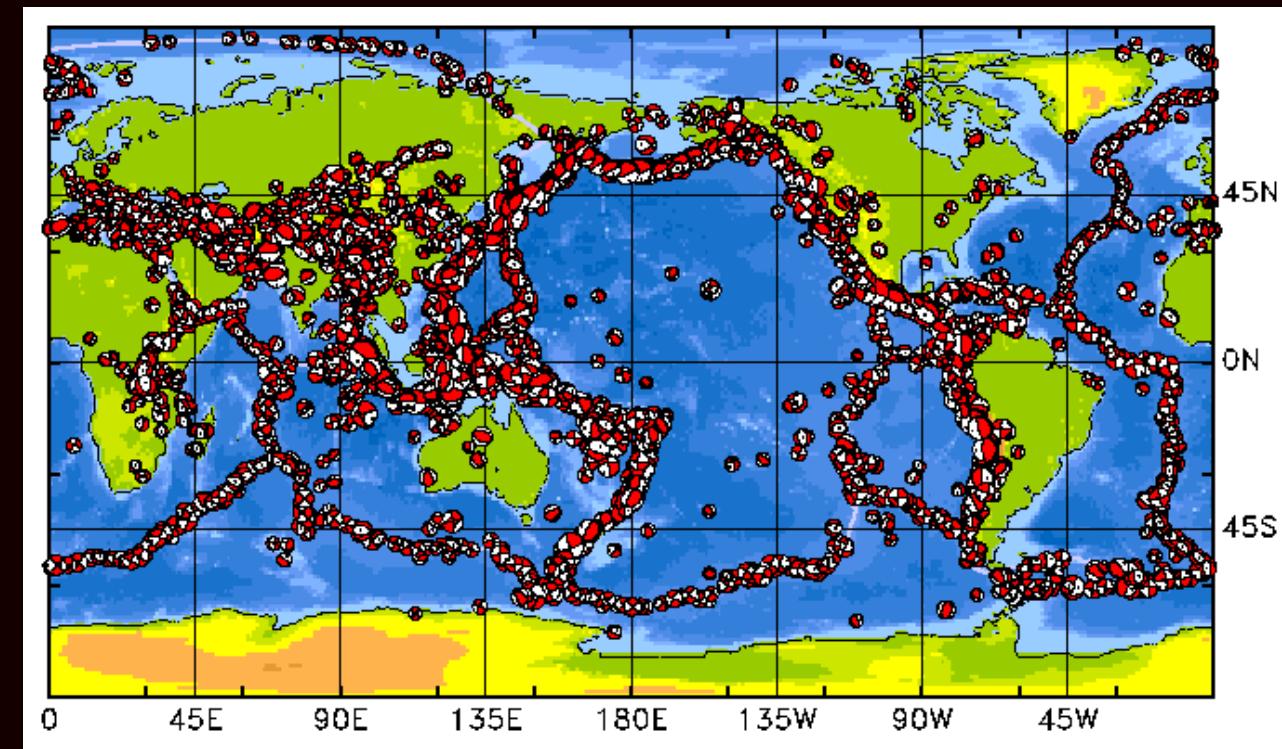


Source inversion in seismology

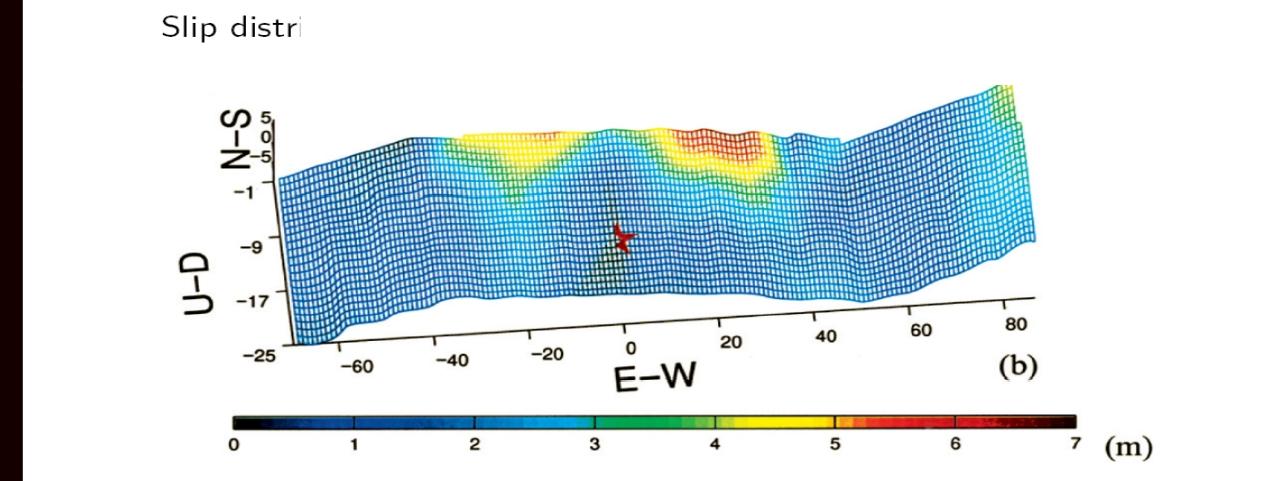


Source inversion in seismology, overview

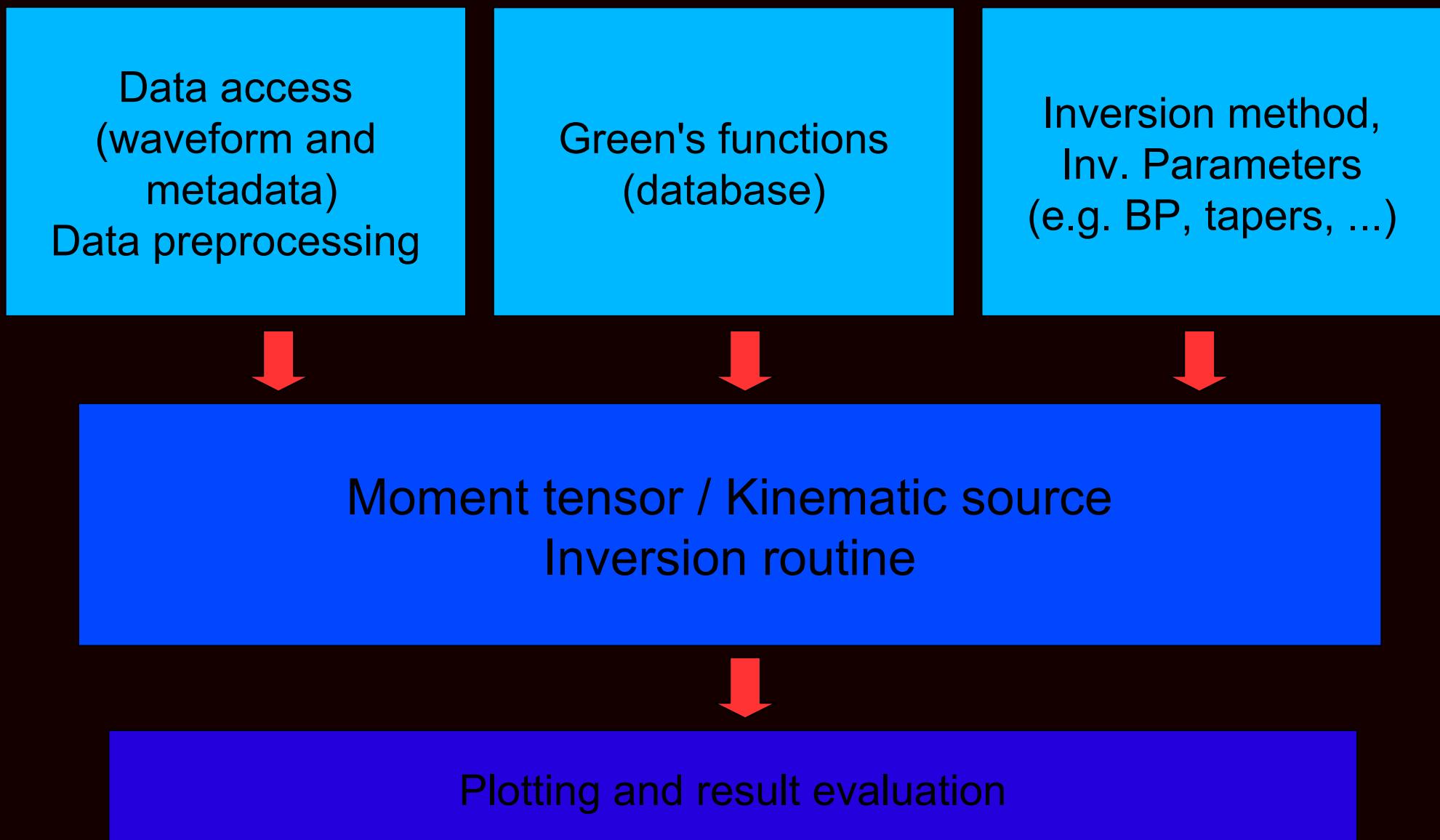
Global CMT catalogue,
1976-2005



Slip map
kinematic model
(Li et al. 2002)



Source inversion in seismology, what do we need?



Source inversion in seismology, what do we need?

Data access
(waveform and
metadata)

Data preprocessing

Data access/preprocessing

Waveforms (here displacements)

Station information (location, instrument, sampling)

Instrumental responses

Processing tools
(filtering, mean/trend removal, tapering, resampling...)

Acceleration/Velocities/Displacements

Data quality evaluation (gaps, spikes, seismic noise)



Source inversion in seismology, what do we need?

MESS 2012 Data

- Displacement waveforms (mostly broadband seismometers)
- Preprocessed (instrument response, integration, ...)
- Metadata: Station information (location, instrument, sampling)

A number of different events

- Mw Ca. 4 - 7
- Epic. Distances up to 1000km
- Source Depth down to 30km



Source inversion in seismology, what do we need?

Green's functions (1D)

Needed to build
synthetic seismograms

Accounting for the earth structure

Green's functions
database

Precompiled database structures to allow rapid access and less storage requirements

What is needed?

- 1D GFs database access for reference models (e.g. PREM, AK135, ...)
- Tools for specific databases for local applications
- Database handlers (generation, access)

We use fast access databases based on HDF5. Kiwi tools handle database access.

The system is independent on the algorithm used to compute GFs.



Source inversion in seismology, what do we need?

MESS 2012 GFDB

- 1D model (physical property = $f(\text{depth})$)
- IASP91 model
- Source depths (0-40km)
- Epic. Distances (0-1000km)
- 10 Gfs



Source inversion in seismology, what do we need?

MESS 2012 Synthetic seismograms

- GFDB ($z, d, 10\text{GFs}$)
- Source model
- Source & station locations
- (station azimuth)
- 10 GFs
 - z =source depth
 - d =epicentral distance
- 3-component Synthetics



Source inversion in seismology, what do we need?

Inversion method/parameters

Many different approaches exist.

Often specific methods are more suited for specific events
(e.g. depth, magnitude)

Tools which may consider specific selection of:

Inversion method,
Inv. Parameters
(e.g. BP, tapers, ...)

- Fitting approach (time domain, amplitude spectra, others?, norms)
- Inversion approach (e.g. grid walk, gradient methods, ...)
- Source constraints (DC, DC+CLVD, DC+CLVD+ISO, extended source models, others?)
- Seismic phases (e.g. full waveforms vs. single phases), tapering
- Frequency range (BP is typically chosen in base of magnitude, phases)
- Selection/removal of stations/components
- Parameters uncertainties

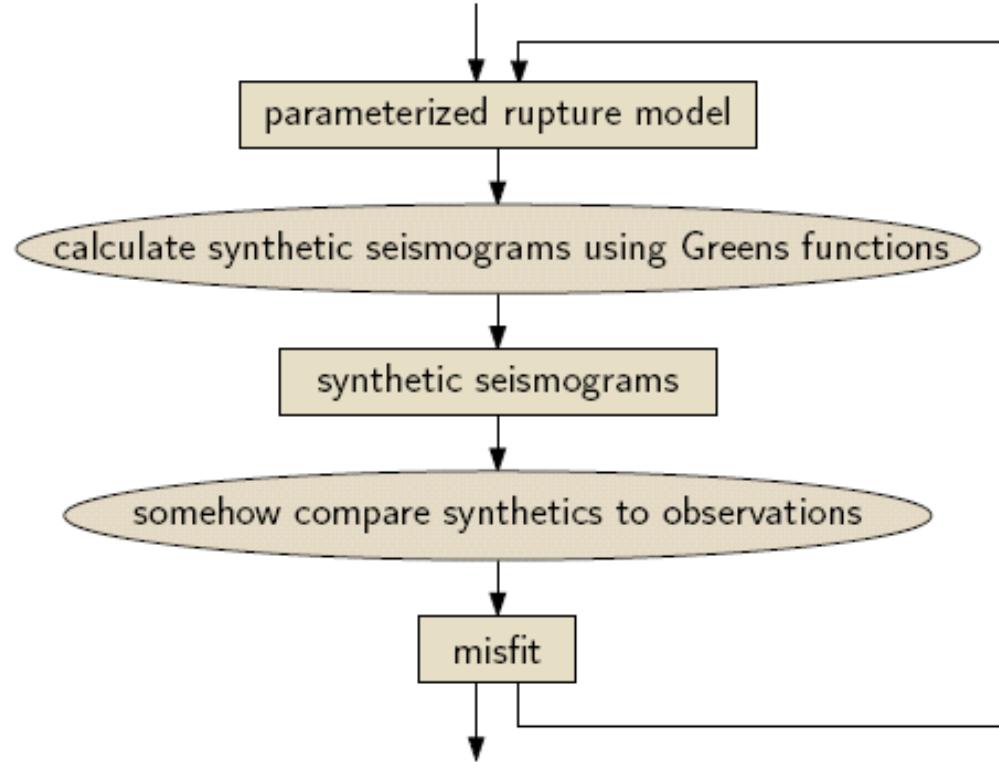


Source inversion in seismology, what do we need?

Inversion method/parameters

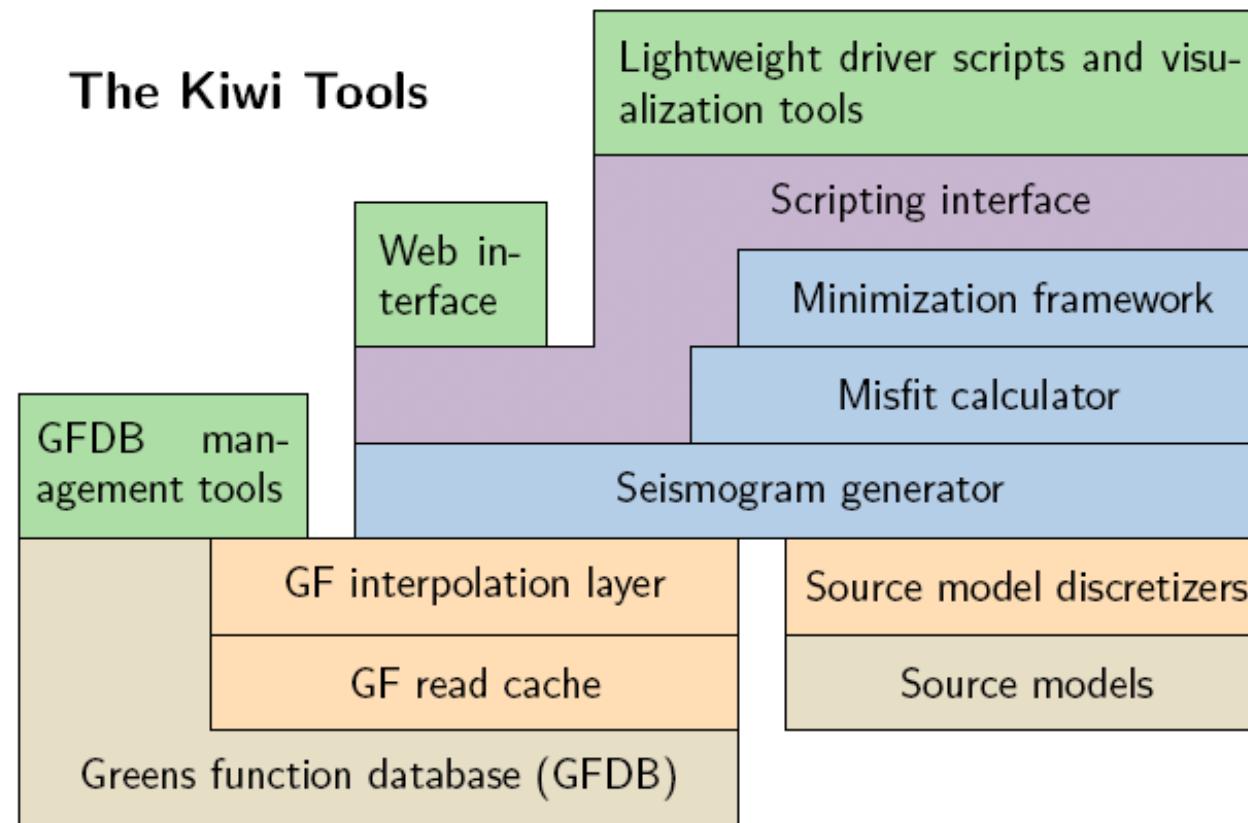
- Time domain inversion (fitting waveforms)
- Frequency domain inversion (fitting amplitude spectra only)
- Own Bandpass
- Own Taper (P, S, P+S, full waveforms)
- Own Norm (L1, L2)
- Parameters uncertainty by bootstrap





Heimann 2011

Source inversion in seismology using the Kiwi tools



Heimann 2011

OpenSource

Running under Linux

Python + Fortran implementation

<http://kinherd.org>

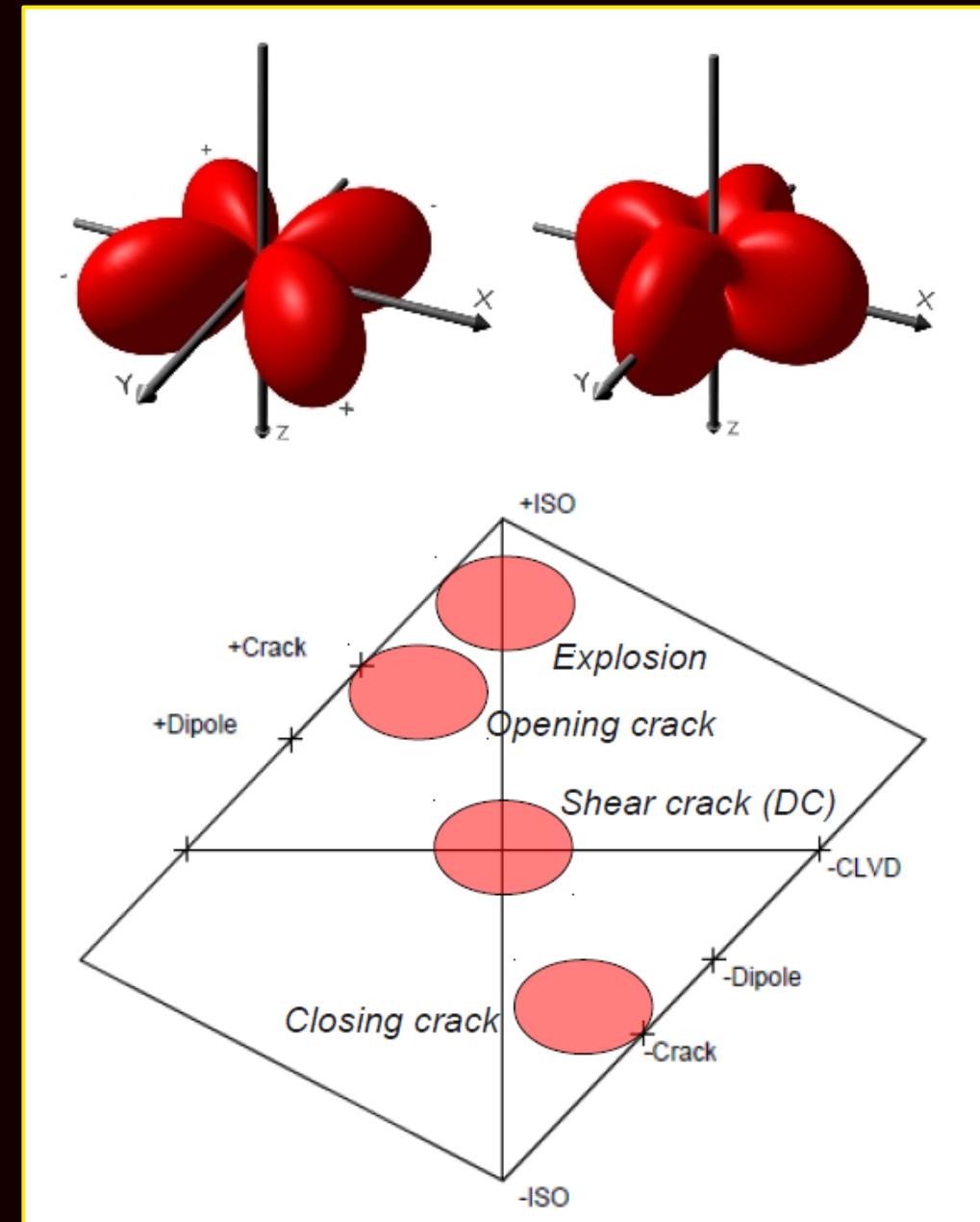


Point source model, double couple & moment tensor

Earthquakes is often well modeled in terms of shear cracks, using a point source representation (DC model).

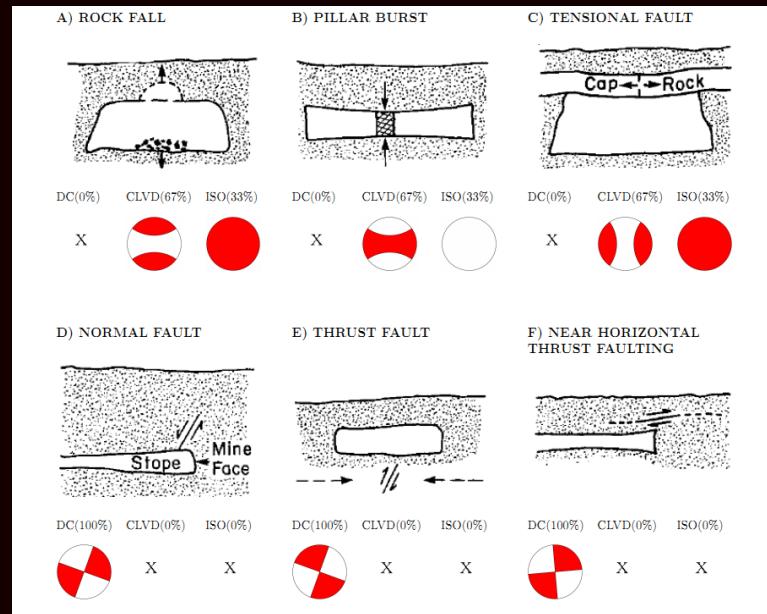
More complete point source model is represented by a moment tensor (MT)

$$MT = MT_{DC} + MT_{CLVD} + MT_{ISO}$$



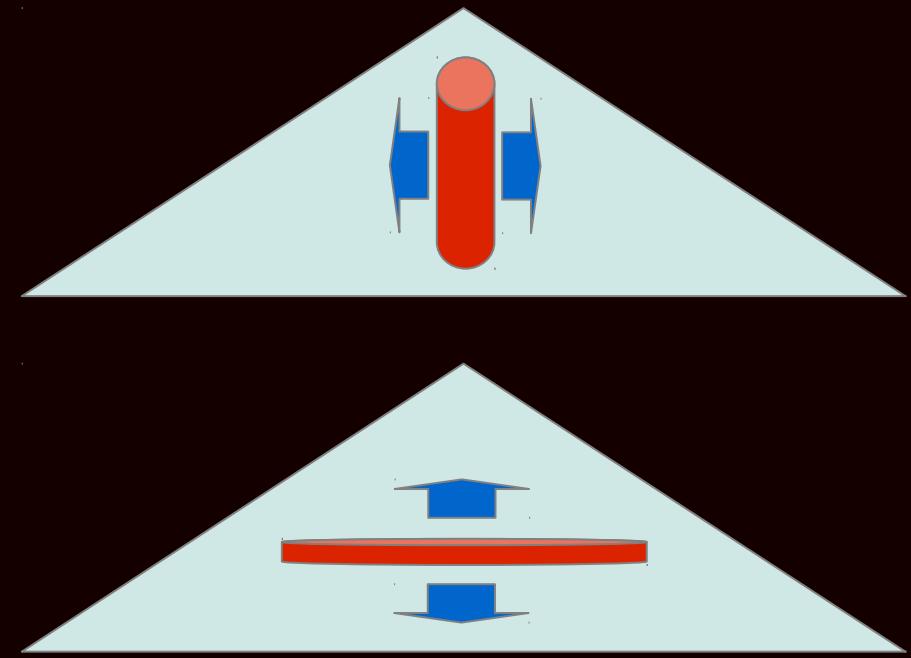
On the adoption of full moment tensor source models

Mining environments



after Hasegawa et al. (1989)

Volcanoes



Non DC source components are relevant

Volume variations, tensile cracks, explosions and collapse sources can be investigated



On the adoption of full moment tensor source models

Common ISO=0 constraint for natural earthquakes (e.g. Global CMT)

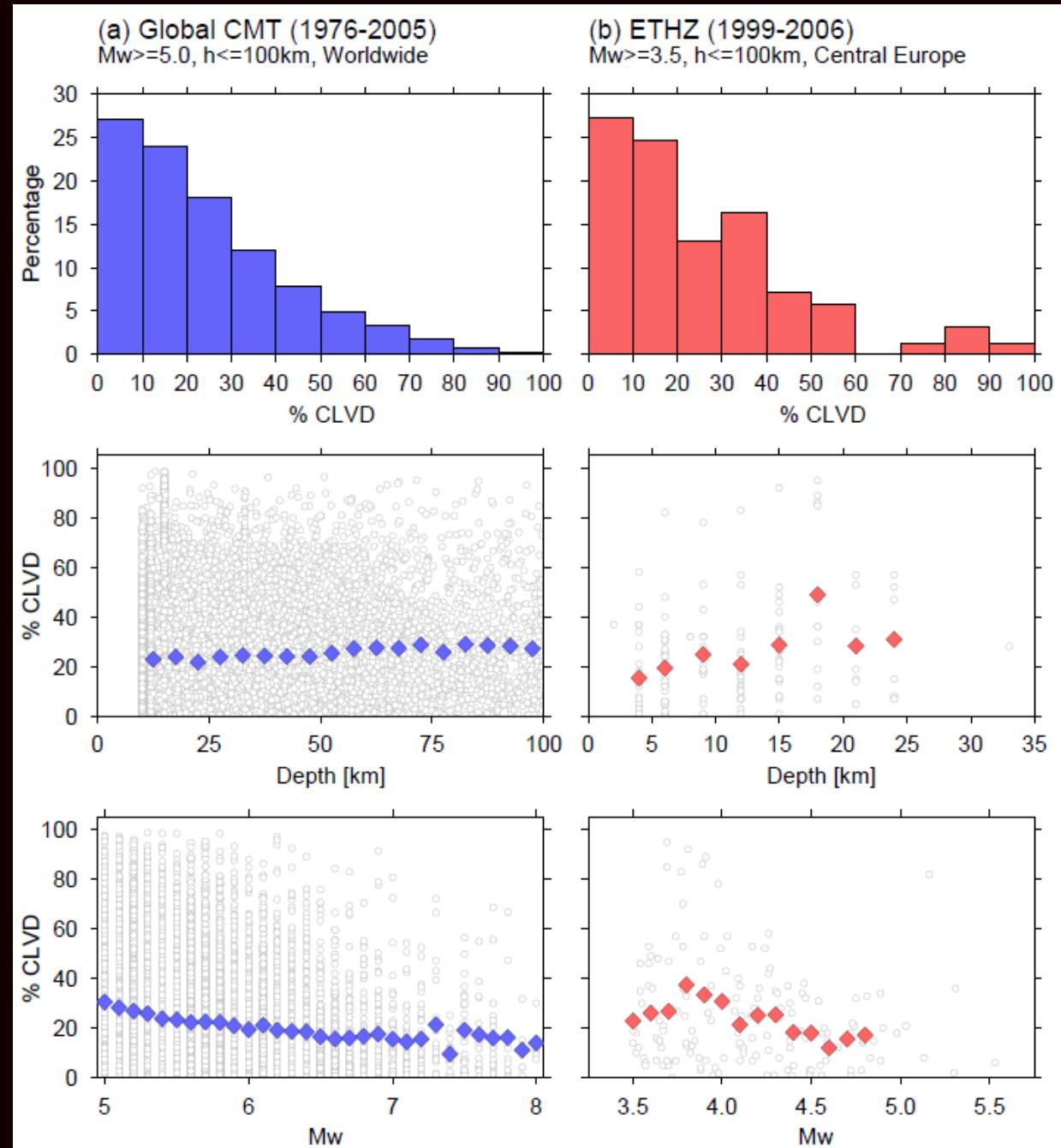
Spurious non-DC terms:

Waveform propagation
mismodeling

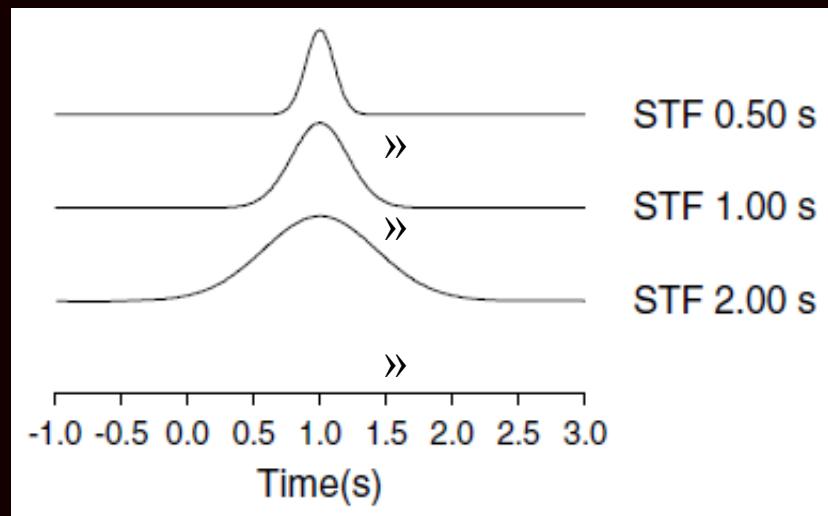
Poor network configurations
and data quality

Complex sources

Real non-DC features



On the source time function



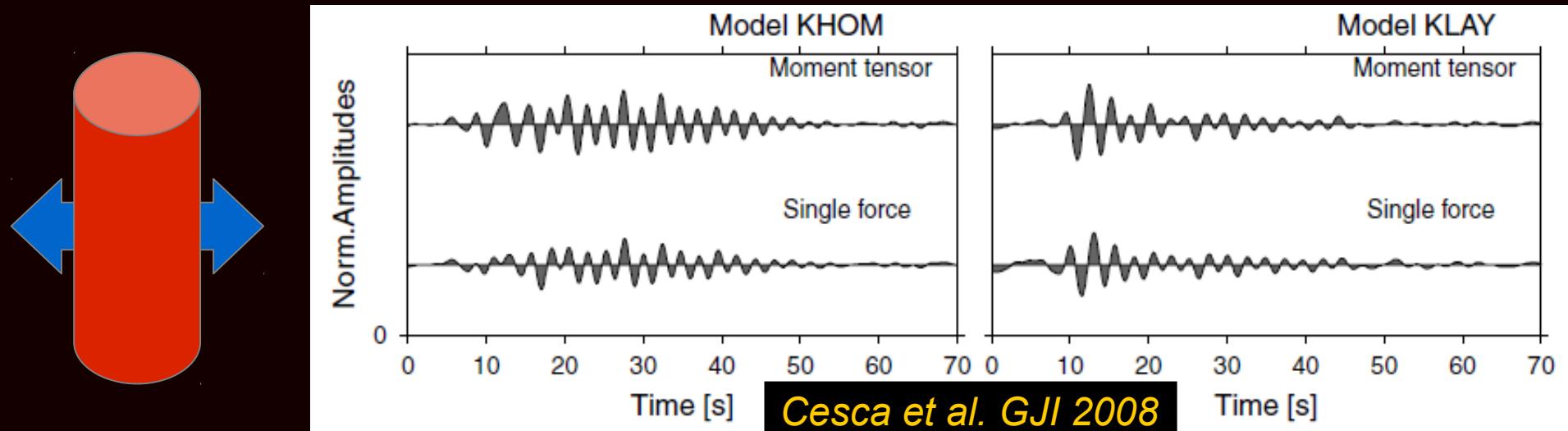
STF (slip rate function)

Simple approximation is valid for DC event

Rise time is the time a point source releases energy

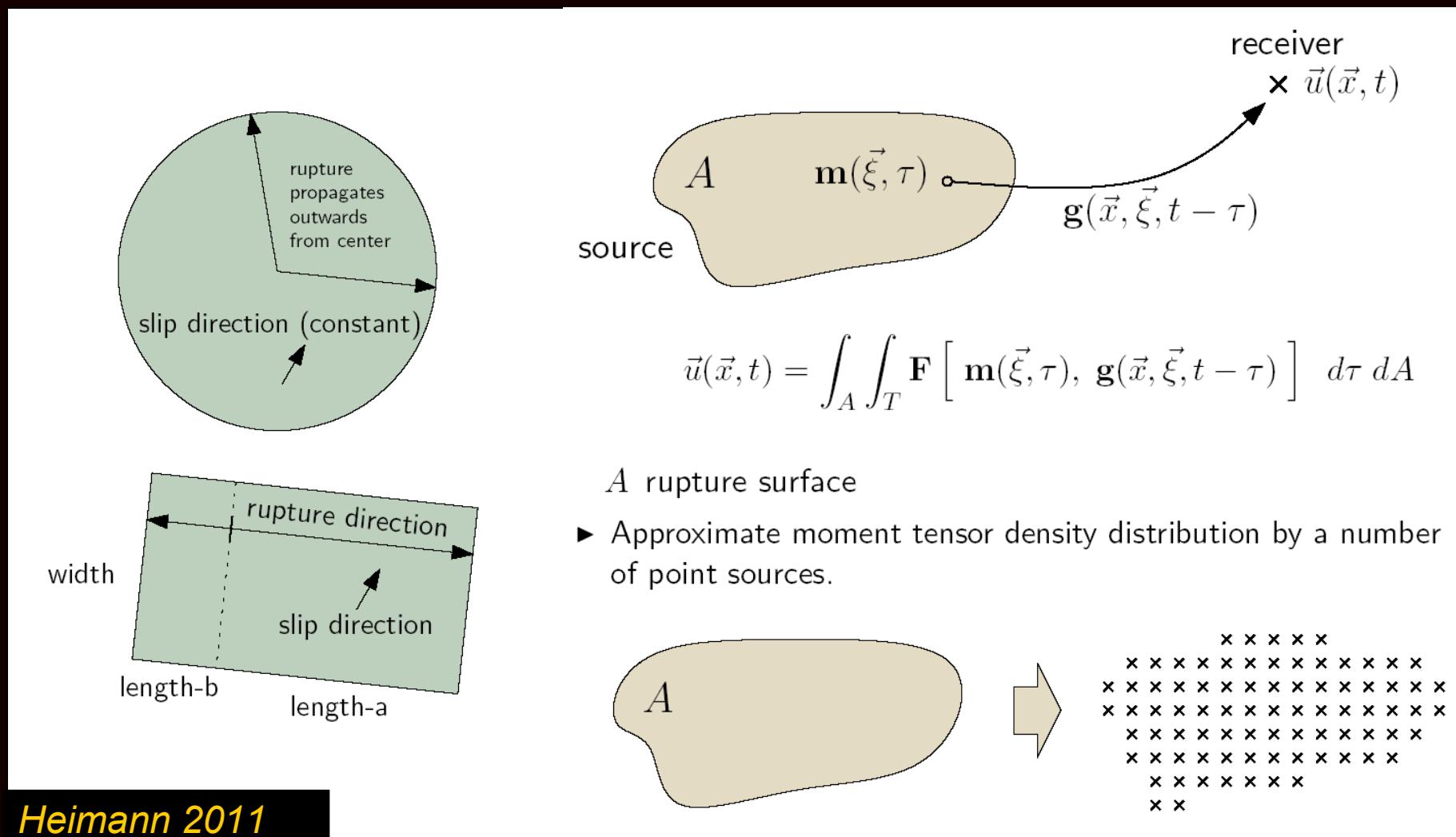
Note that finite rupture are superposition of point sources with constant rise time

Complex STFs may be needed for other environments, e.g. at volcanoes, to describe resonant sources, tremors, and in general sources excited along a large time.

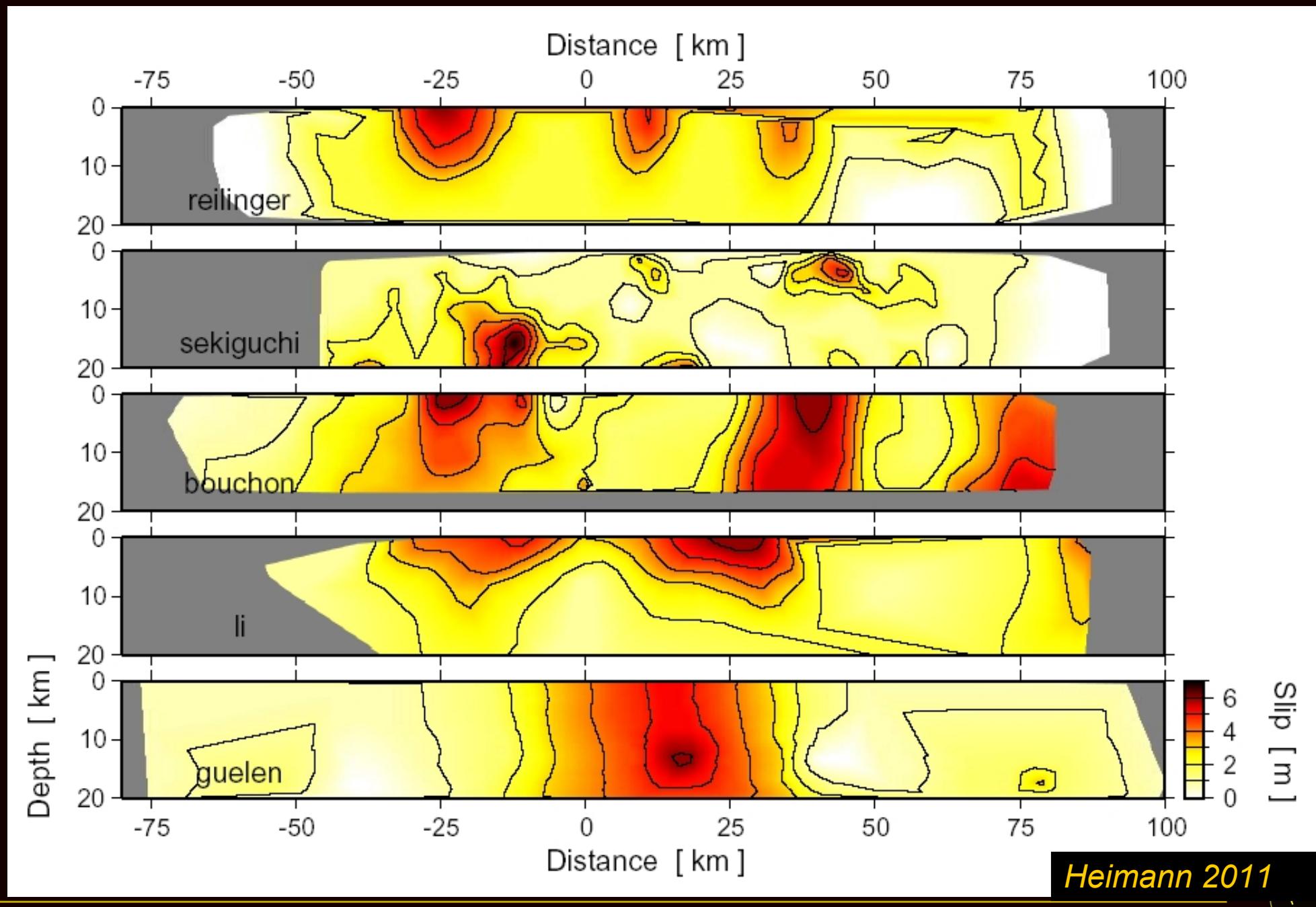


Extended source model, definitions

Extended sources may be reproduced by superposition of several point sources distributed along a planar (or bended) rupture surface. Each point source start radiating when reached by the rupture front. Radiation lasts for a given (rise) time.



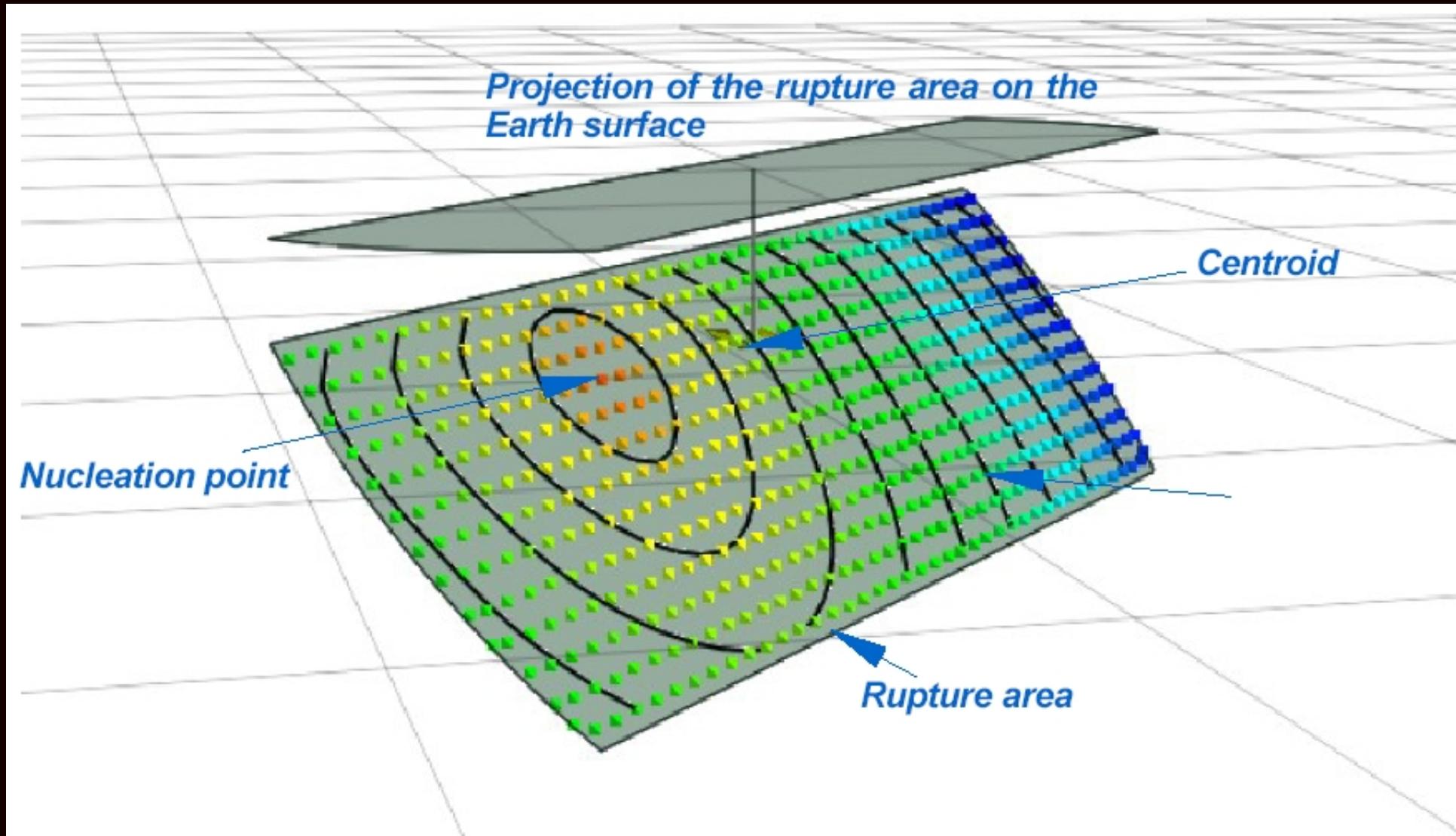
One earthquake, five solutions



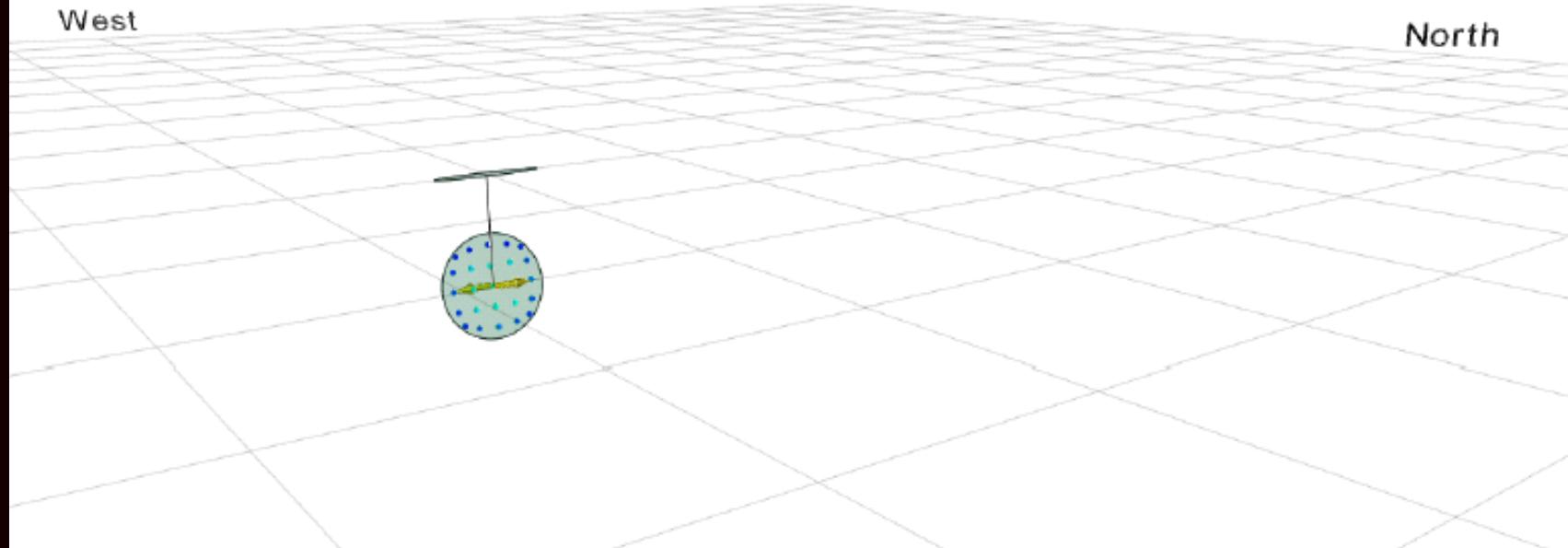
Heimann 2011



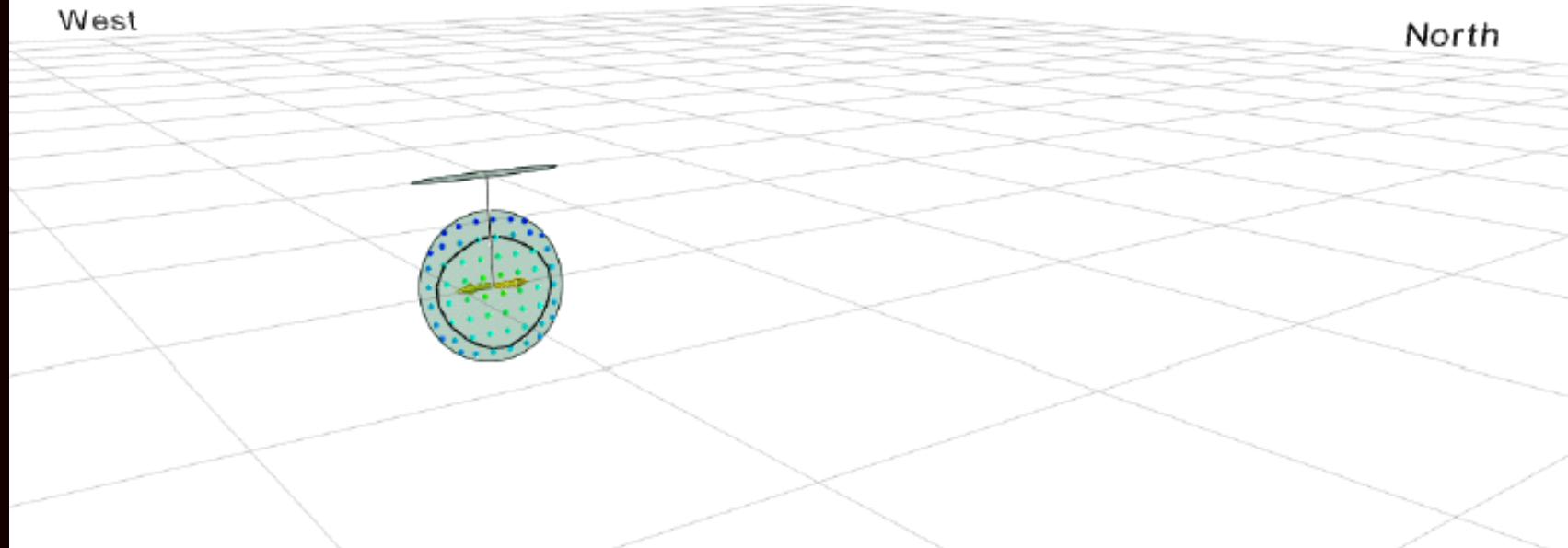
The eikonal source model



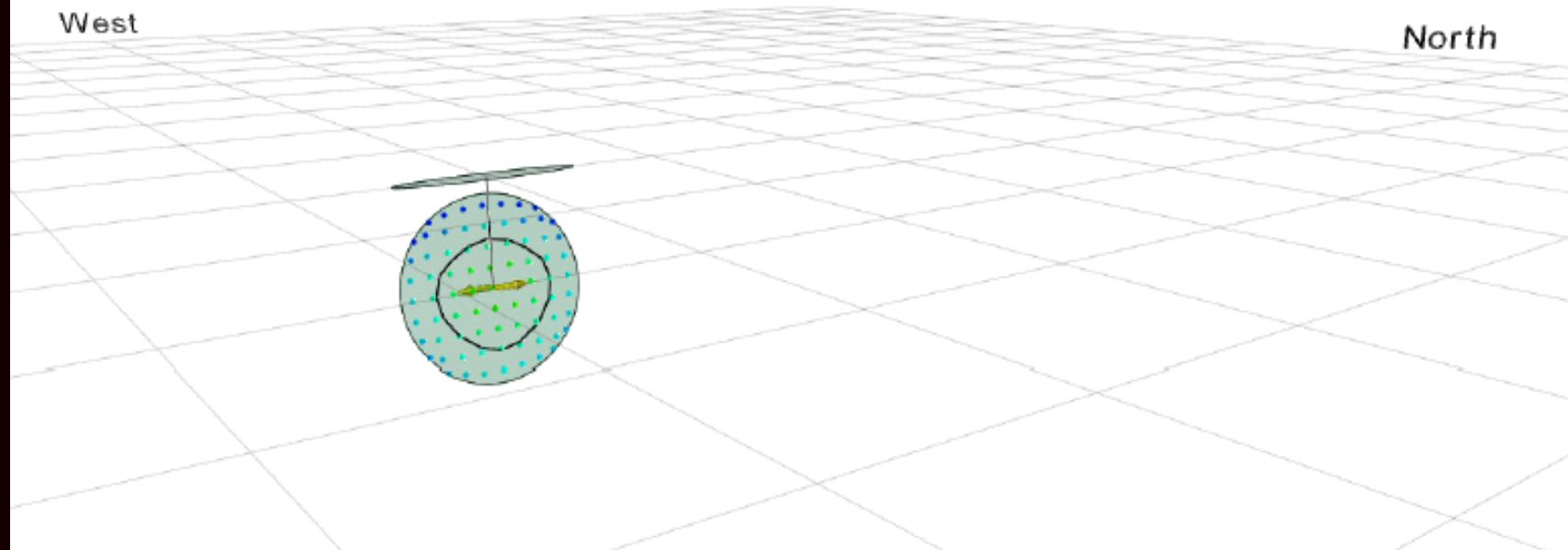
- ▶ Initially circular
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- ▶ Region may be constrained by additional planes
- ▶ Variable nucleation point
- ▶ Rupture velocity proportional to shear wave velocity profile



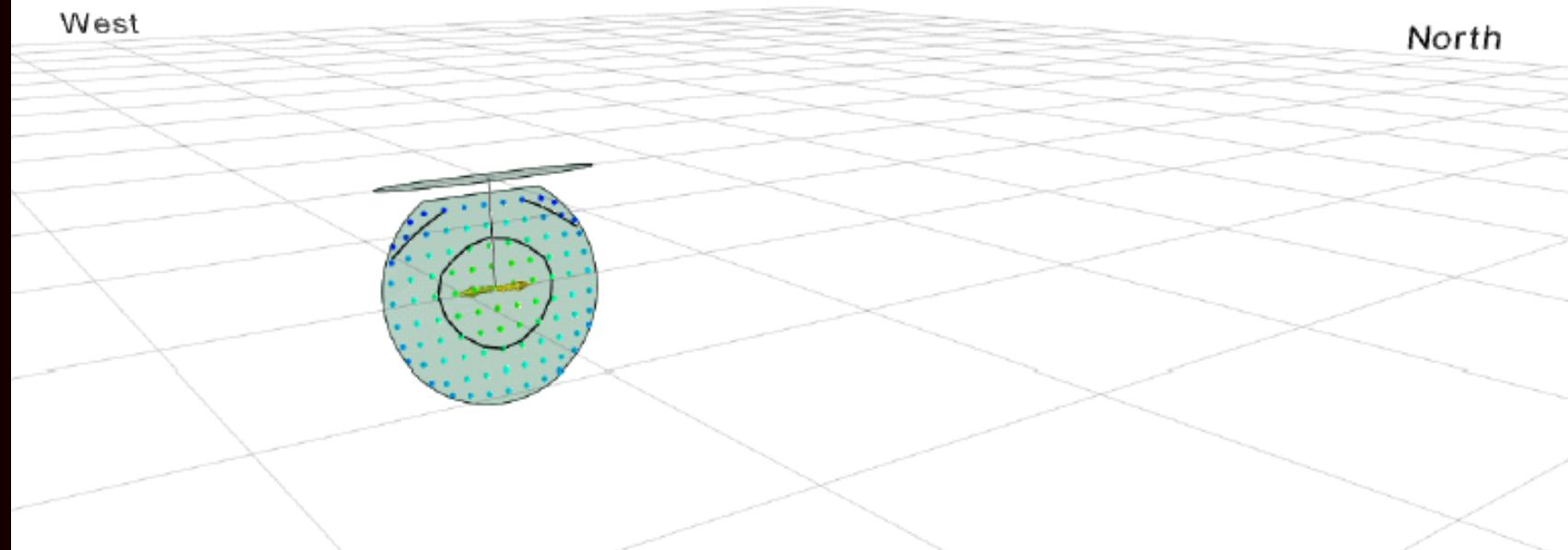
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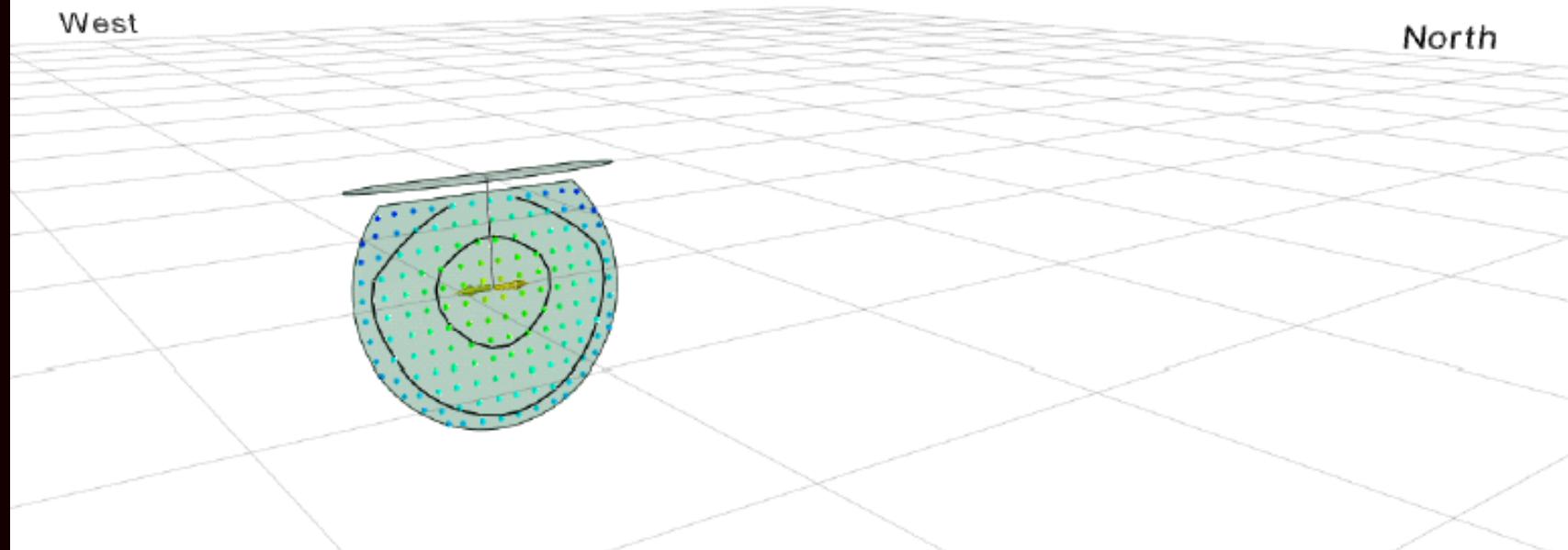
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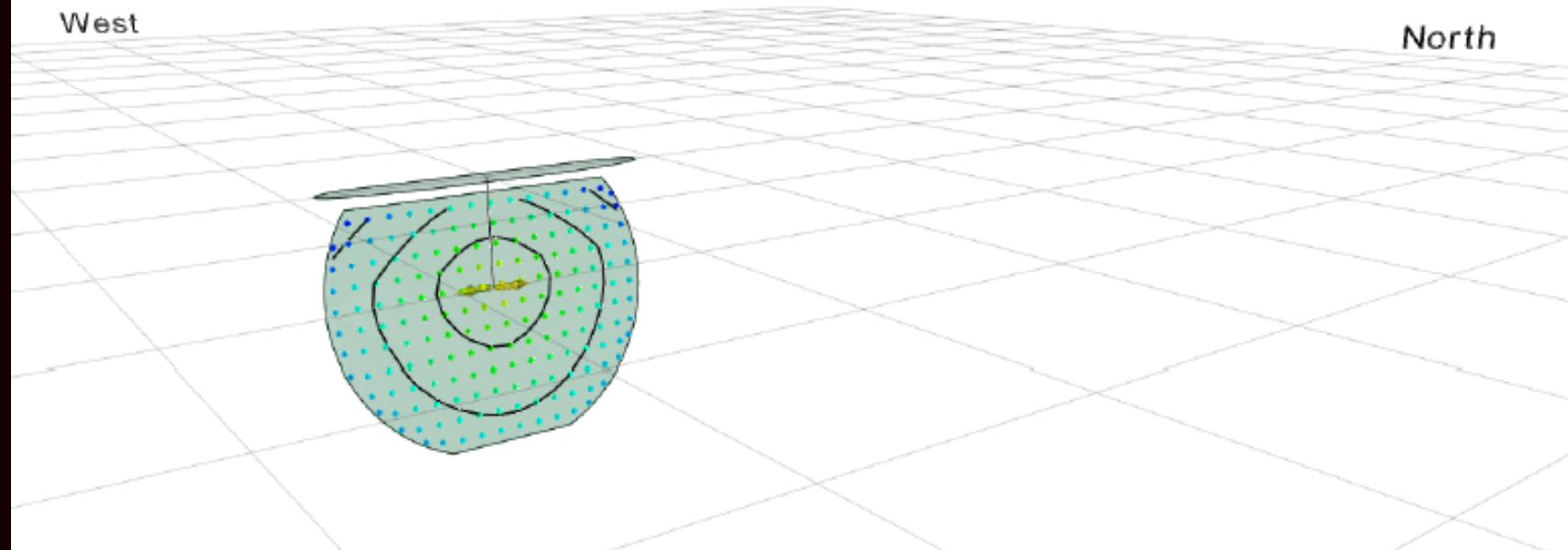
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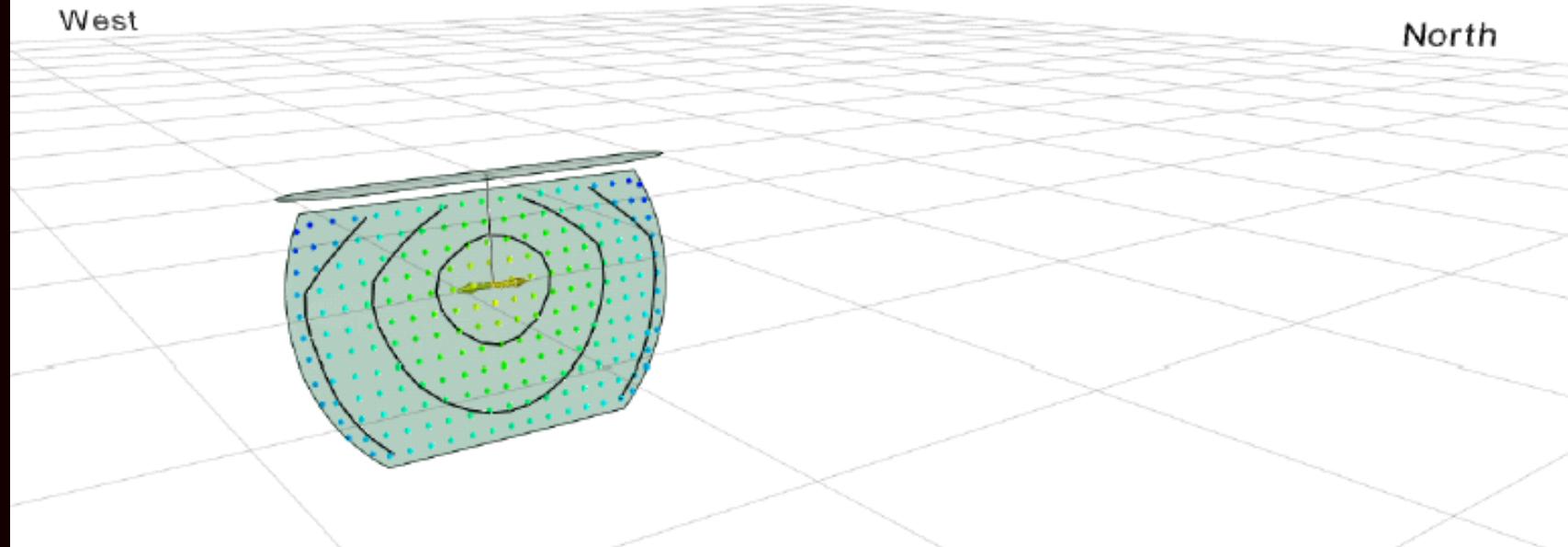
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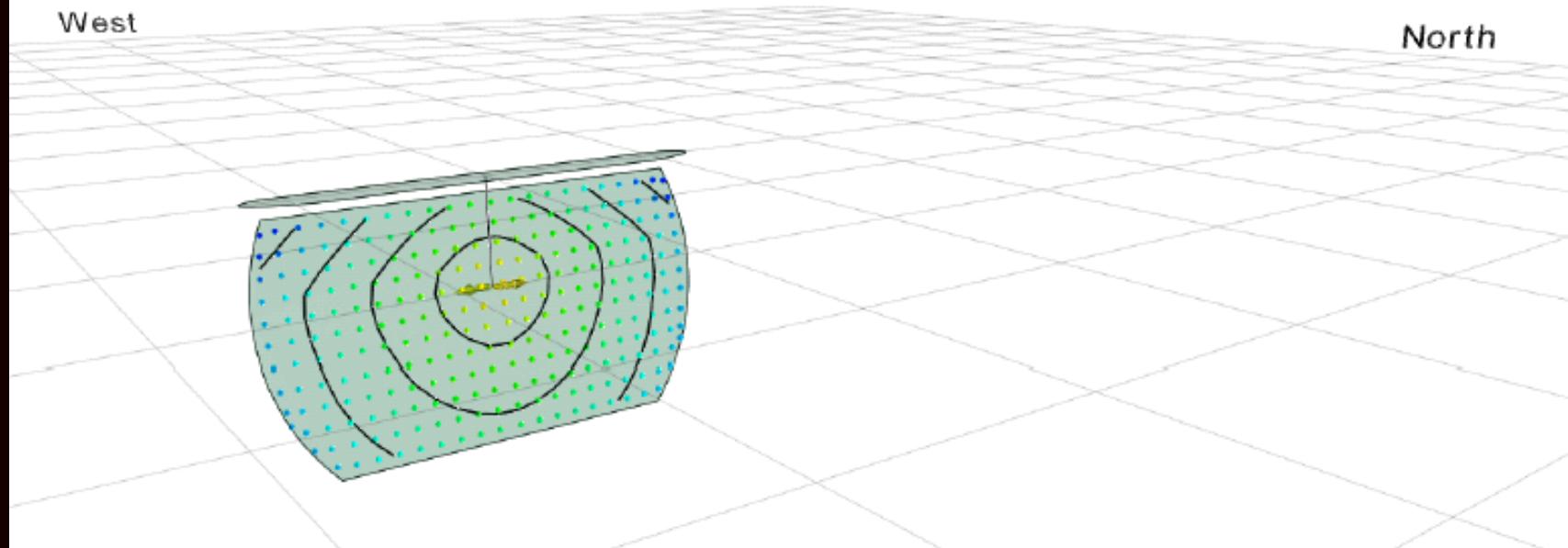
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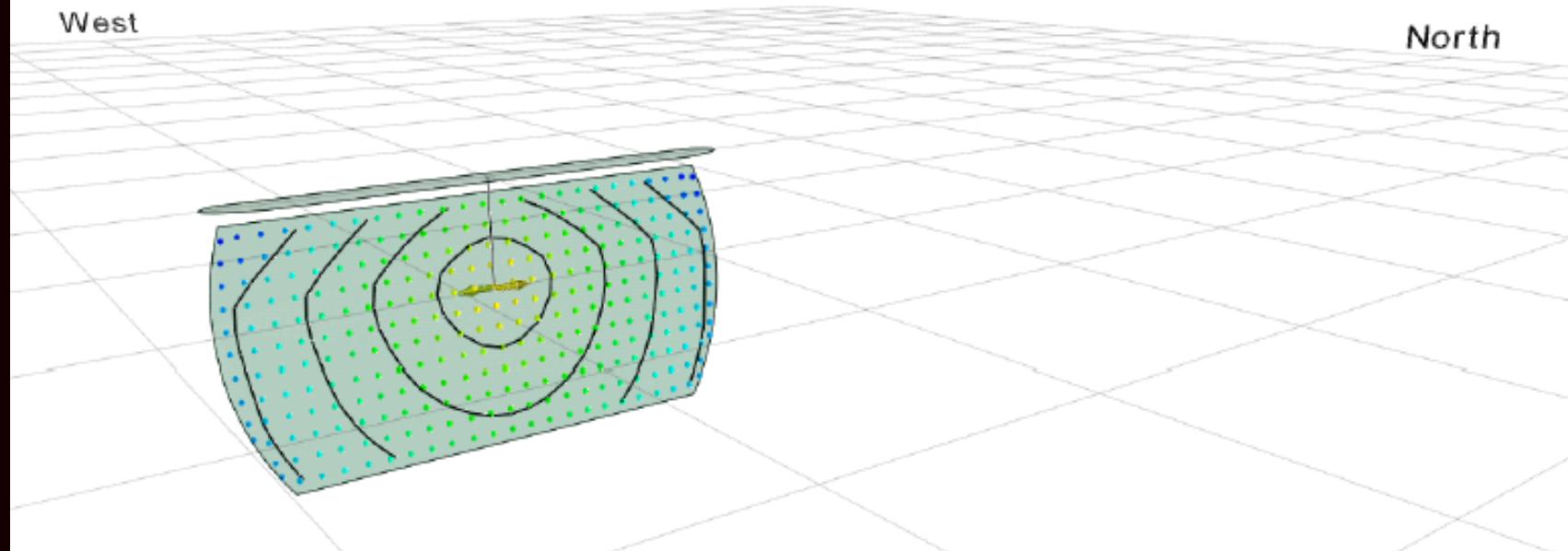
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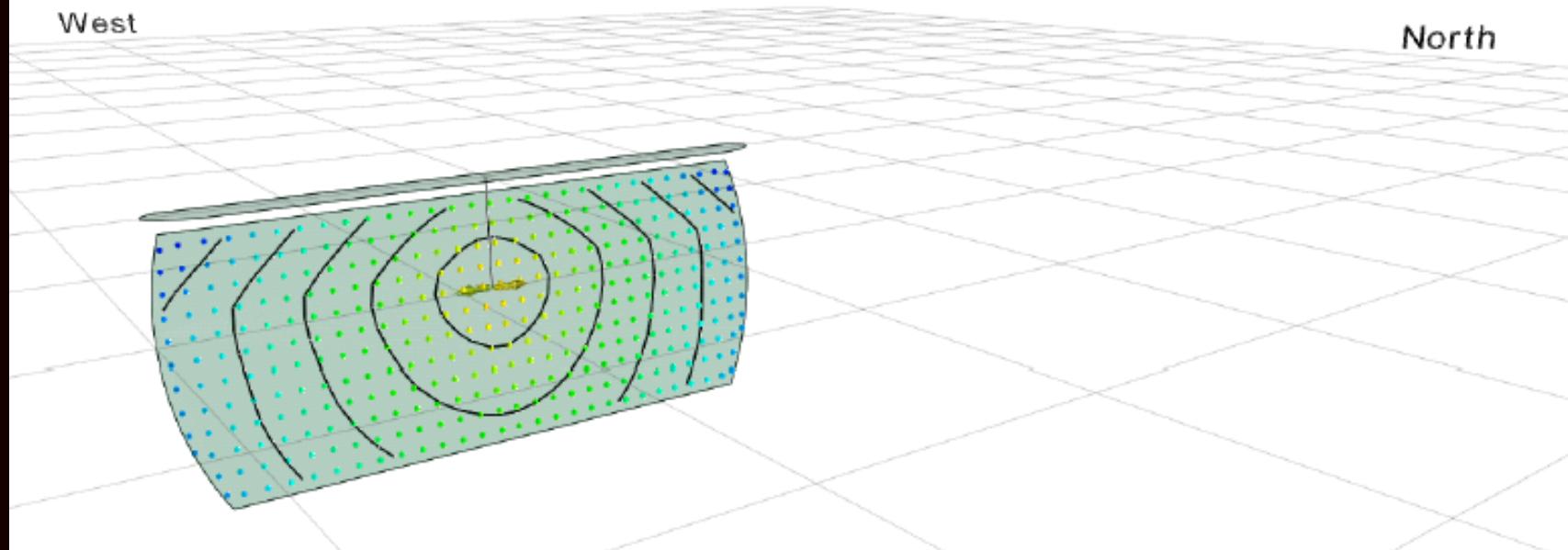
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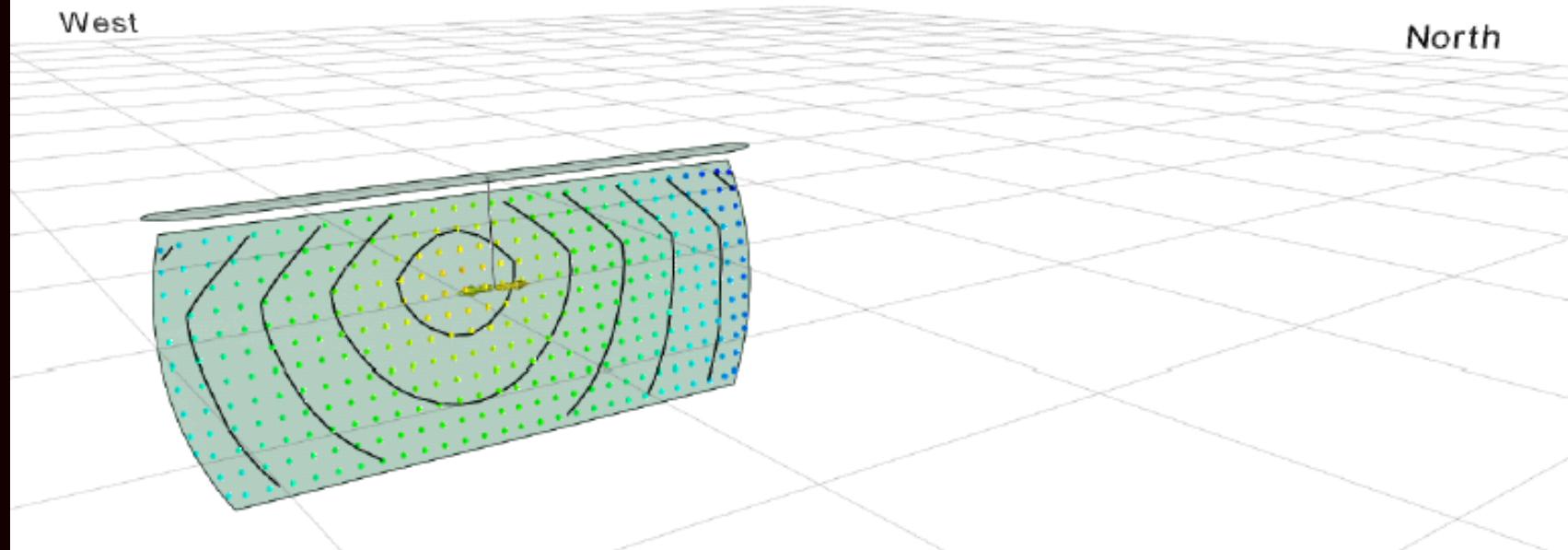
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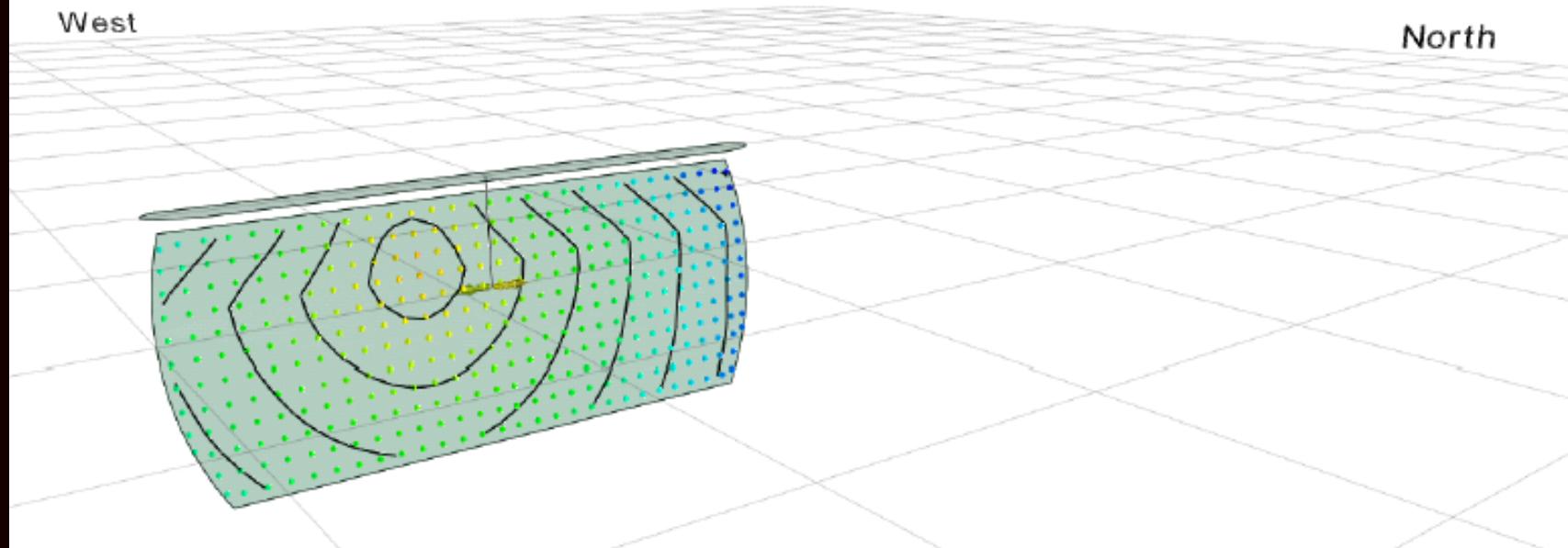
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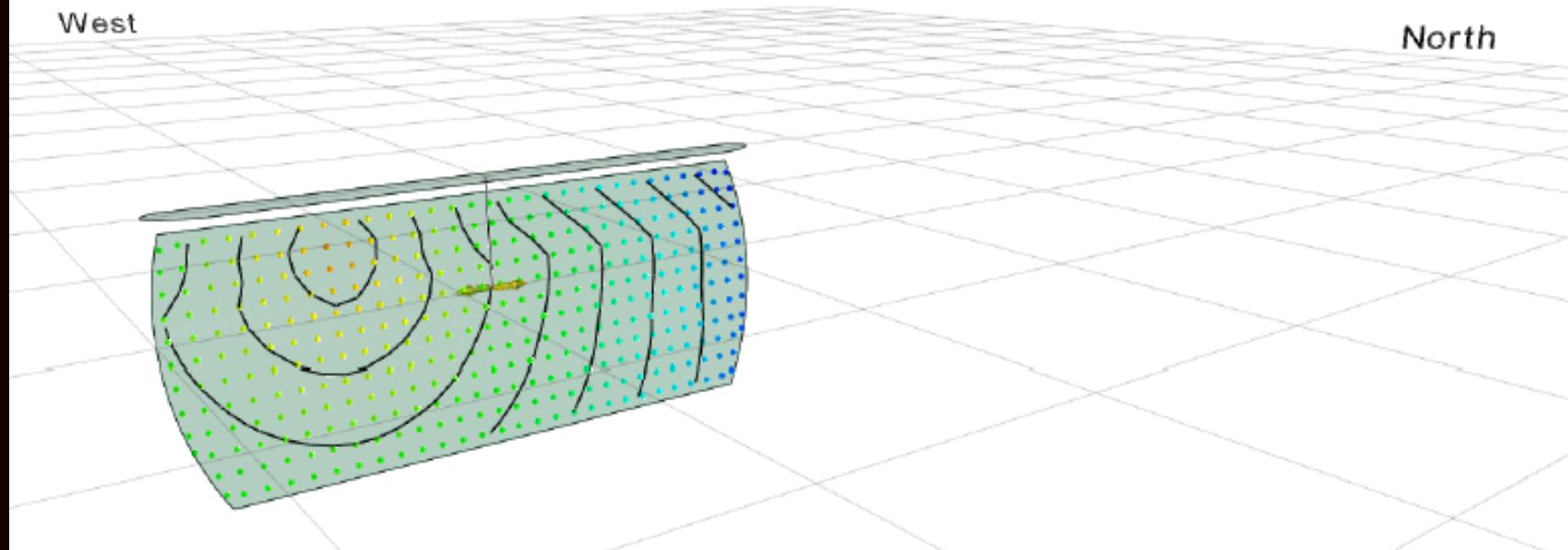
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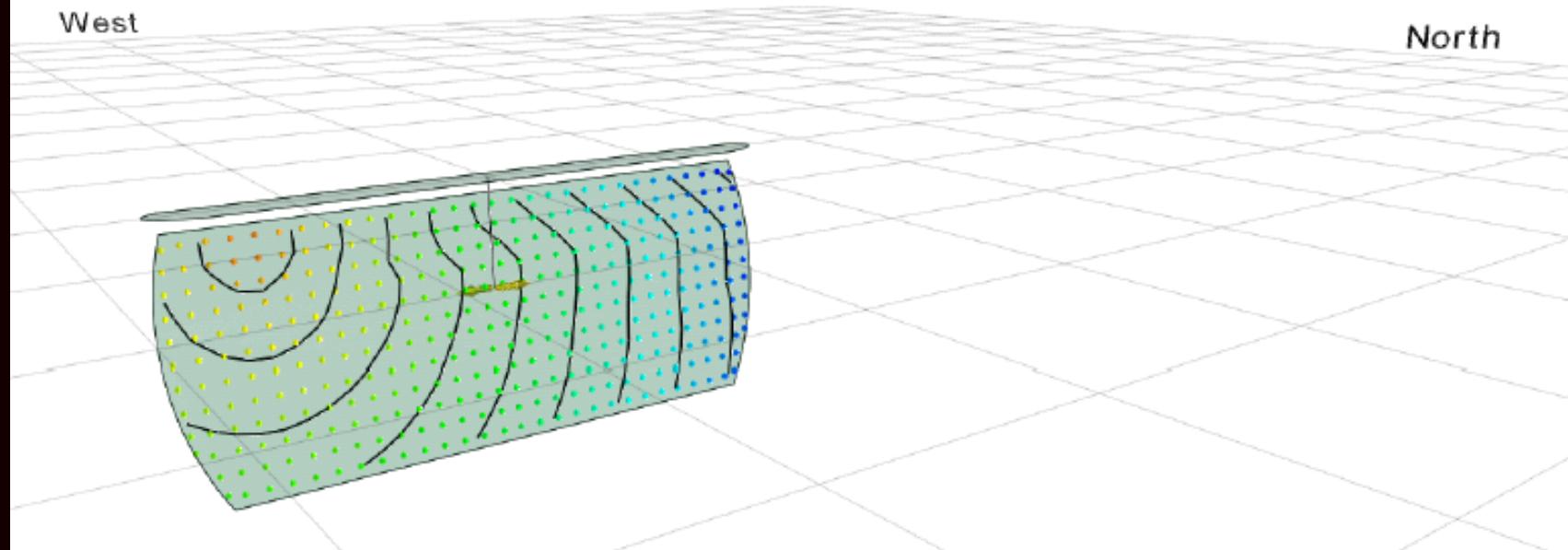
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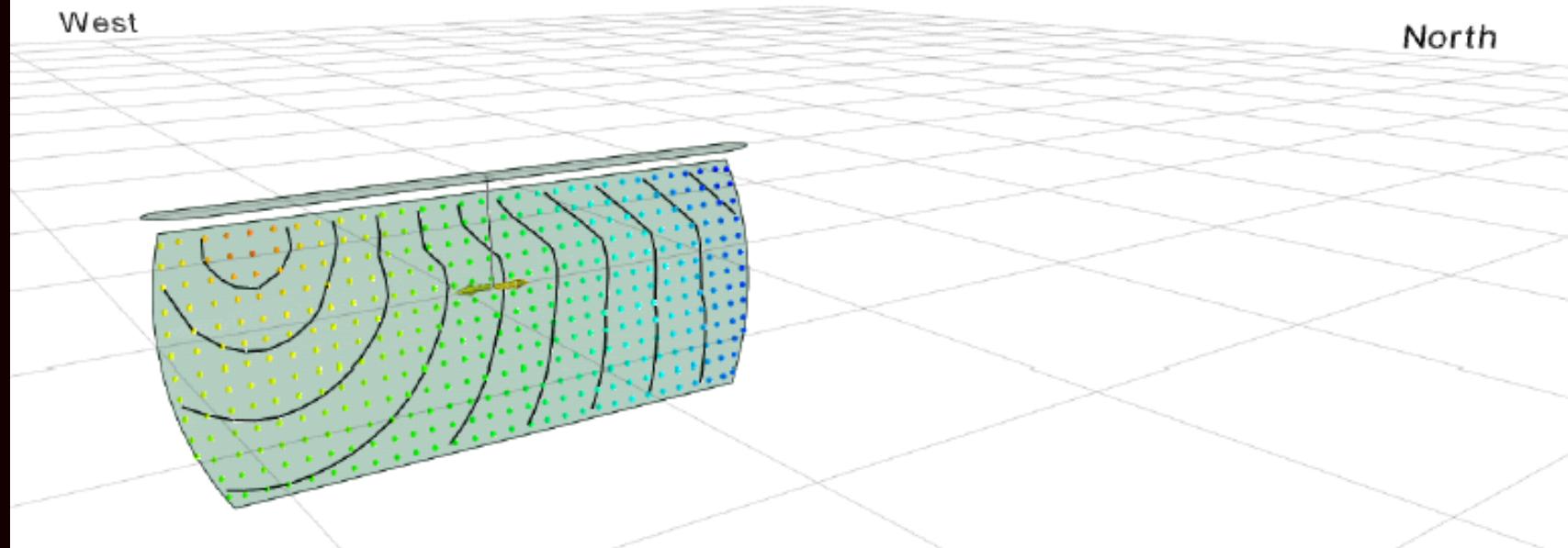
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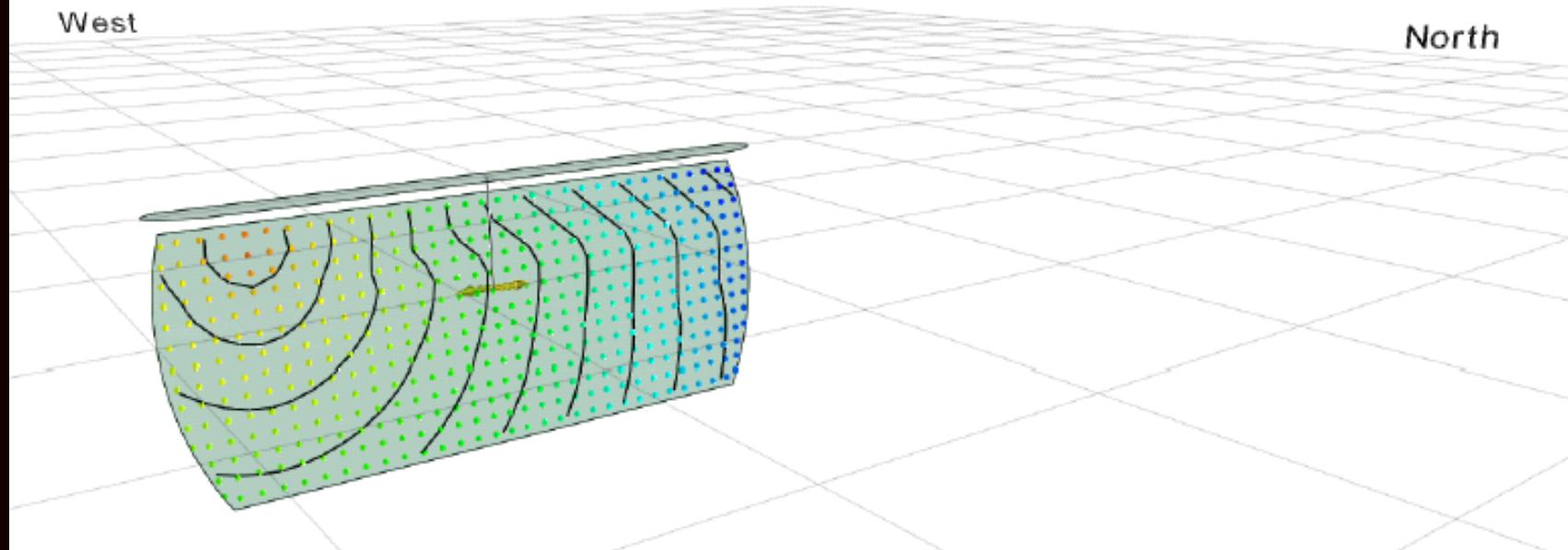
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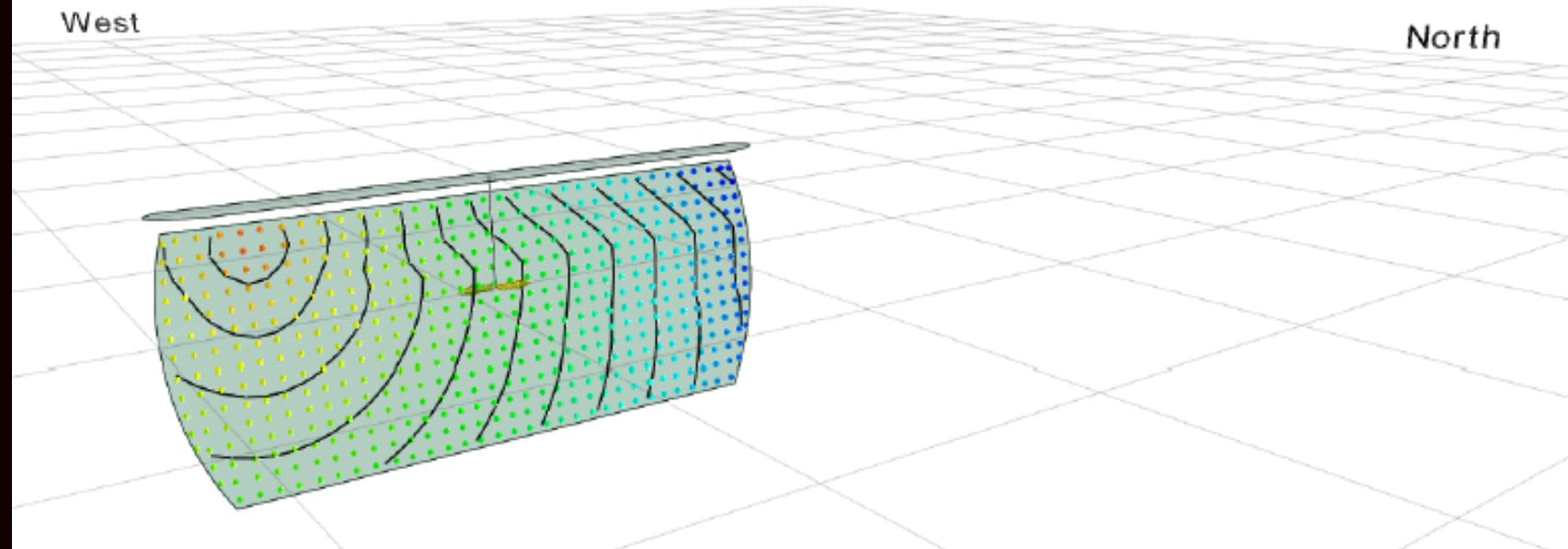
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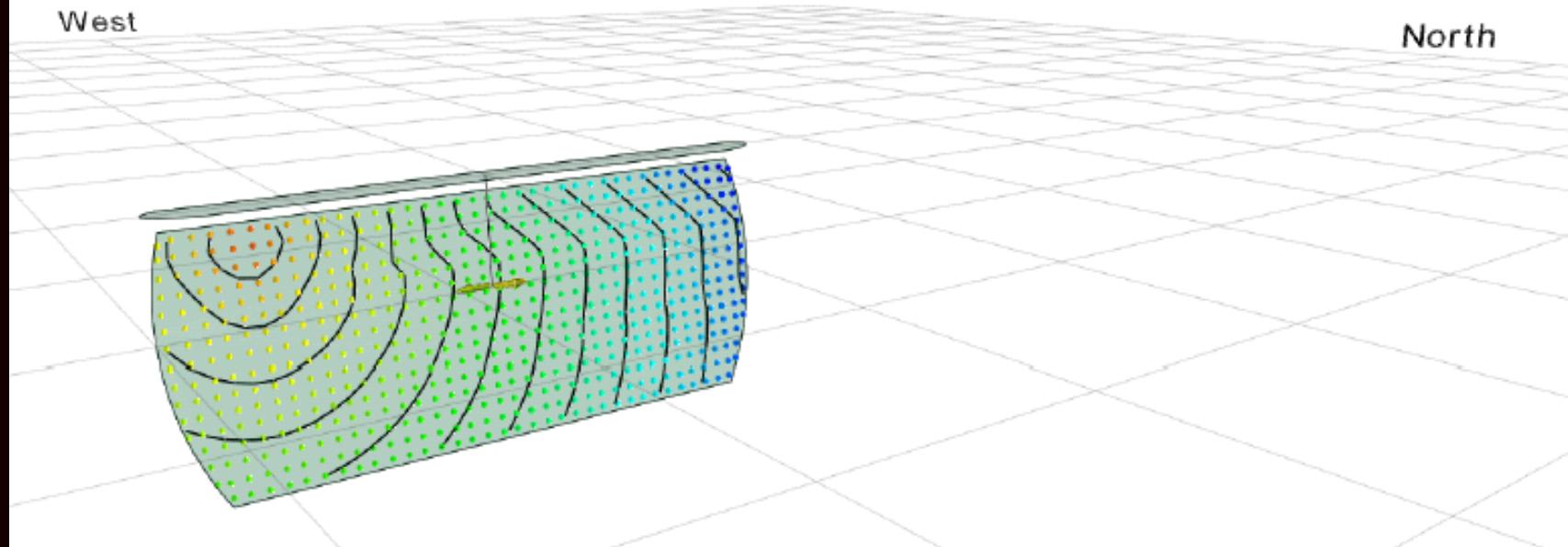
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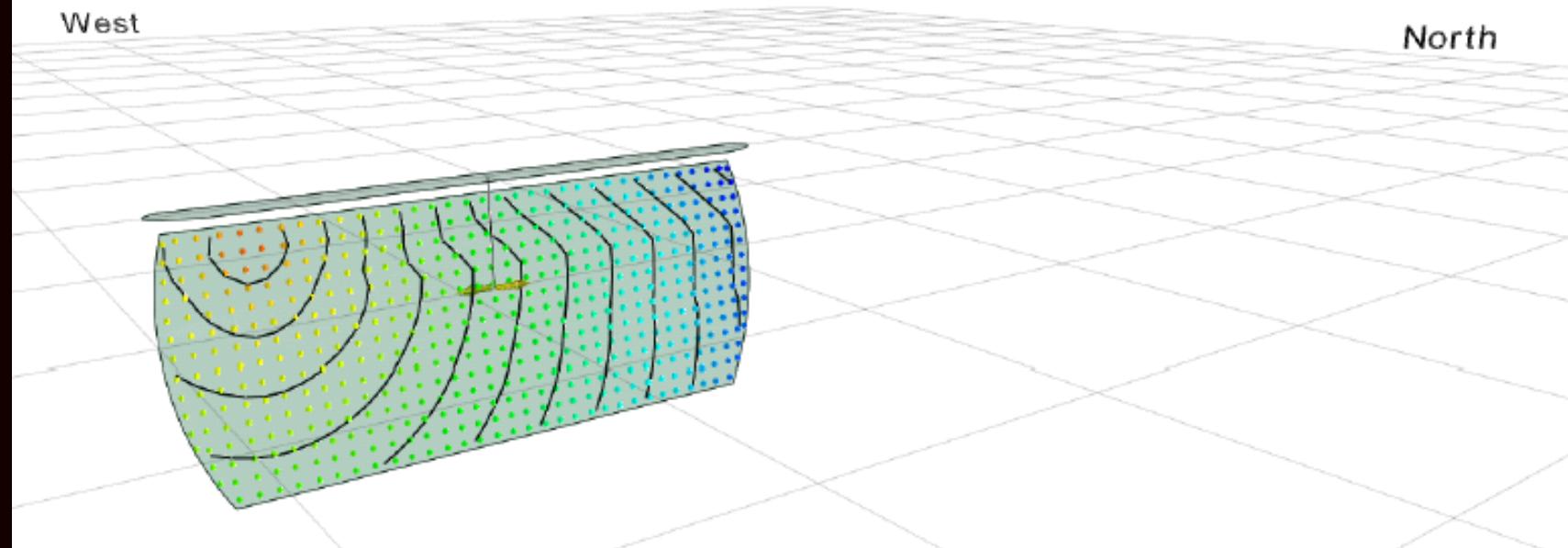
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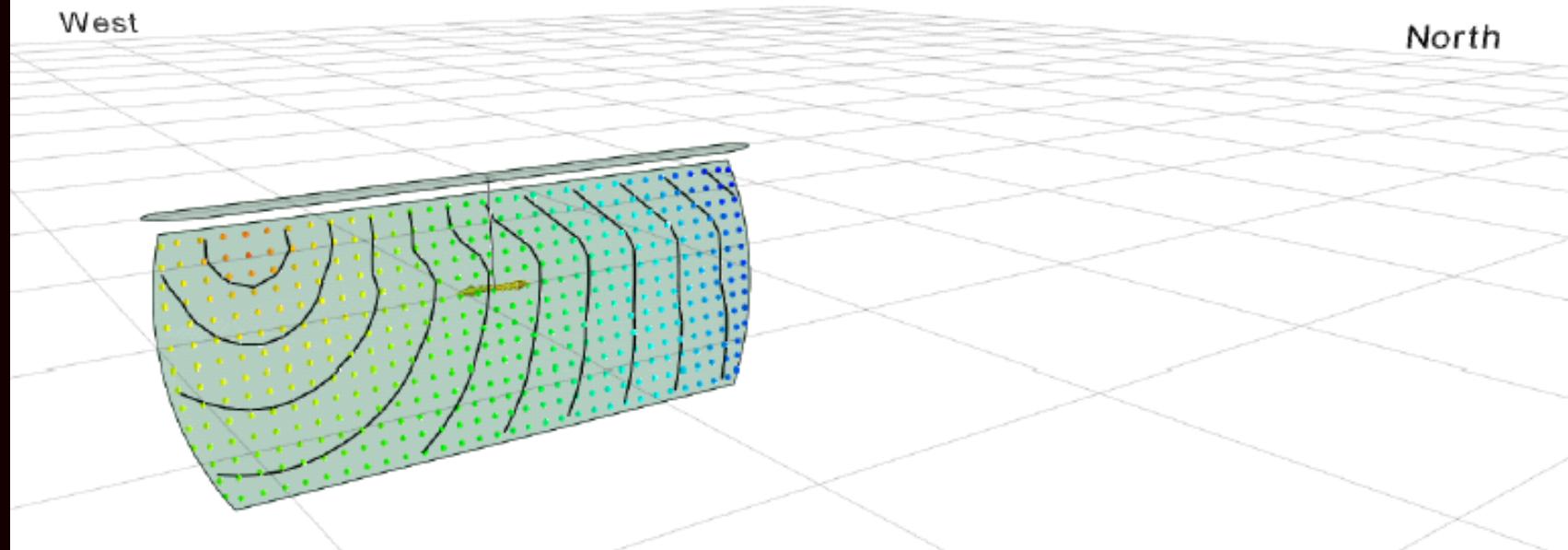
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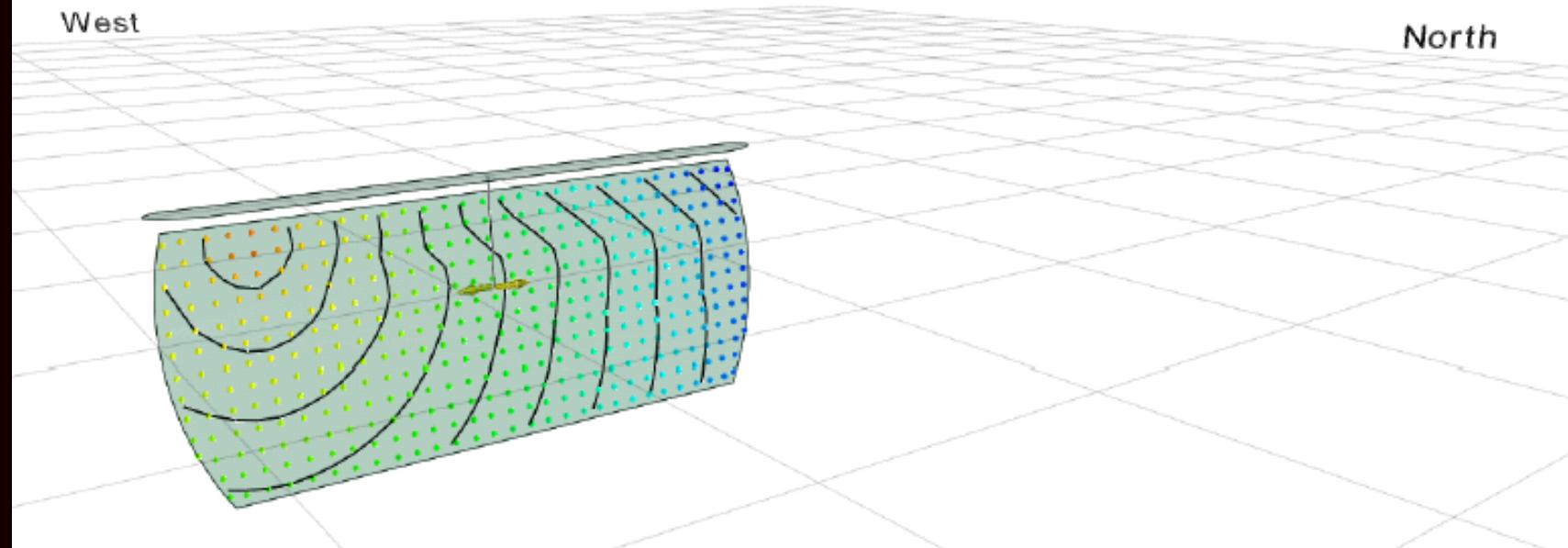
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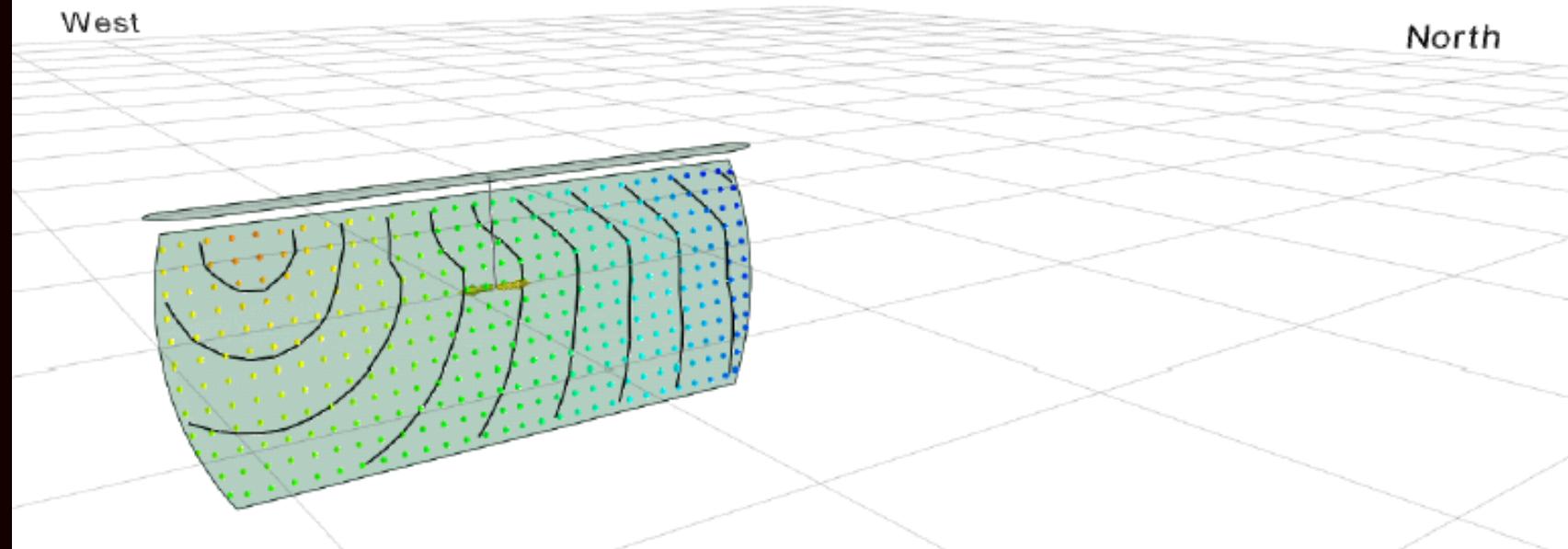
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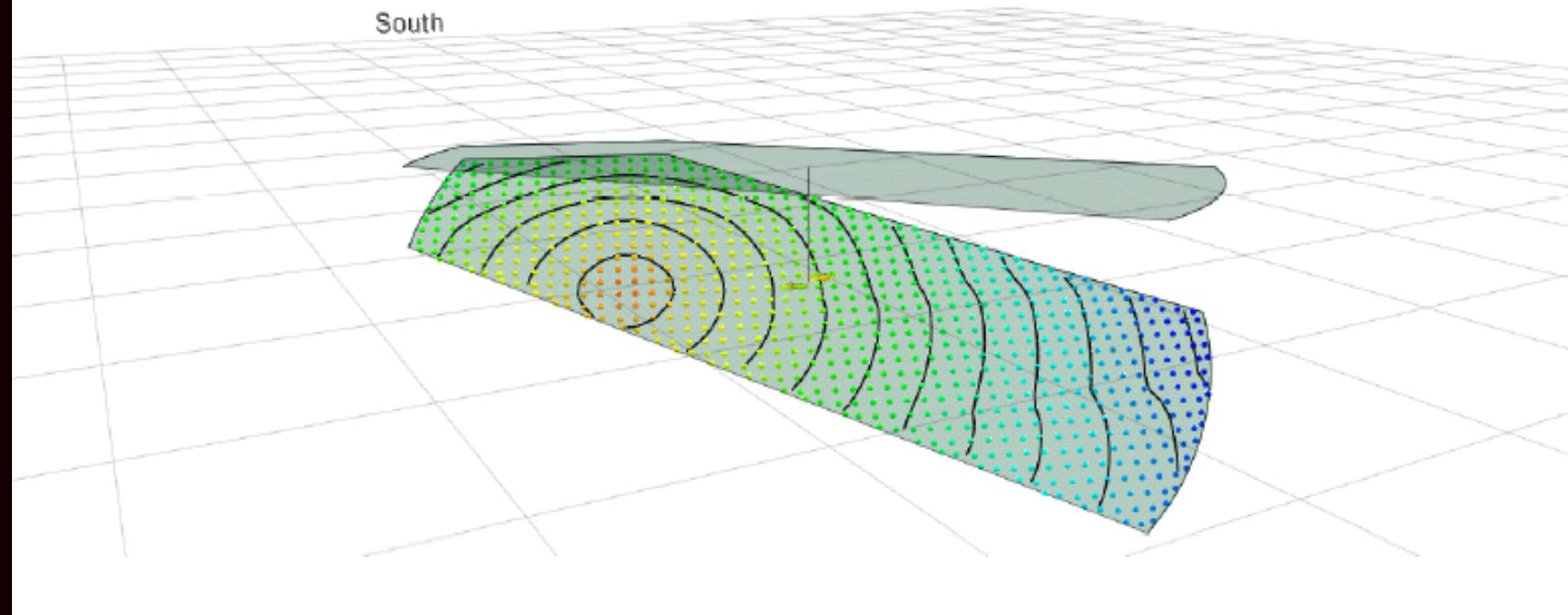
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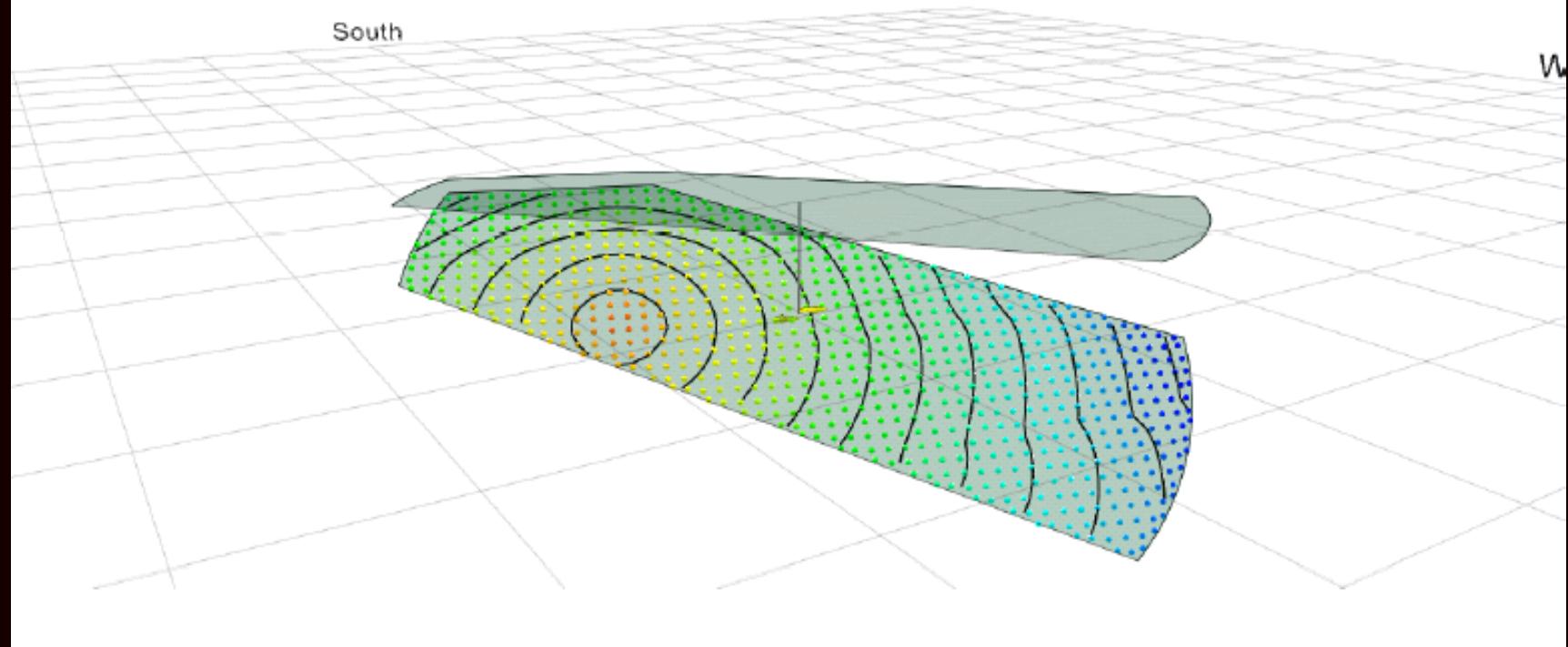
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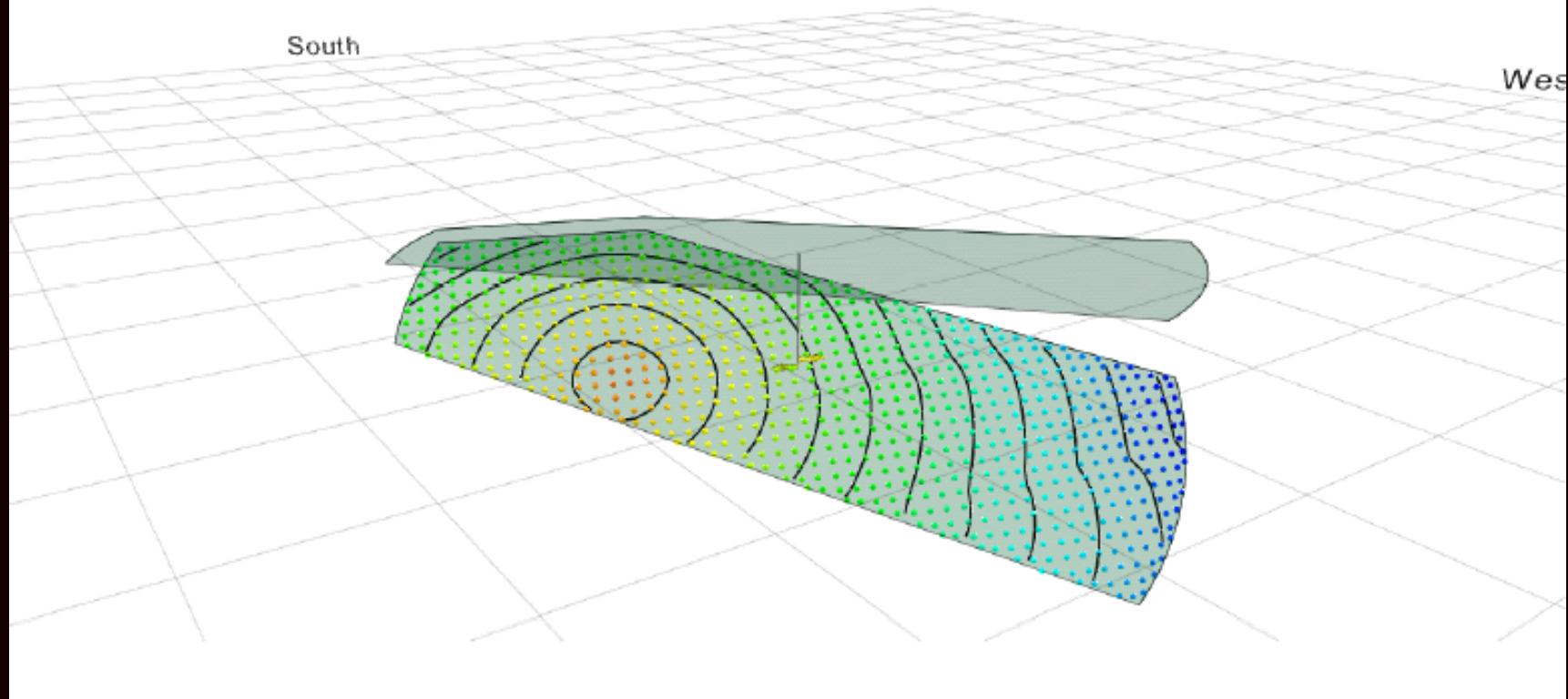
- ▶ Constraining planes enable implementation of quite complex geometries.
- ▶ E.g. the geometry of a subduction slab could be given.



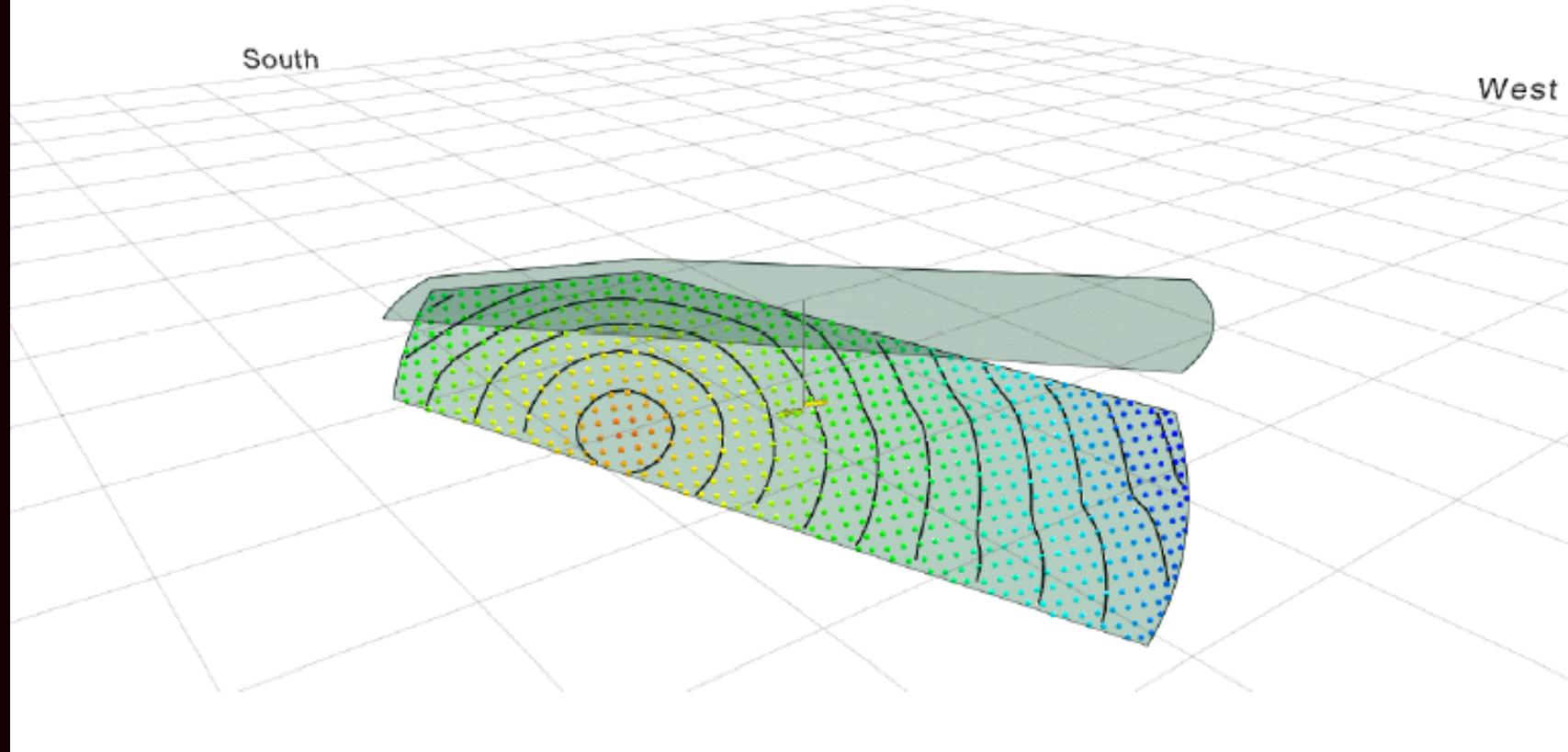
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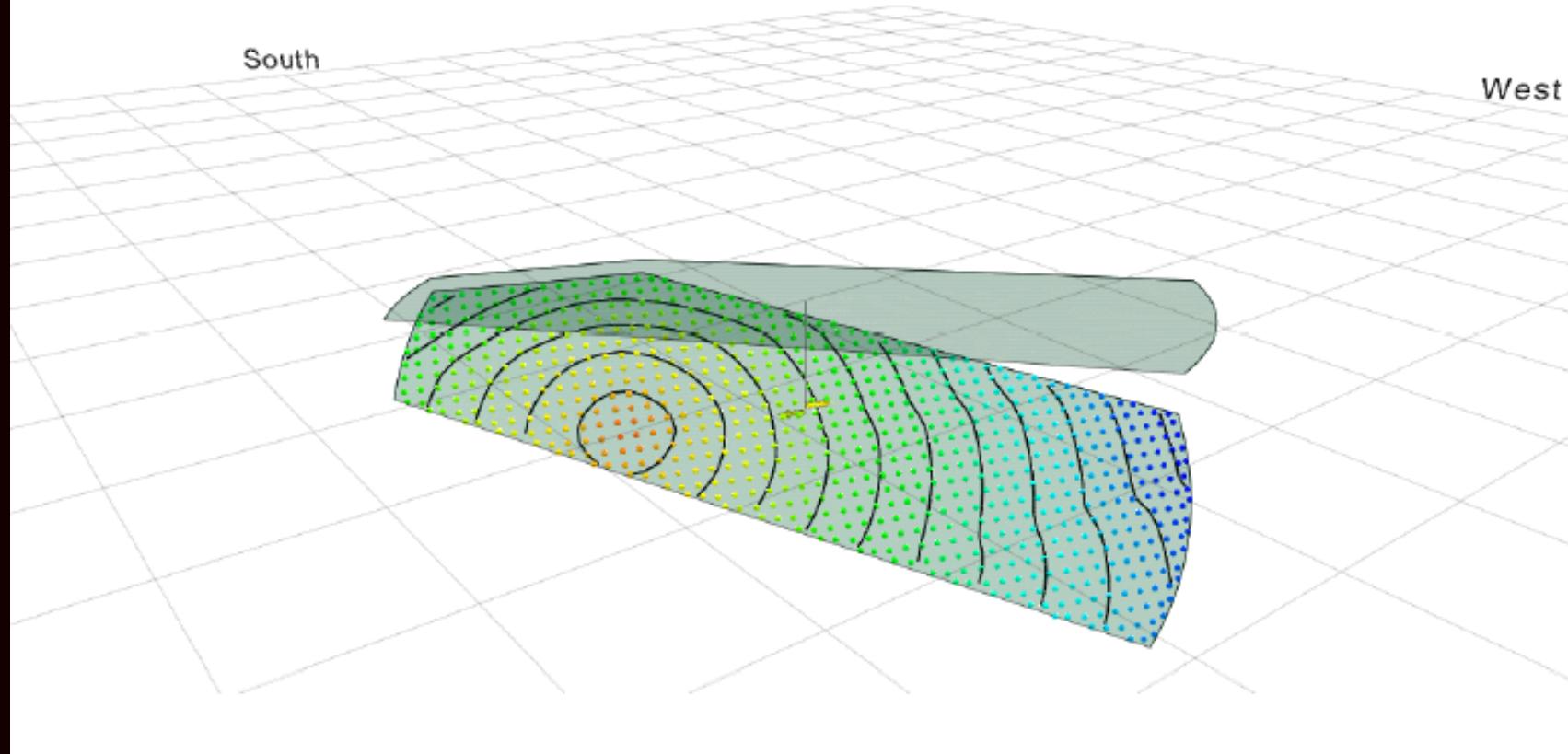
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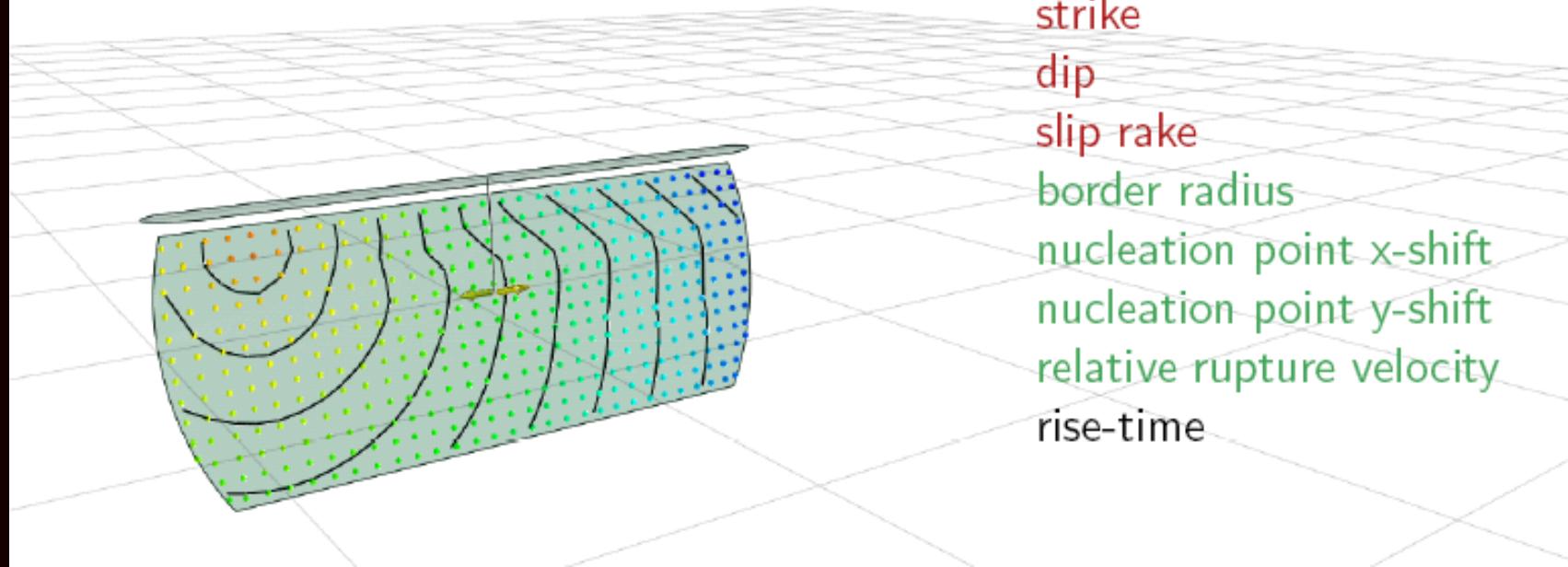


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- ▶ E.g. the geometry of a subduction slab could be given.



Despite its flexibility the eikonal source model is described by only 13 parameters.

(Considering constraints and earth model as fixed and known. :-)



13 parameters:

time

north-shift

east-shift

depth

moment

strike

dip

slip rake

border radius

nucleation point x-shift

nucleation point y-shift

relative rupture velocity

rise-time

The eikonal source model, only 13 parameters

Circular area, plus constraints

Rupture velocity scales with shear velocity

Despite its flexibility, the eikonal source model is described by only 13 parameters (considering constraints and earth model as fixed and known)

13 parameters:

time

north-shift

east-shift

depth

moment

strike

dip

slip rake

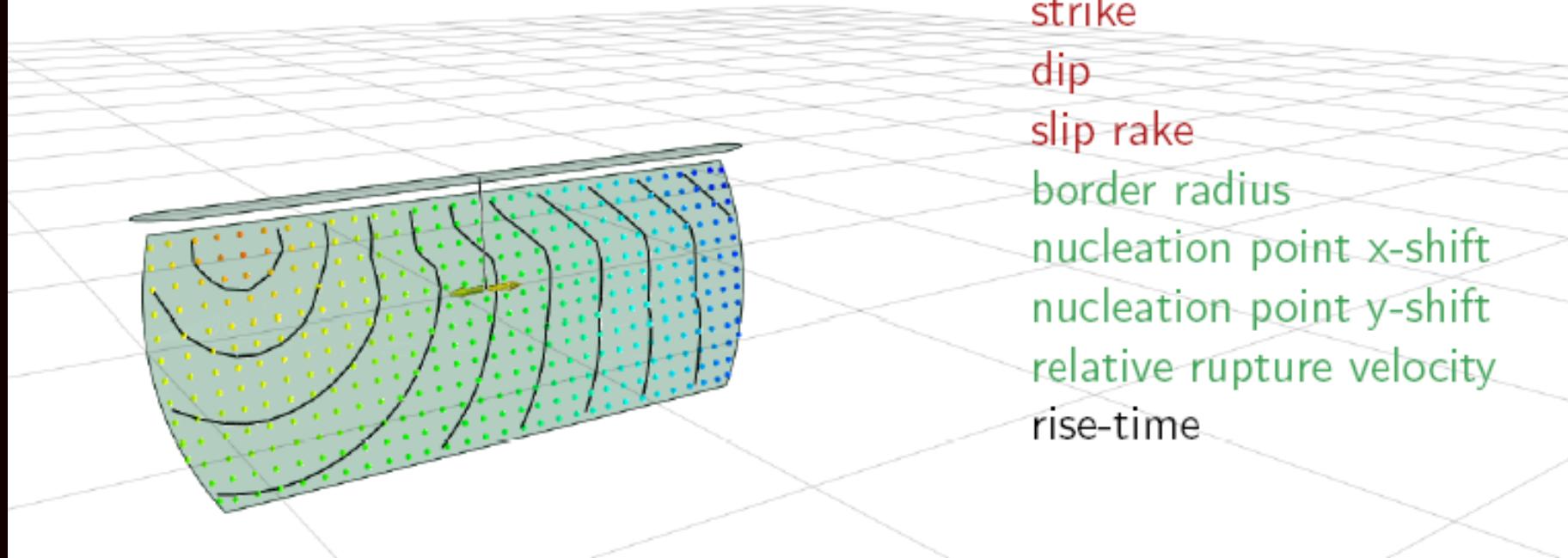
border radius

nucleation point x-shift

nucleation point y-shift

relative rupture velocity

rise-time



Heimann 2011

Source model parameters and inversion priorities

Source model parameters (13)

Time Lat Lon Depth M_0 Strike Dip Rake Rad NucX NucY RuptV RiseT

General source description

Source location

Radiation pattern

Rupture process

Scale of source model

Point source

Finite source

Information from data

Low frequencies

High frequencies

Inversion priority

Step 1, 2

Step 3



Inversion strategy

Time Lat Lon Depth M_0



Step 1, Focal mechanism (DC and full moment tensor)

amplitude spectra inversion

Depth M_0 Strike Dip Rake

Inversion strategy

Time Lat Lon Depth M_0



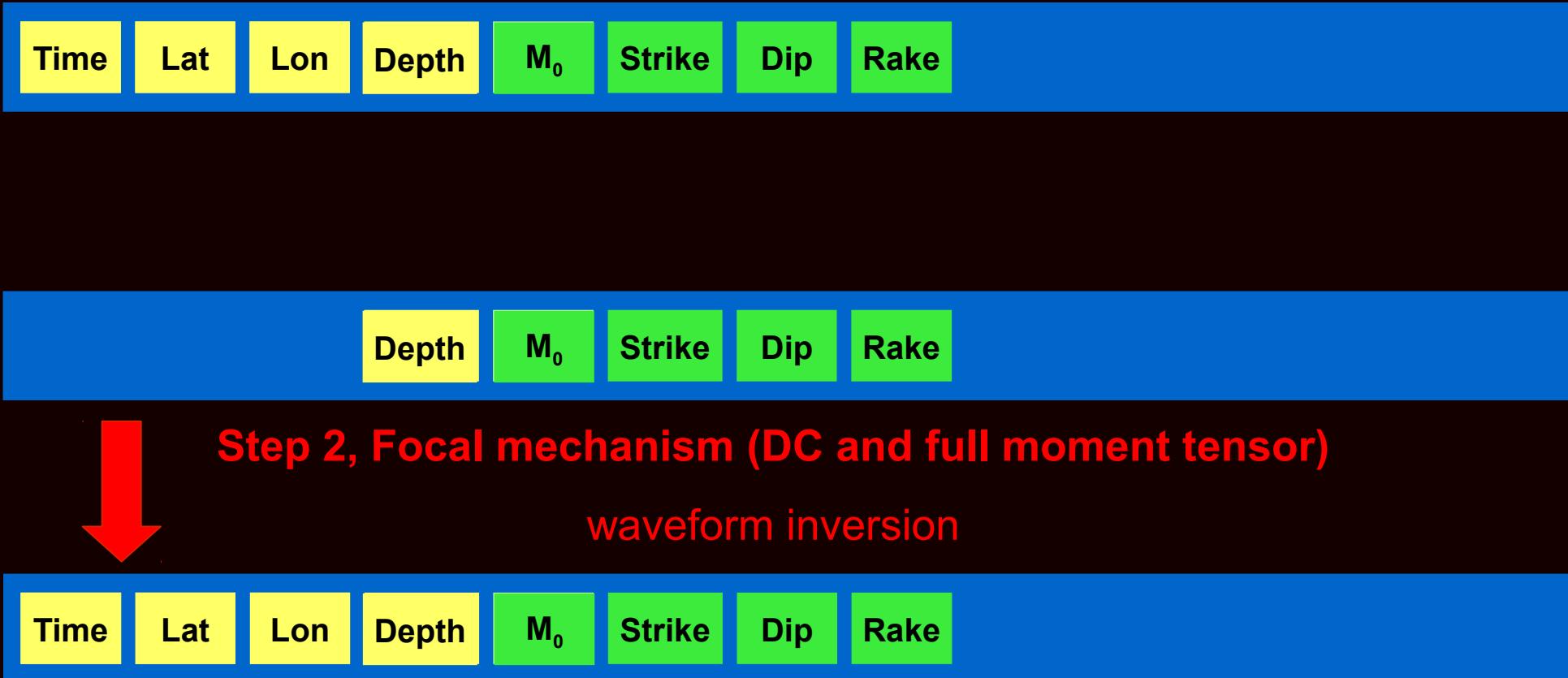
Step 1b, Full moment tensor

amplitude spectra inversion

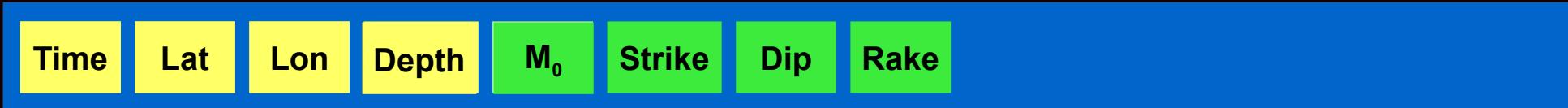
Depth M_0 Strike Dip Rake

Depth M_{xx} M_{yy} M_{zz} M_{xy} M_{xz} M_{yz}

Inversion strategy



Inversion strategy

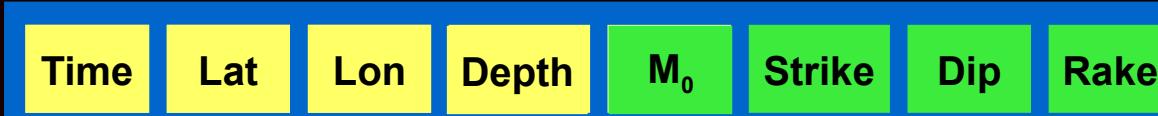


Step 2b, Full moment tensor

waveform inversion

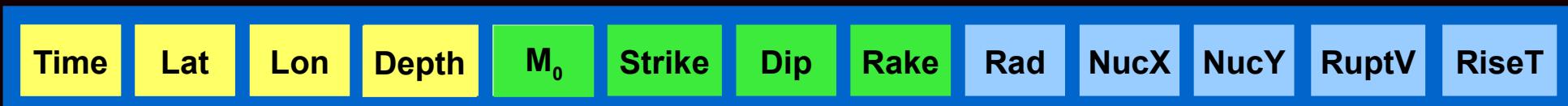


Inversion strategy



Step 3, Kinematic source model

amplitude spectra inversion (incl. higher frequencies)



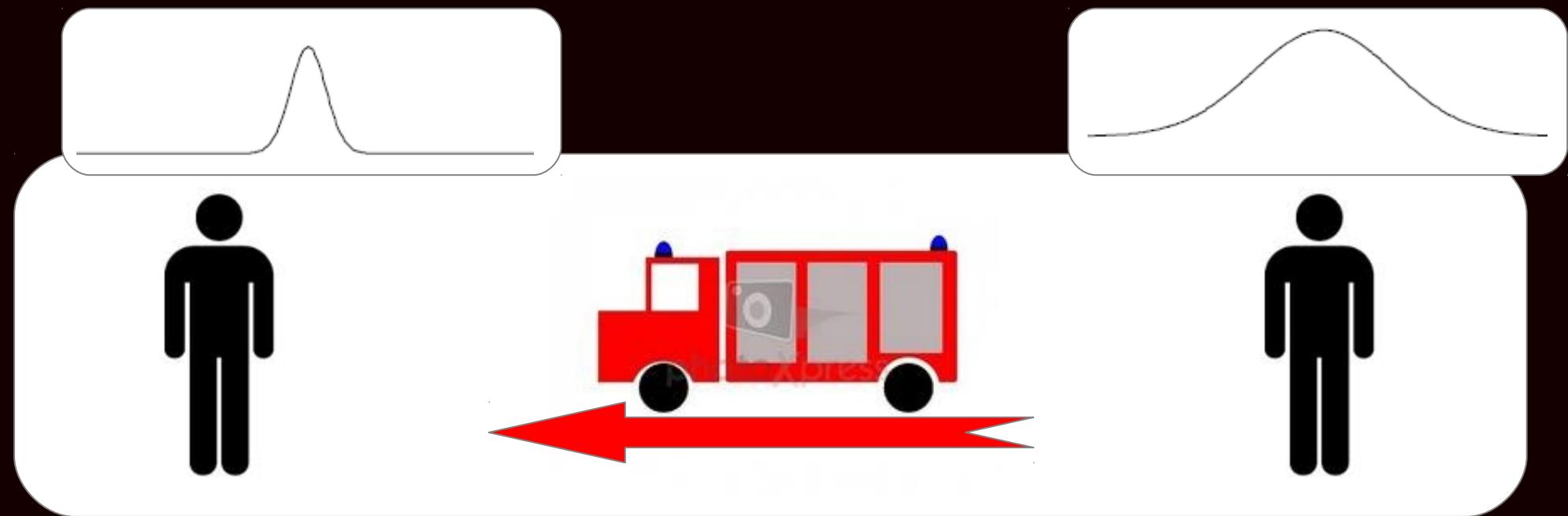
Fast directivity detection

A simplified, but fast, alternative approach

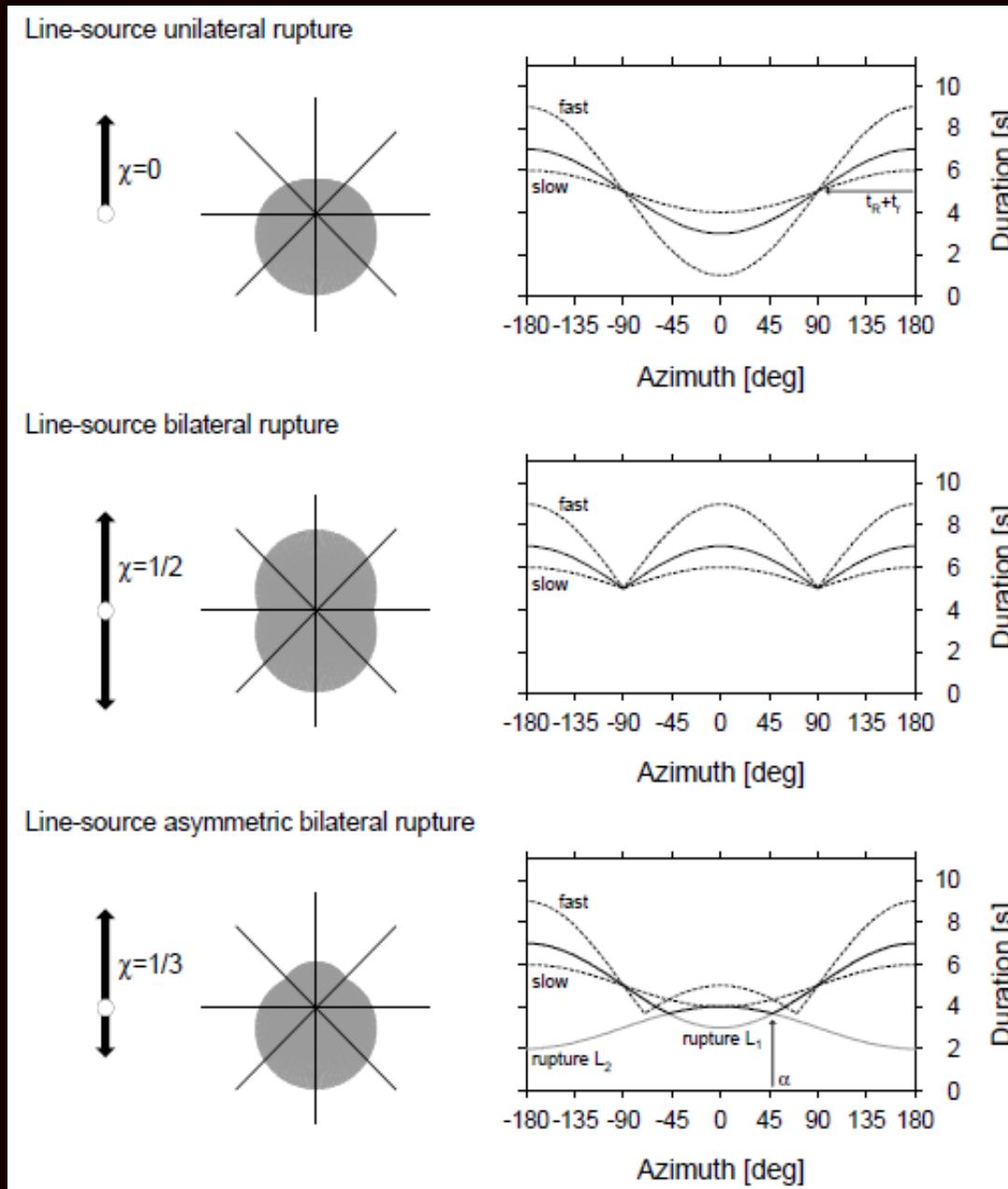
Spatial point source approximation

Apparent STF duration at single station

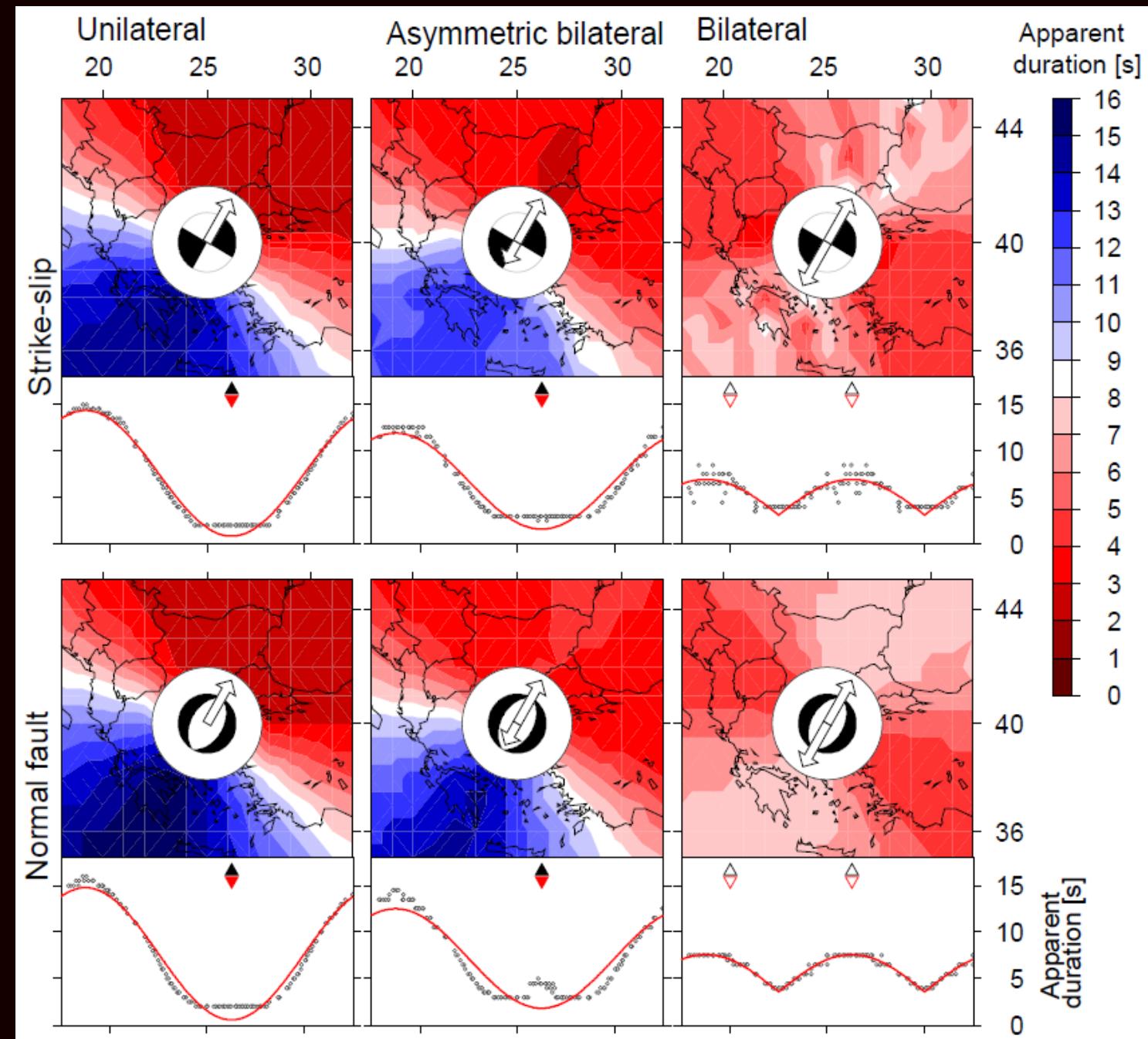
Azimuthal variation of apparent STF



Fast directivity detection

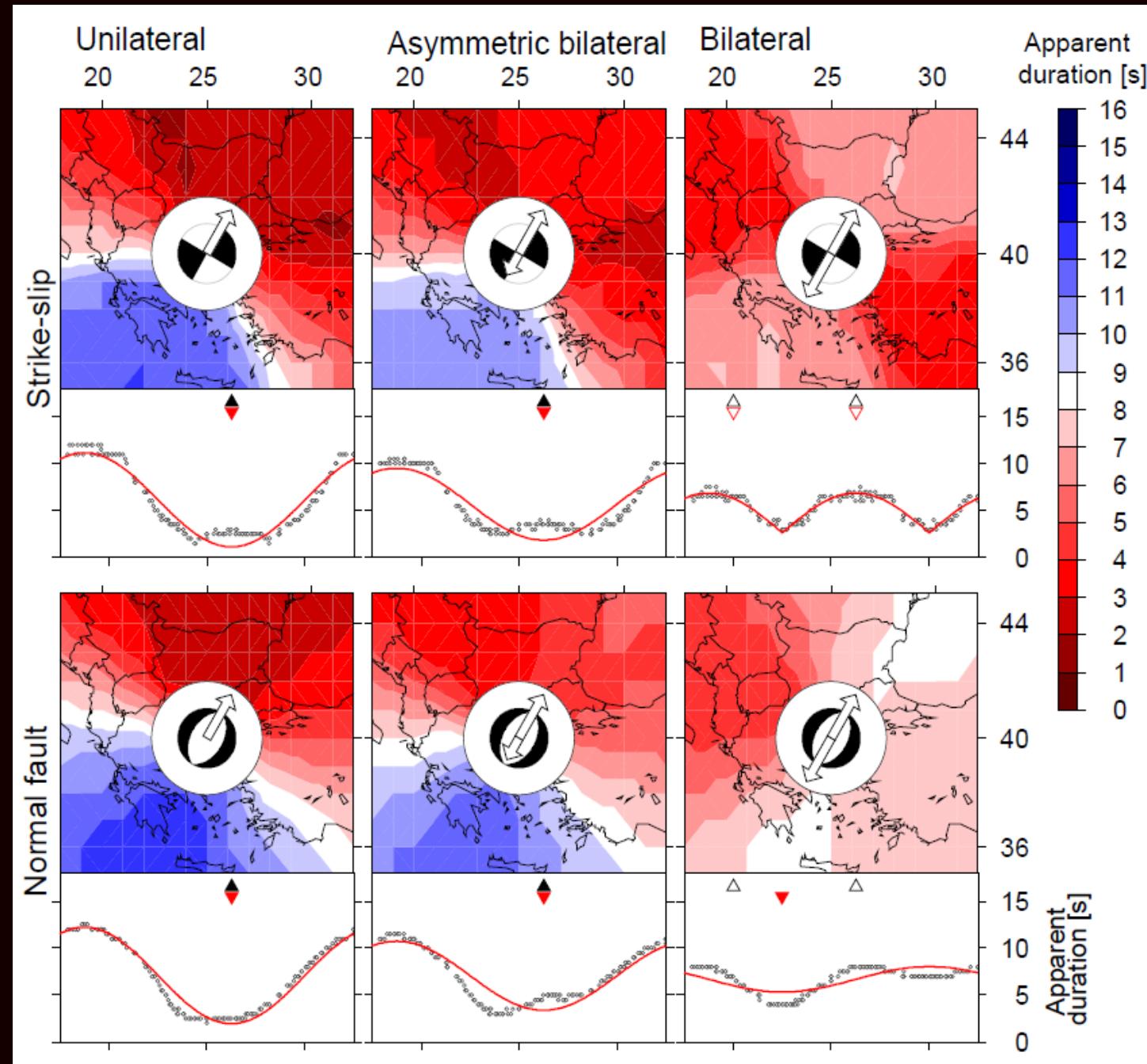


Cesca et al.
J. Seismol. 2011

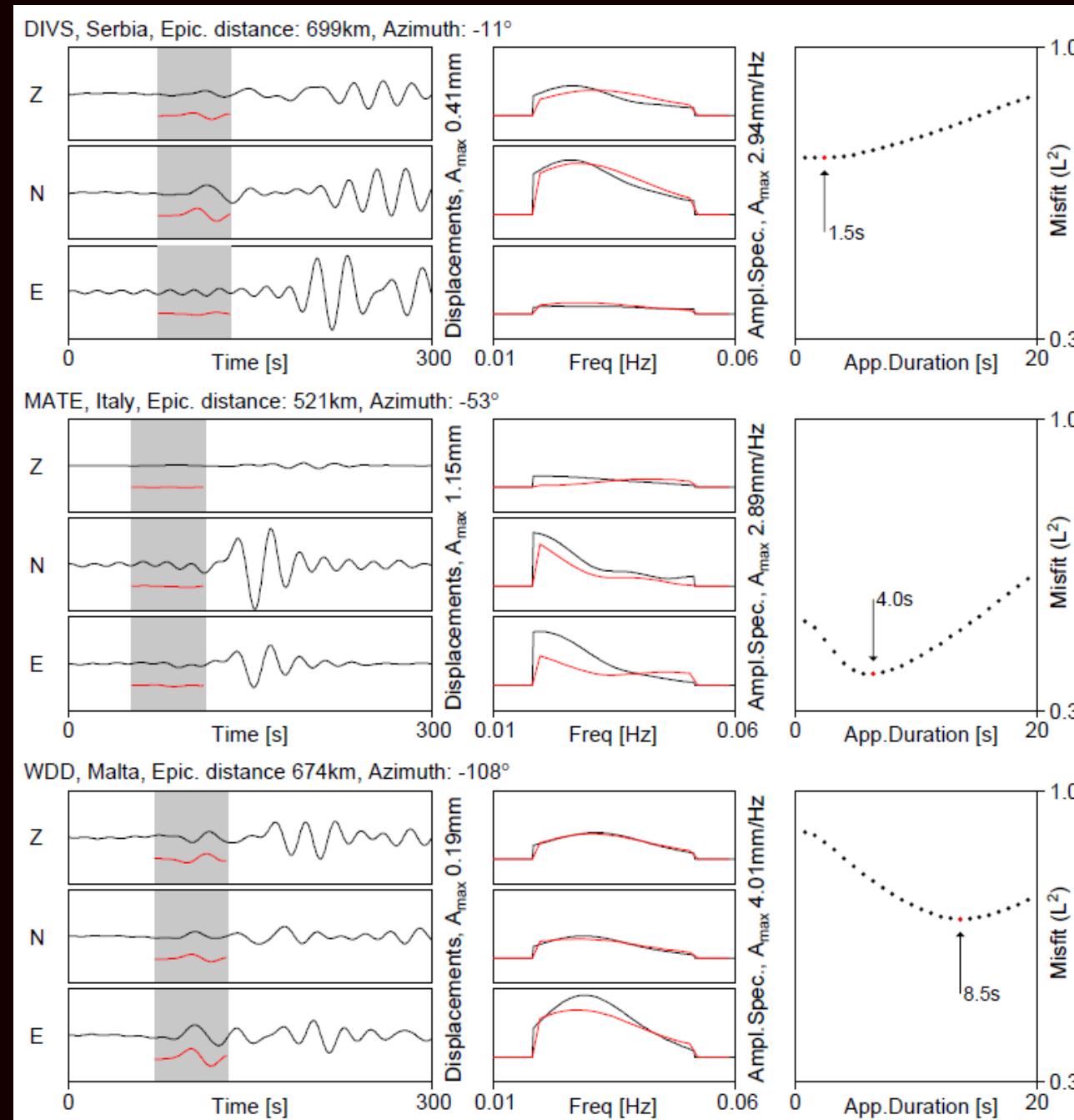


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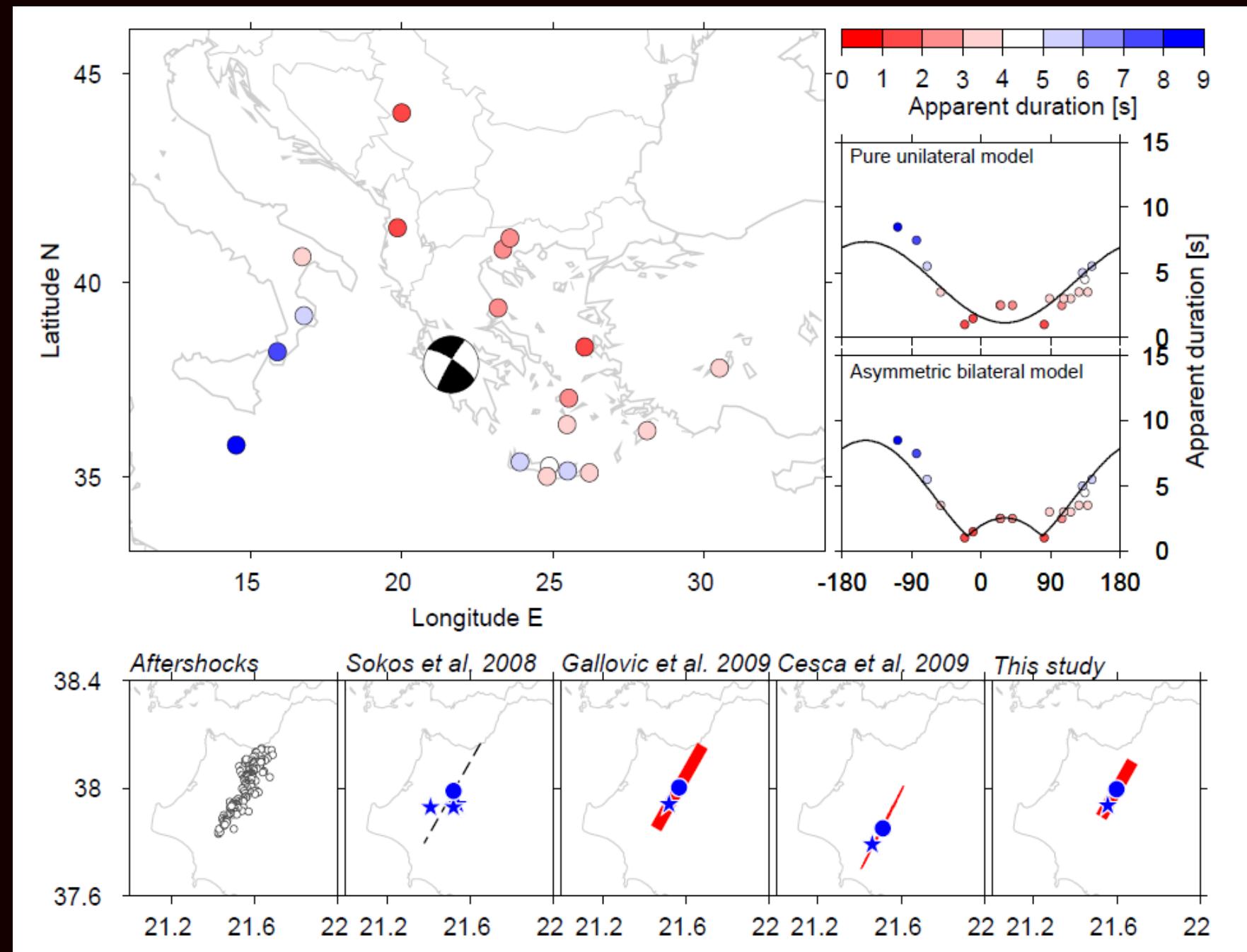


Fast directivity detection



Cesca et al.
J. Seismol. 2011





Inversion tips



Time vs. Frequency domain

Time domain inversion

Widely used at regional and teleseismic distances

Sensitive to traces alignment

Unstable at higher frequencies, for simplified velocity models

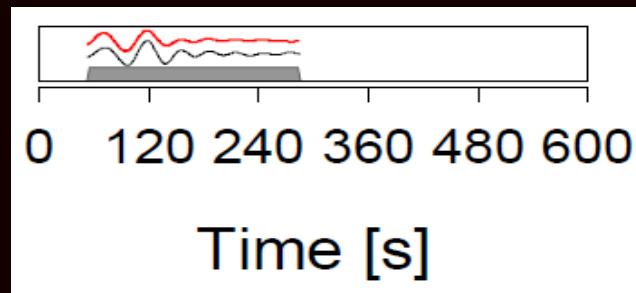
Frequency domain (amplitude spectra) inversion

- Less sensitive to traces alignment, wave propagation mismodeling
- Implicit polarity ambiguity

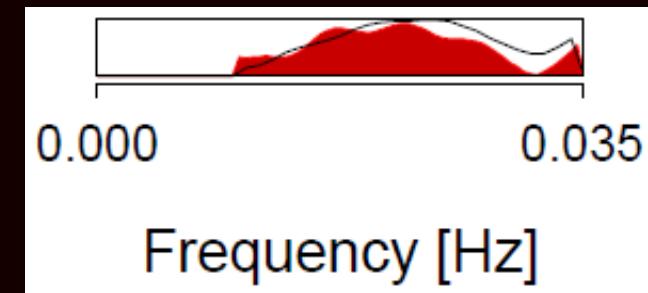


Time vs. Frequency domain

Time domain inversion



Frequency domain

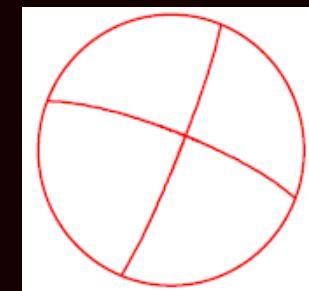


Time domain inversion

- Widely used at regional and teleseismic distances
- Sensitive to traces alignment
- Unstable at higher frequencies, for simplified velocity models

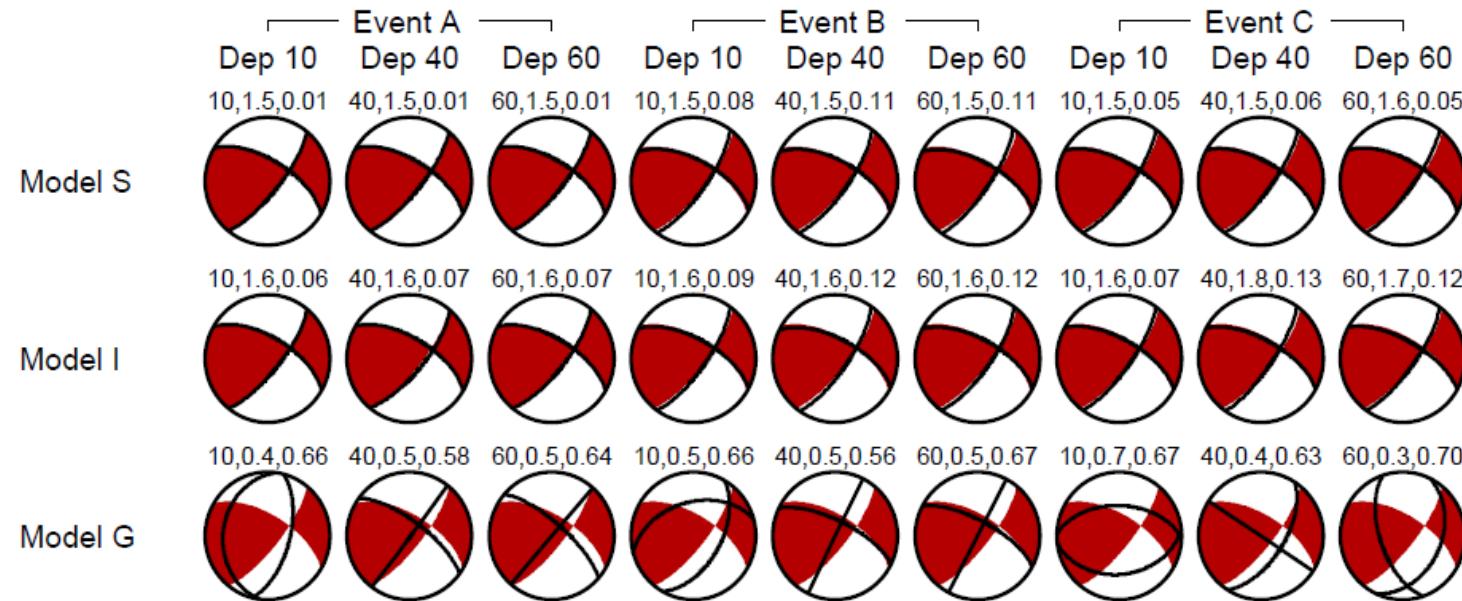
Frequency domain (amplitude spectra) inversion

- Less sensitive to traces alignment, wave propagation mismodeling
- Implicit polarity ambiguity

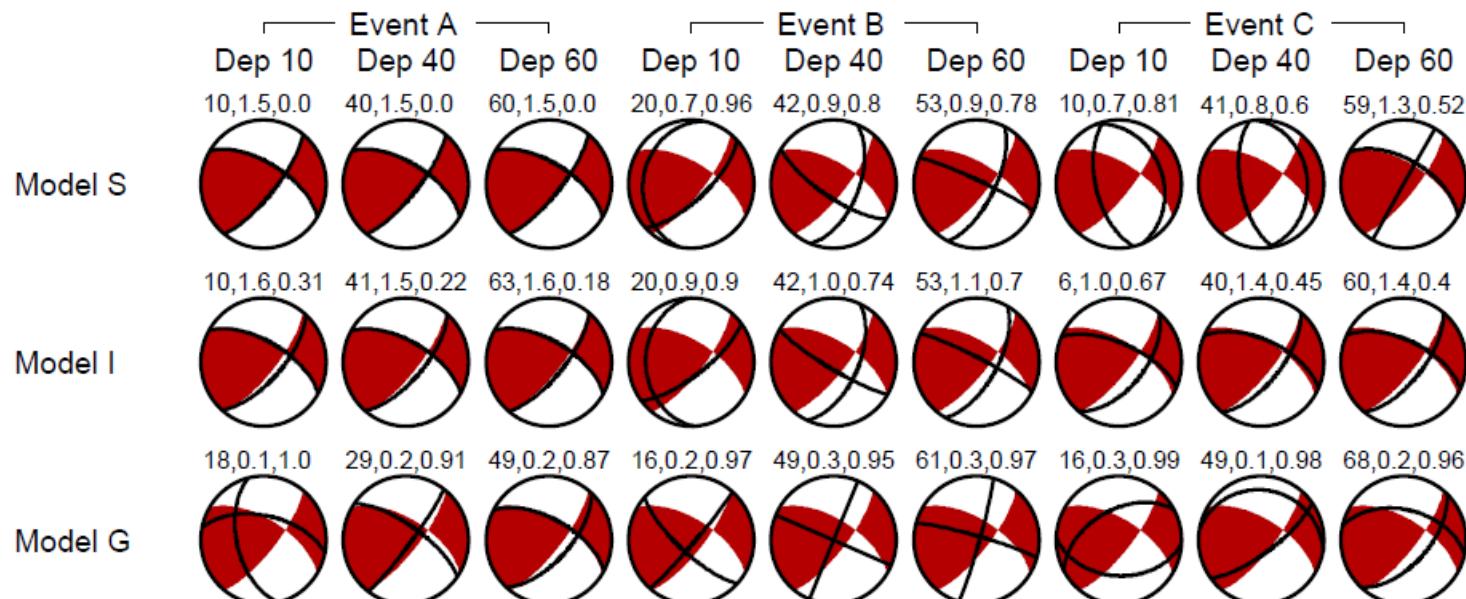


Amplitude spectra

(a) Crustal structure mismodelling

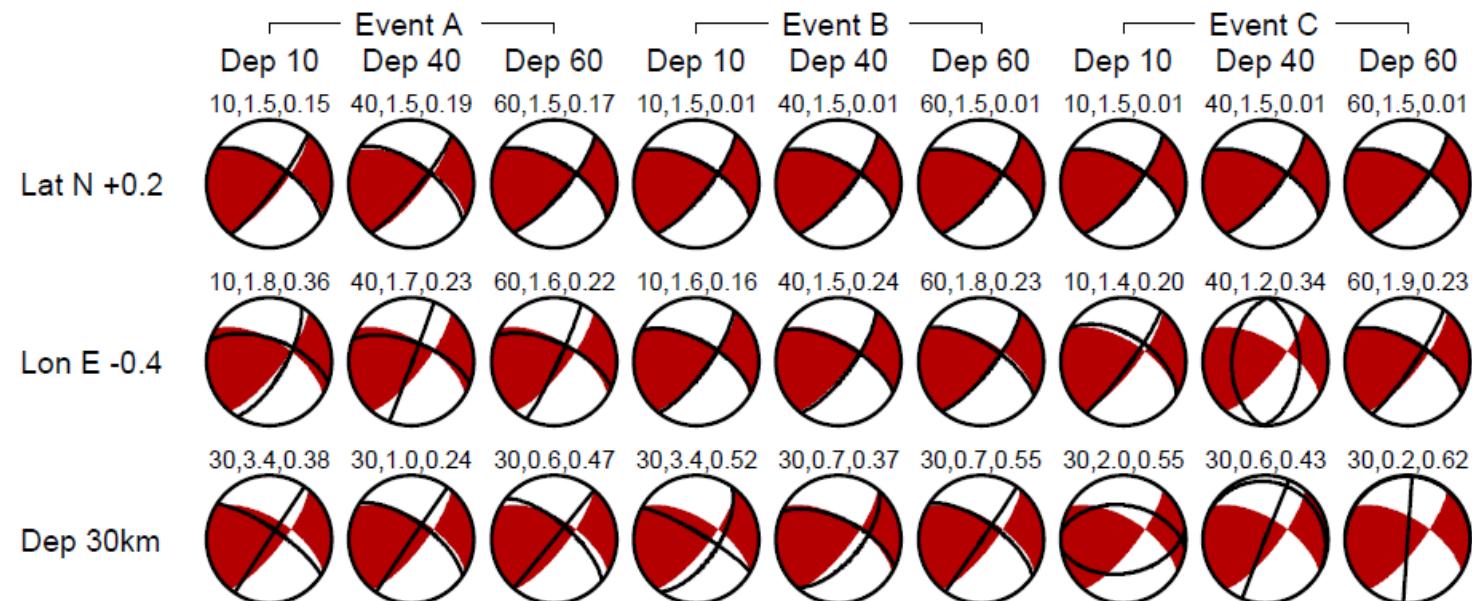
**Waveforms (time domain)**

(a) Crustal structure mismodelling

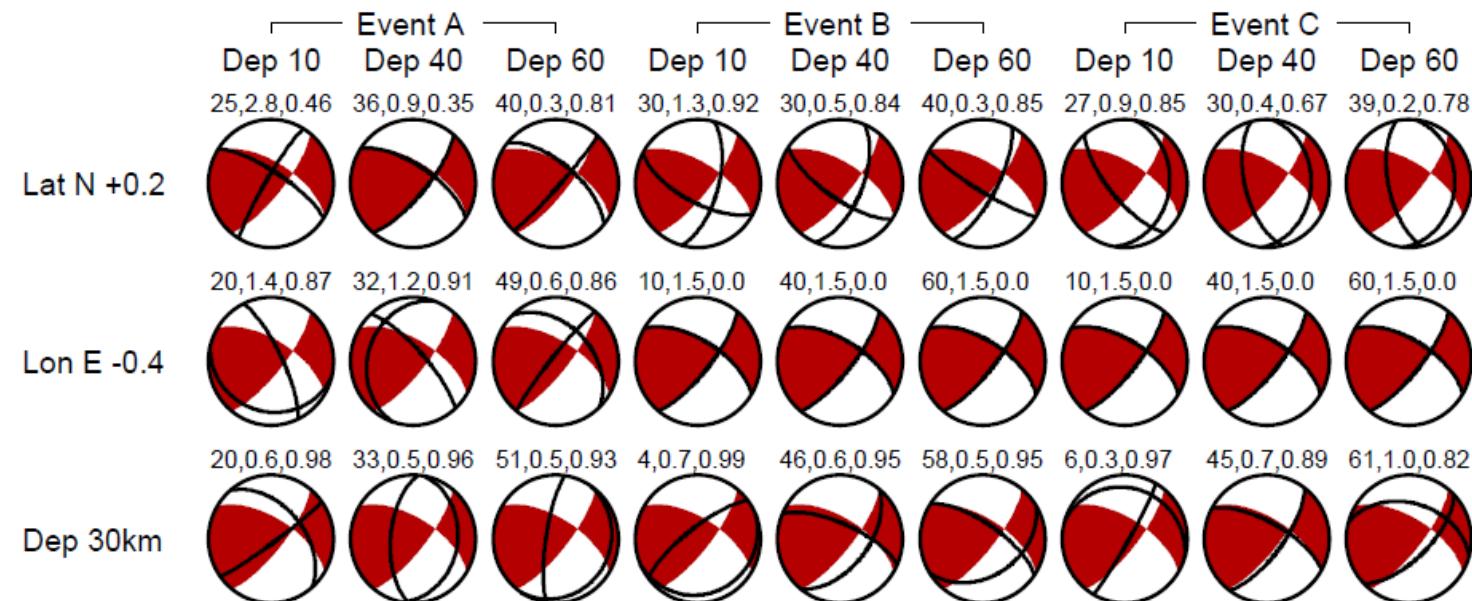


Amplitude spectra

(b) Wrong starting location



(b) Wrong starting location



Surface waves vs. Body waves

Surface waves (or full waveform)

Widely used at regional (and teleseismic distances)

Robust as low frequencies can be used

Poor resolution (M_{xz} , M_{yz}) for shallow sources

Bodywaves

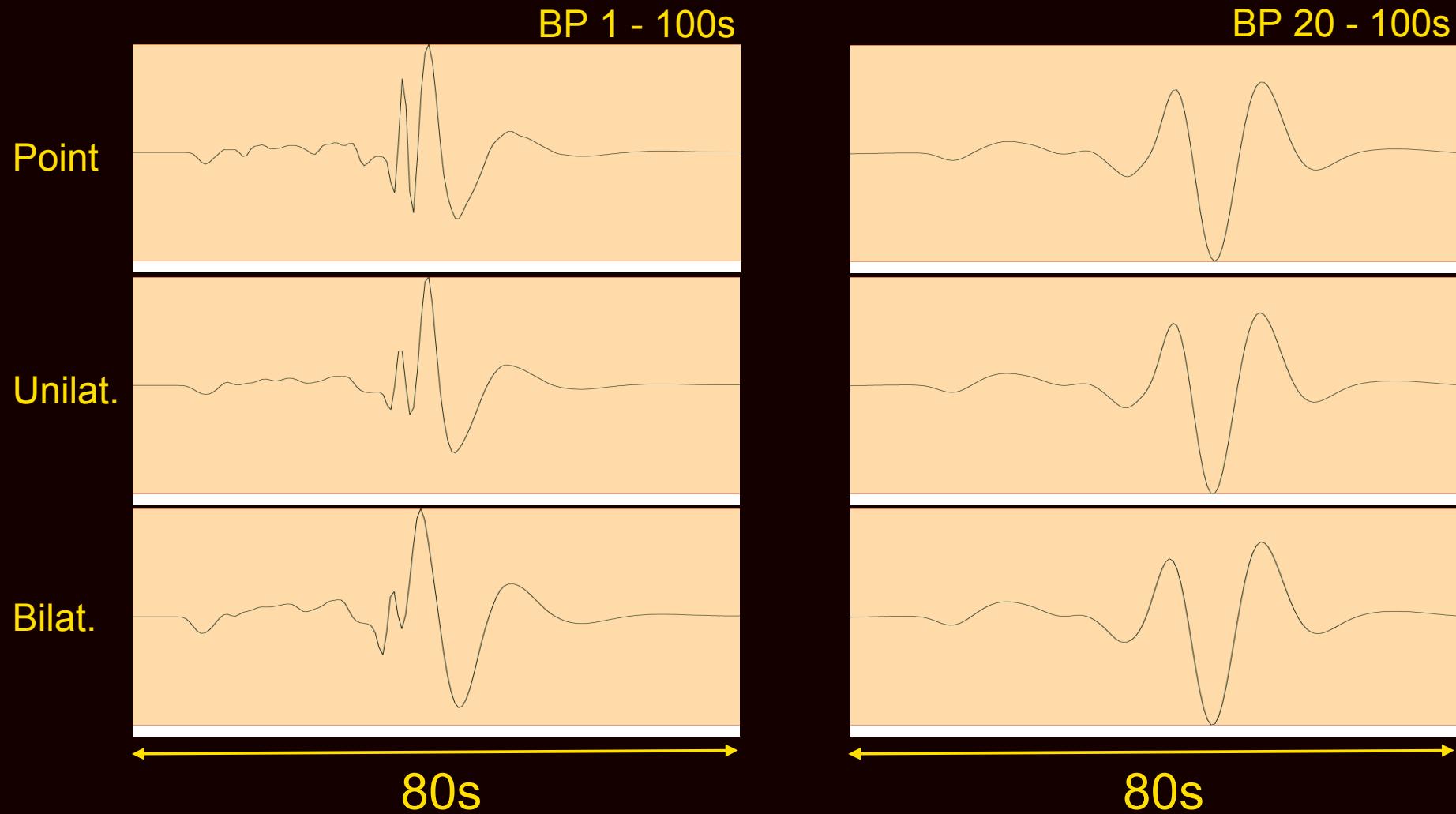
Strong dependency on precise velocity and attenuation models

Potentially good focal mechanism coverage and MT resolution

Intermediate/deep seismicity



On the choice of the best frequency range



Flat/known instrumental response

Below spectra corner frequency (point source), or above (to resolve finite rupture)

10-50s for local/regional earthquakes $Mw < 5.5$

30-100s for regional/teleseismic distances $Mw > 5.5$

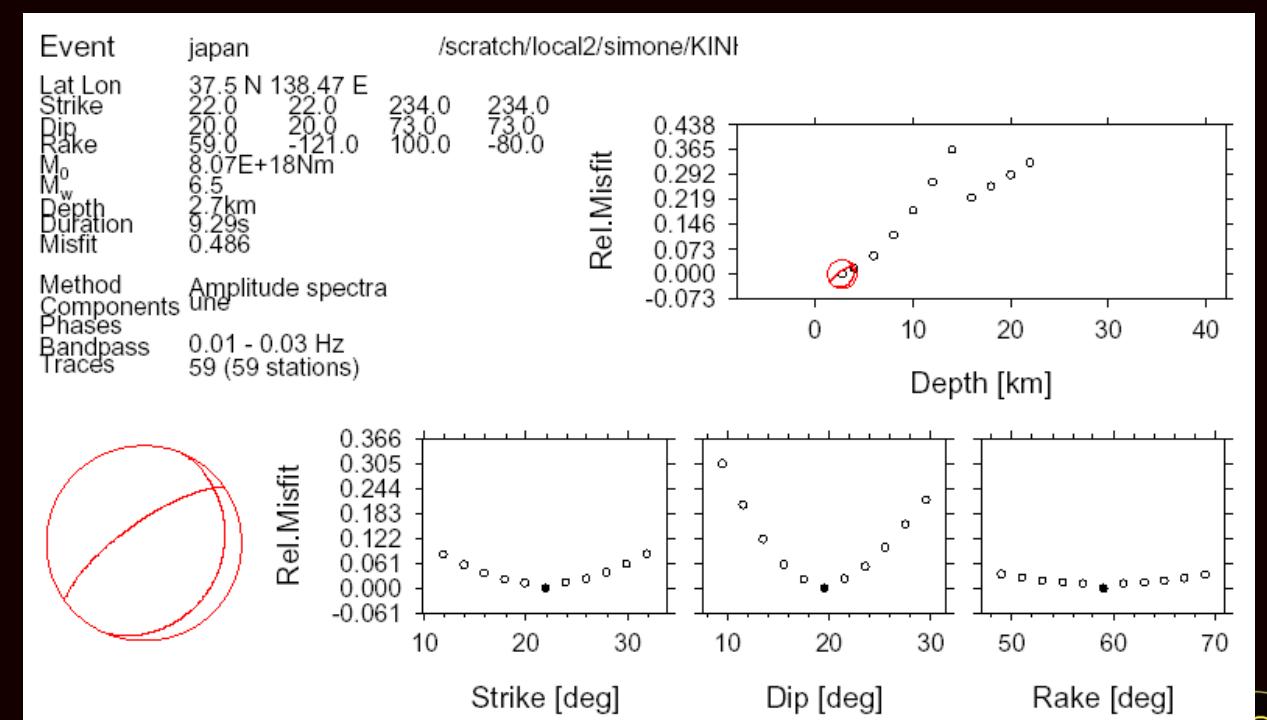


About the bootstrap approach

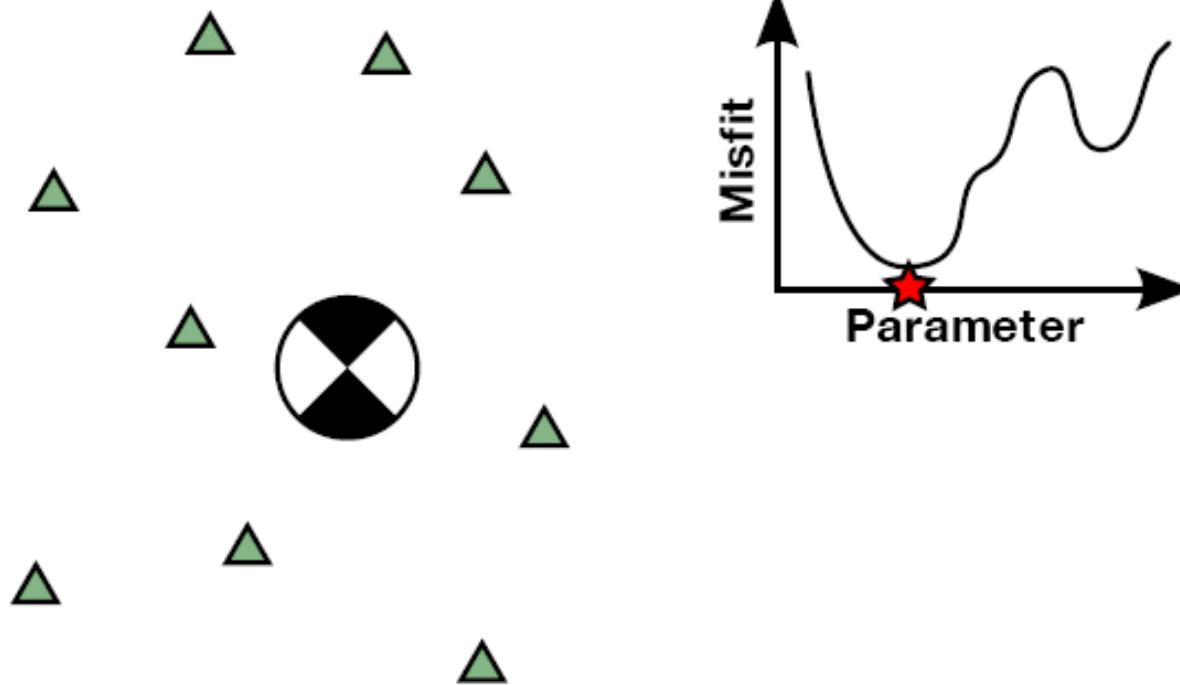
General estimation of data fit

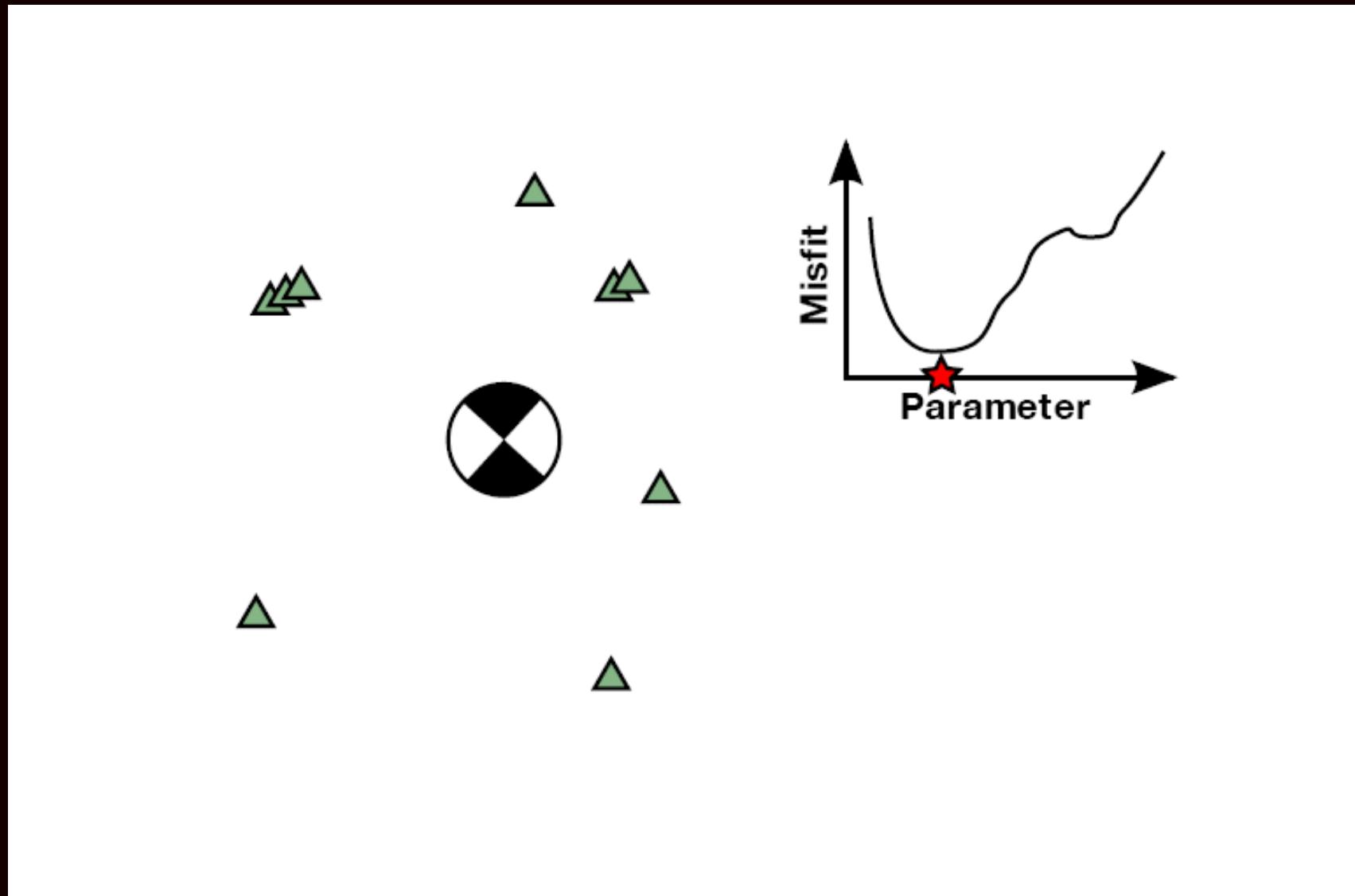
We need additional information on
inversion stability

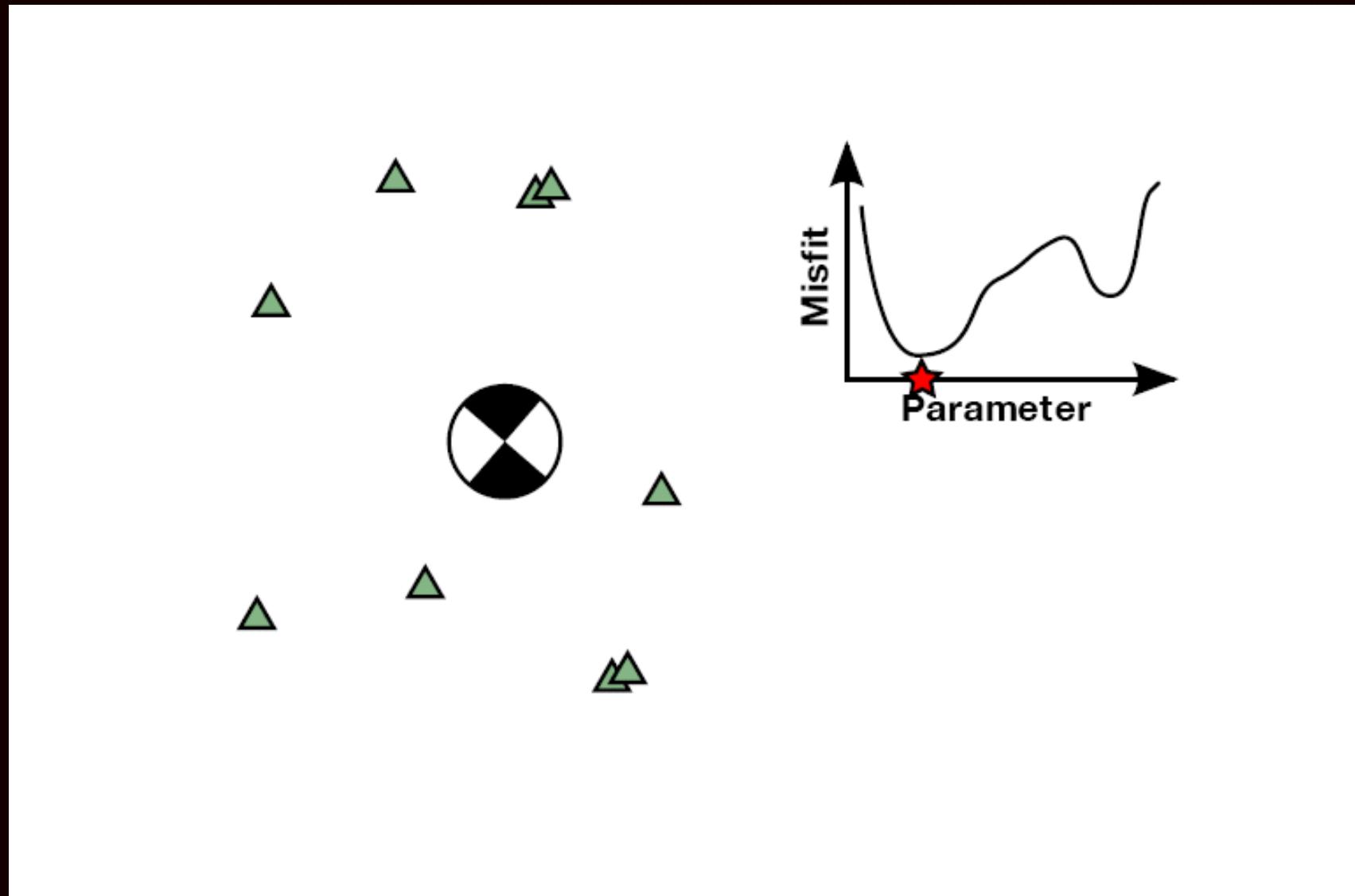
Relative misfit curve (perturbation of
single source parameters)

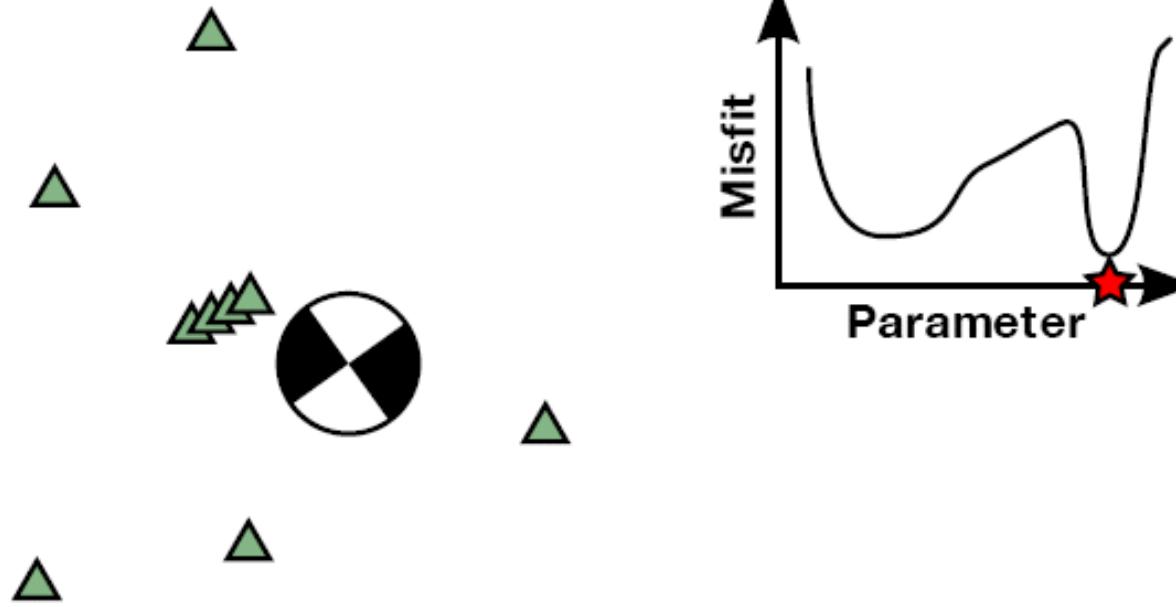


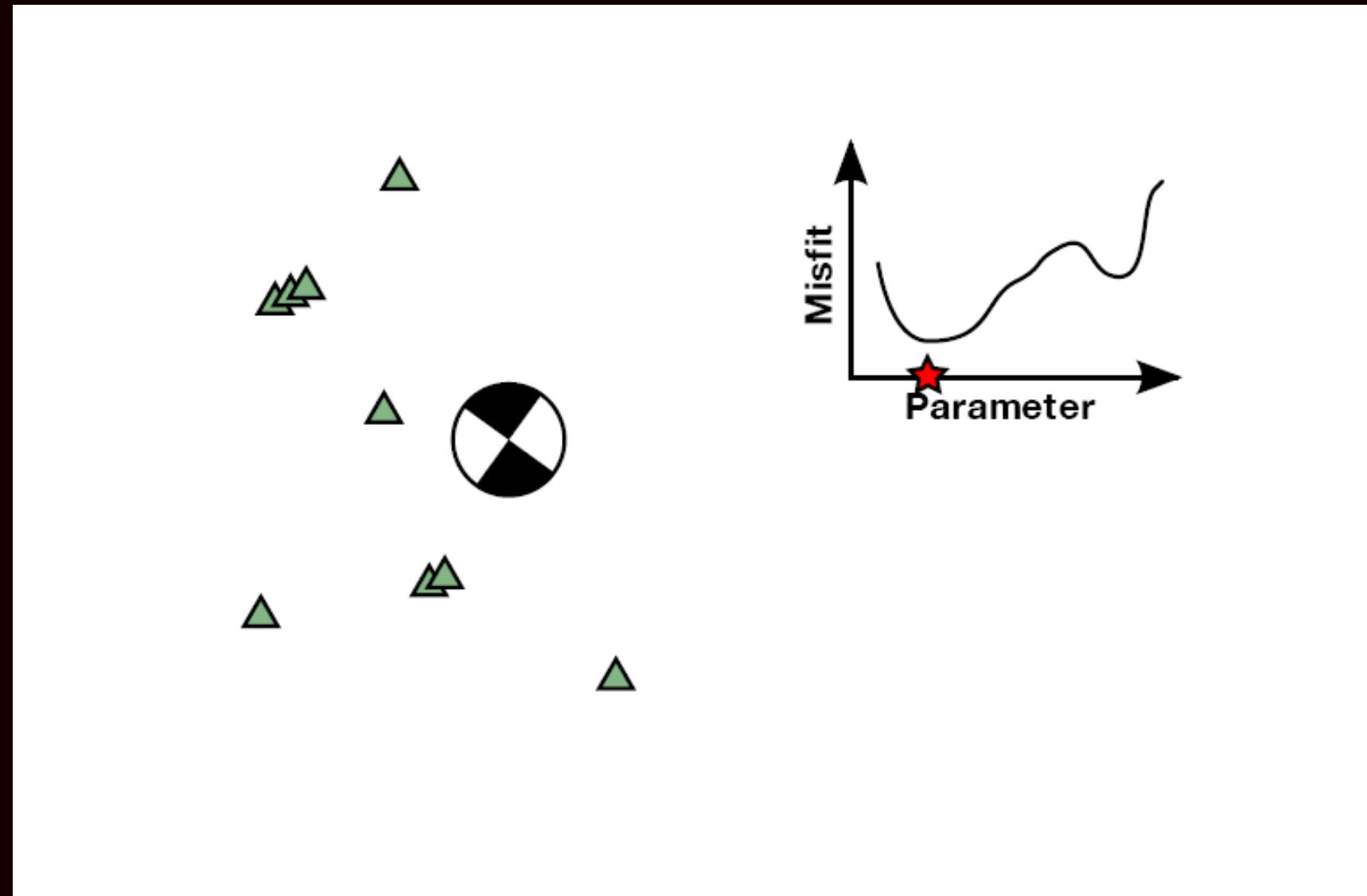
About the bootstrap approach

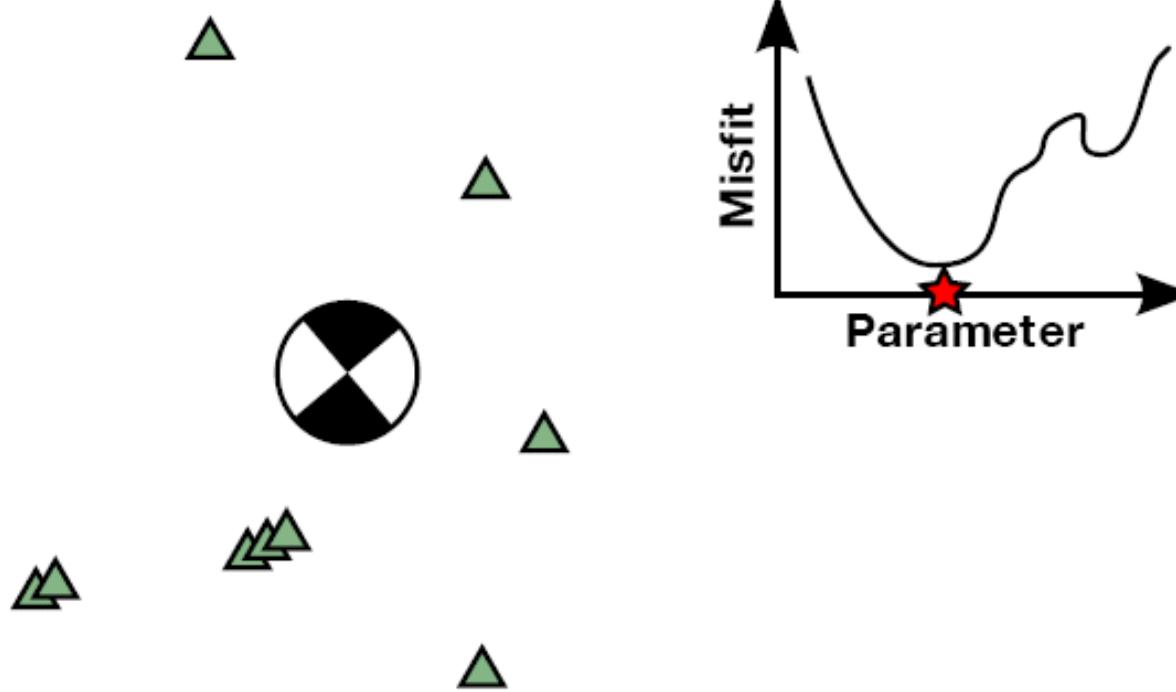


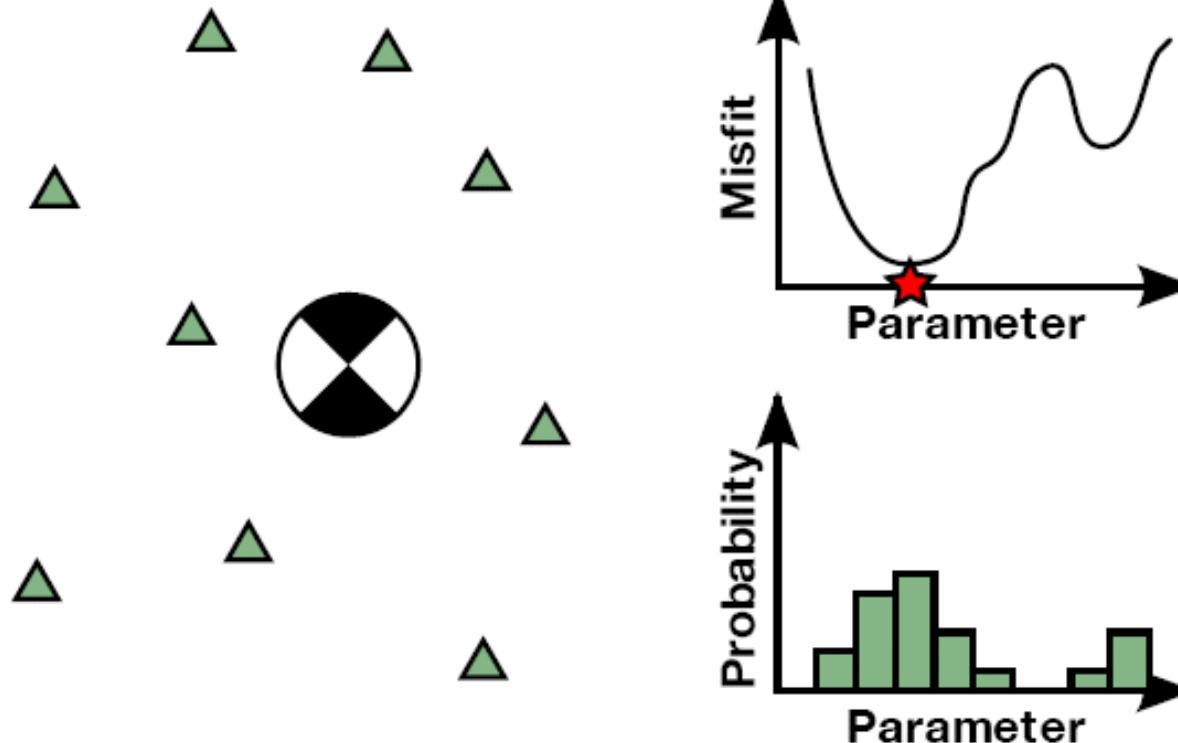








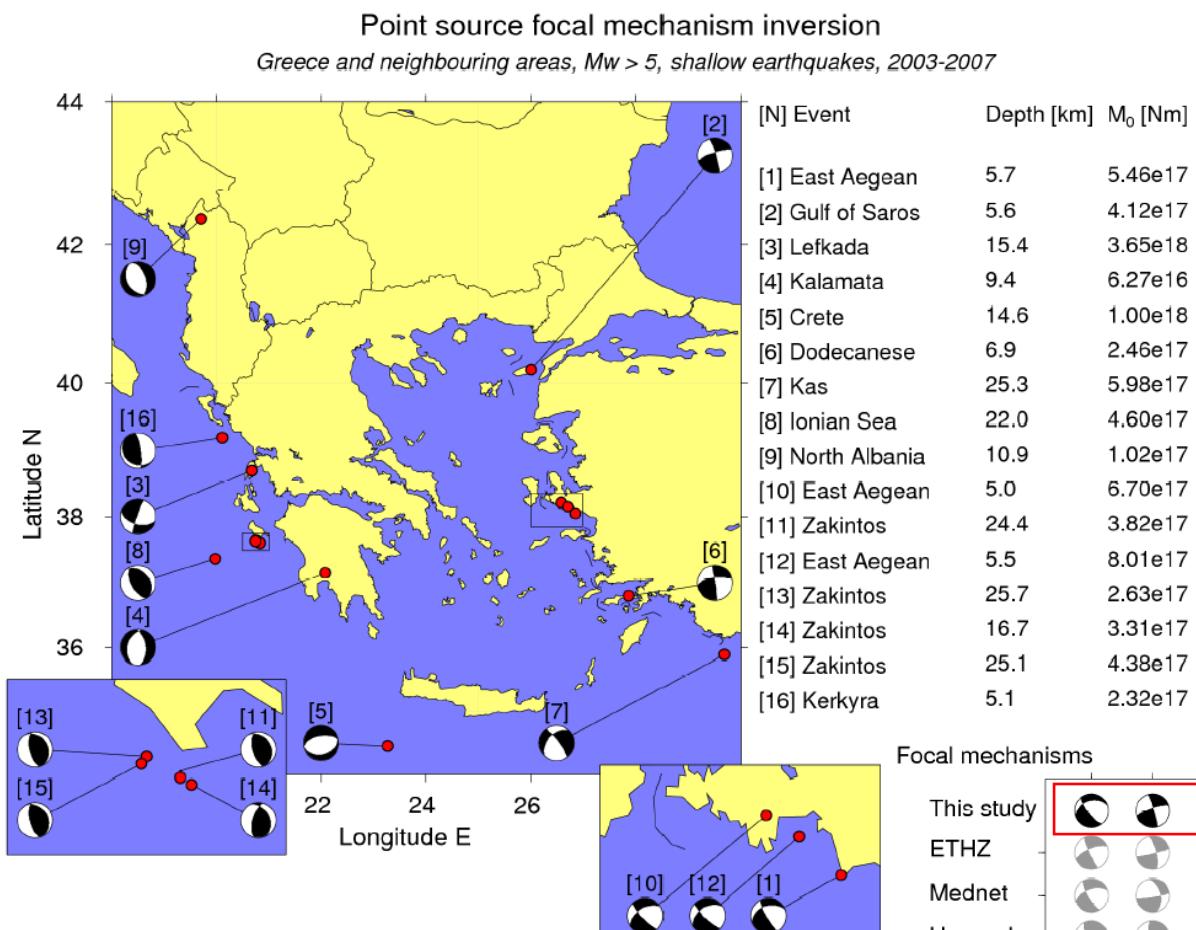




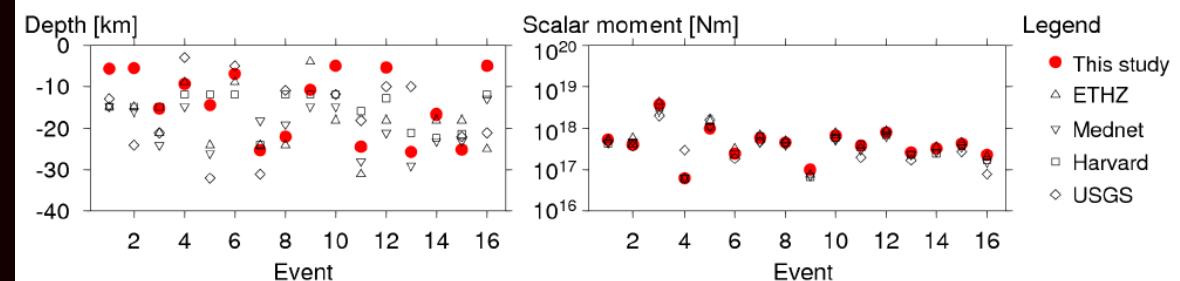
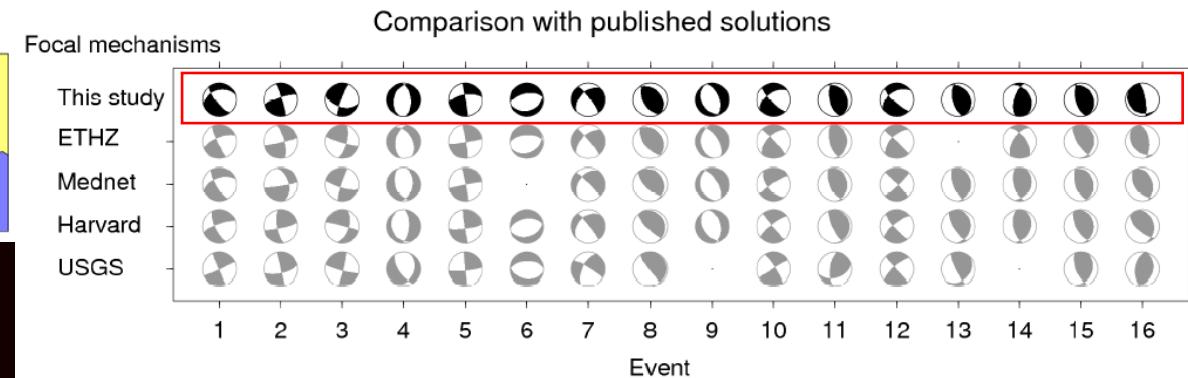
Example of applications

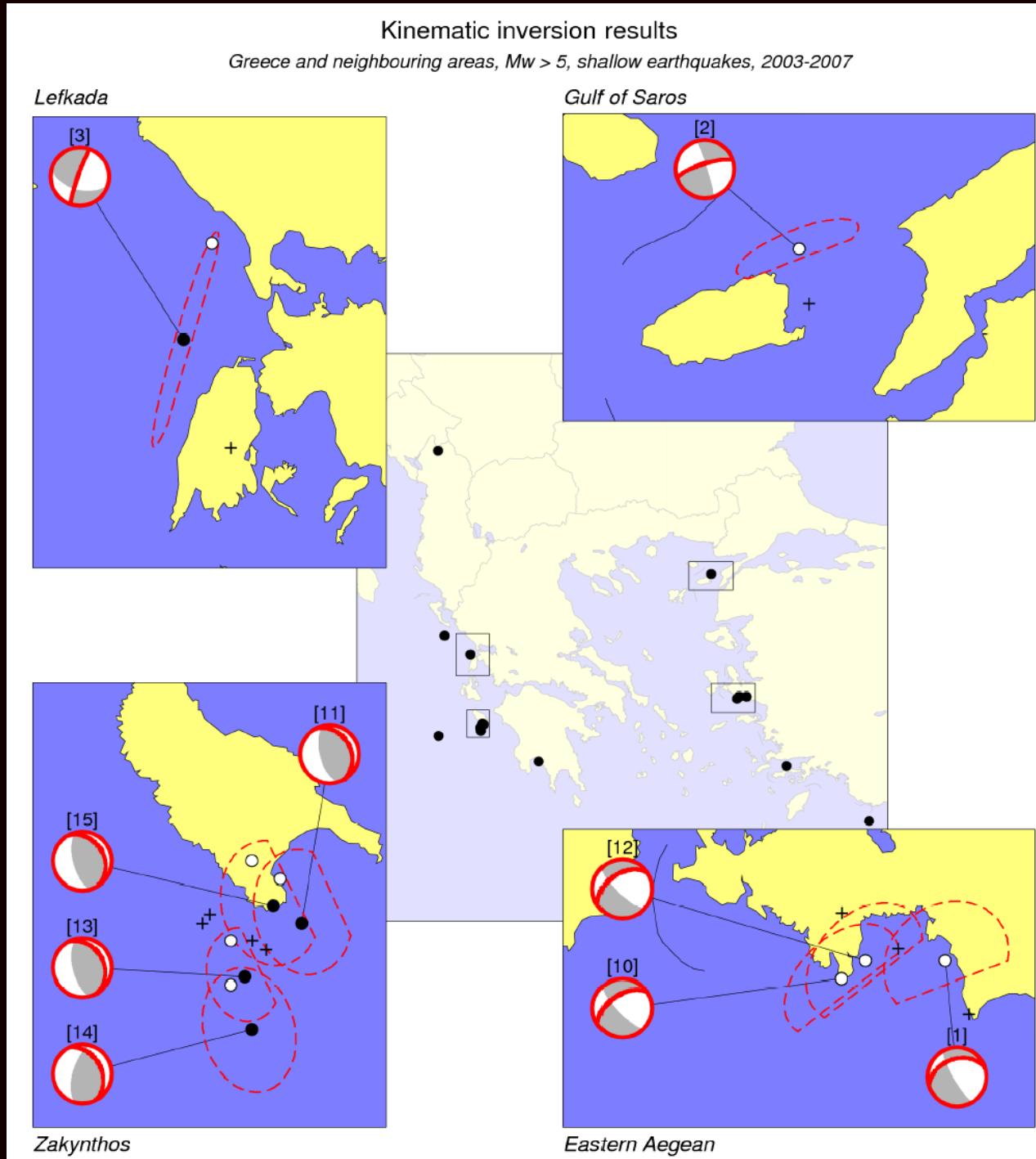


Greece,
Shallow earthquakes
2003-2007
point sources



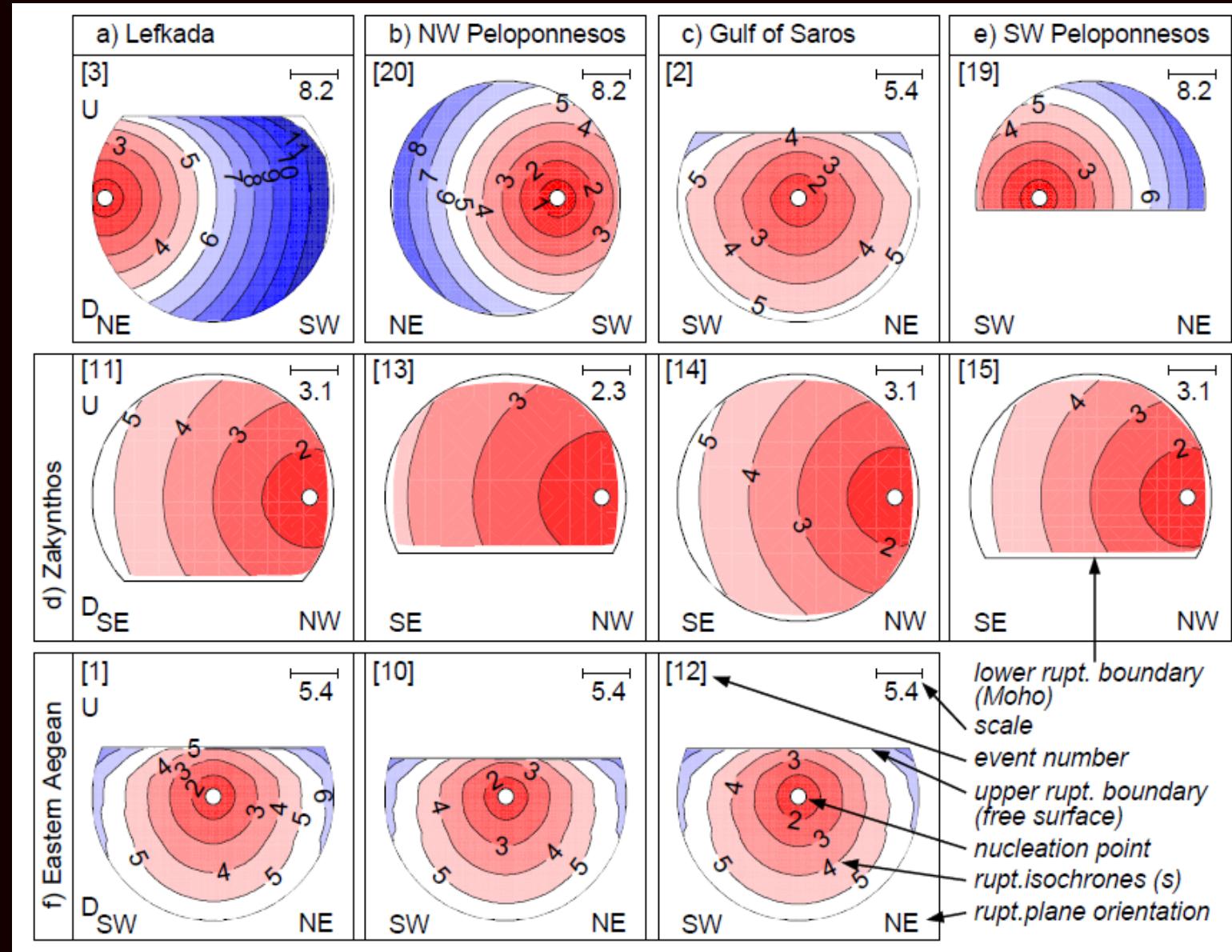
Cesca et al. JGR 2010





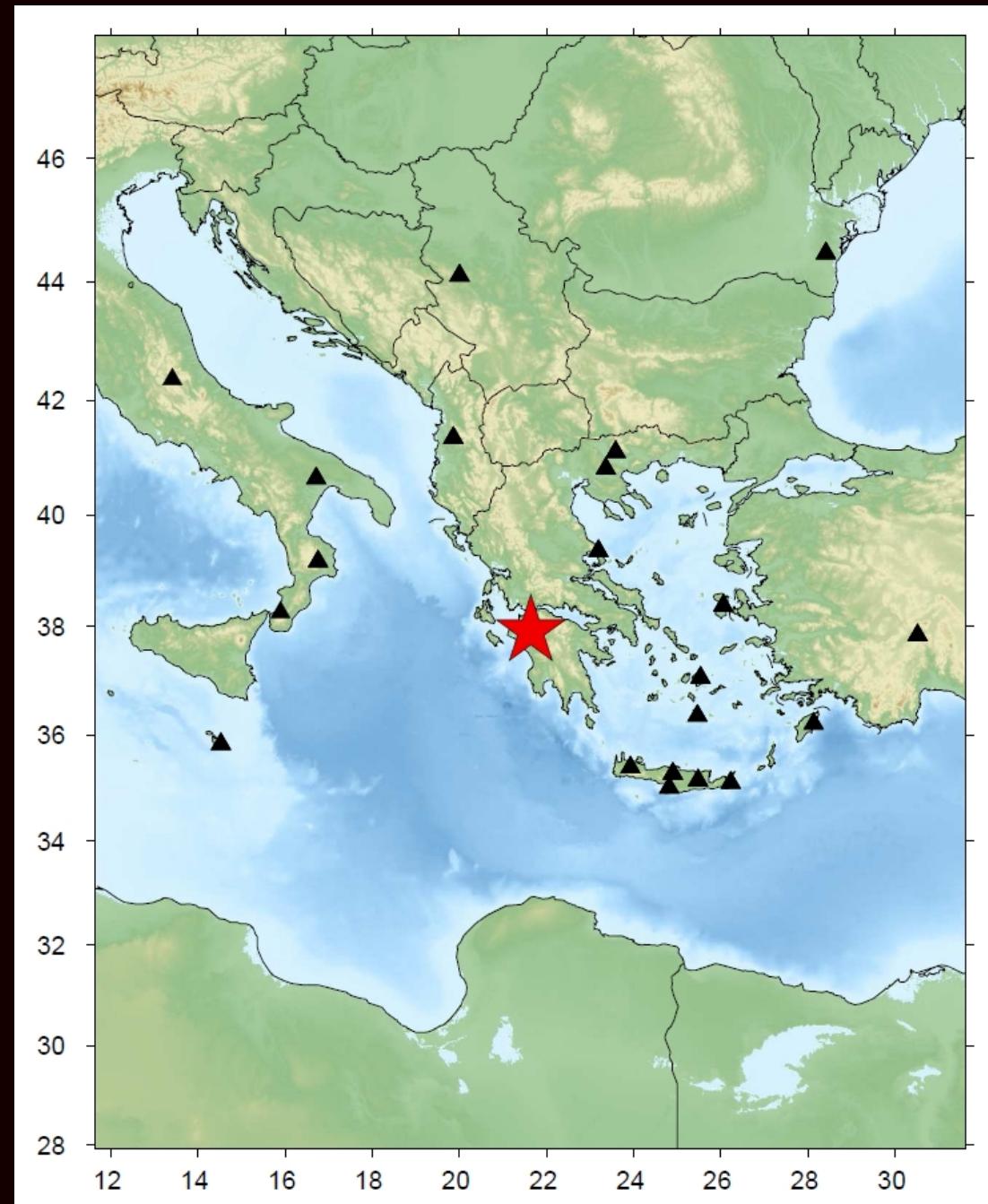
Greece,
Shallow earthquakes
2003-2007
extended sources

Cesca et al. JGR 2010

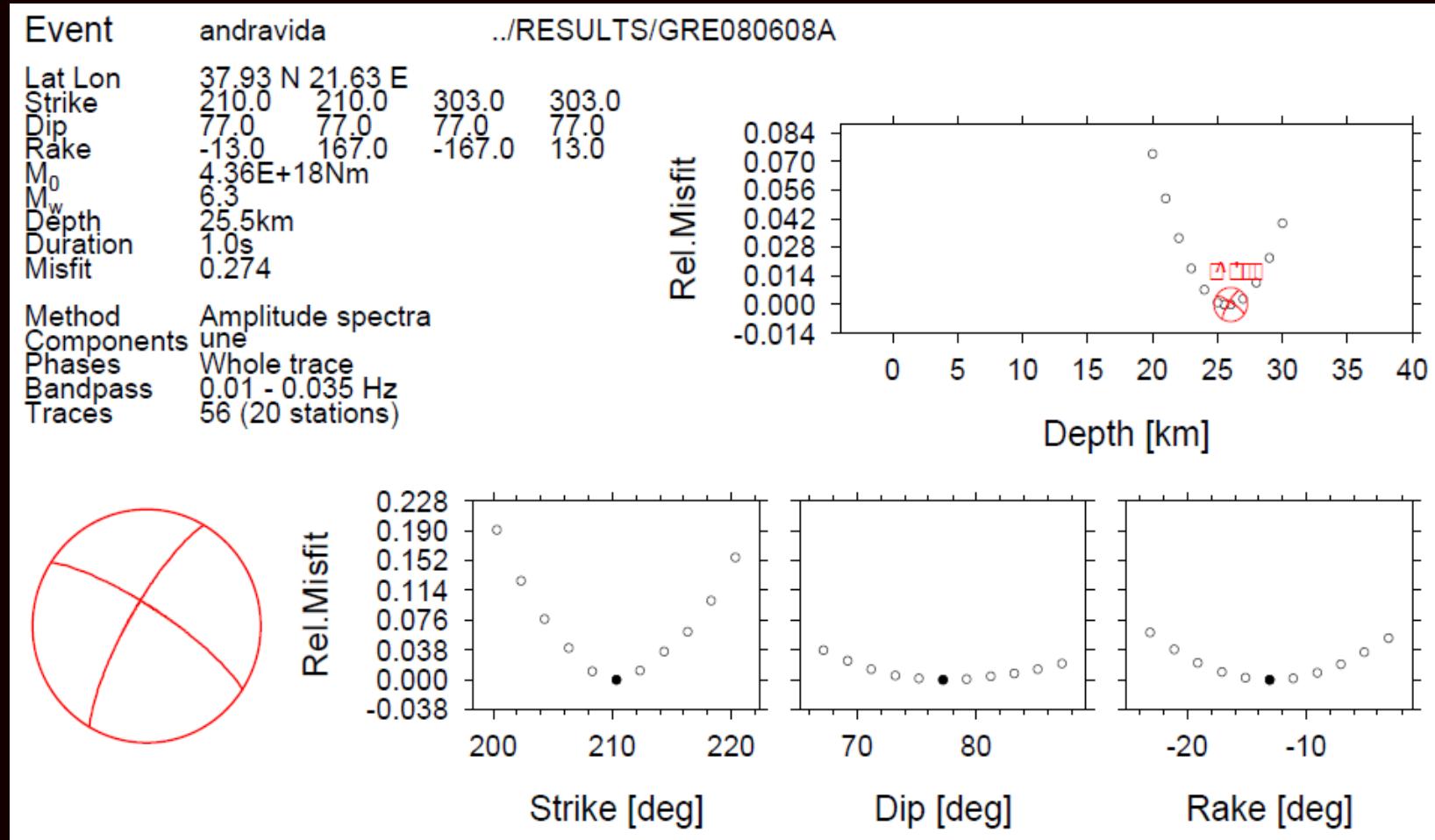


Cesca et al. JGR 2010

The Andravida earthquake – different inversion approaches



The Andravida earthquake – different inversion approaches



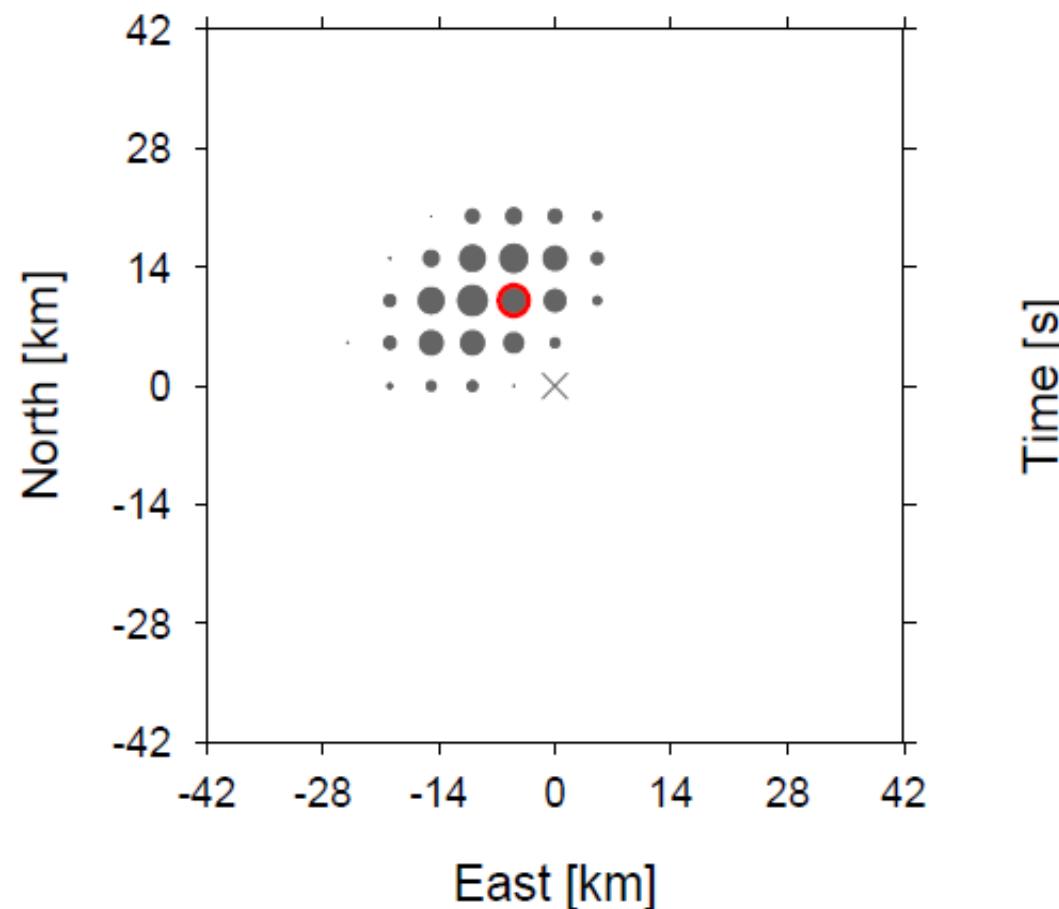
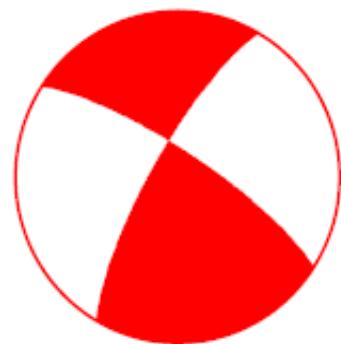
The Andravida earthquake – different inversion approaches

Event

andravida

..//RESULTS/GRE080608A

Lat Lon	37.93 N 21.63 E
Strike	210.0 303.0
Dip	77.0 77.0
Rake	167.0 13.0
M_0	4.36E+18Nm
M_w	6.3
Depth	25.5km
Duration	1.0s
Misfit	0.472
Method	Time domain
Components	une
Phases	Whole trace
Bandpass	0.01 - 0.035 Hz
Traces	56 (20 stations)



The Andravida earthquake – different inversion approaches

Epicenter – Centroid Relative Location

Event

andravida

..//RESULTS/GRE080608A

Lat Lon

37.93 N 21.63 E

Strike

210.0 303.0

Dip

77.0 77.0

Rake

167.0 13.0

M_0

4.36E+18Nm

M_w

6.3

Depth

25.5km

Duration

1.0s

Misfit

0.472

Method

Time domain

Components

une

Phases

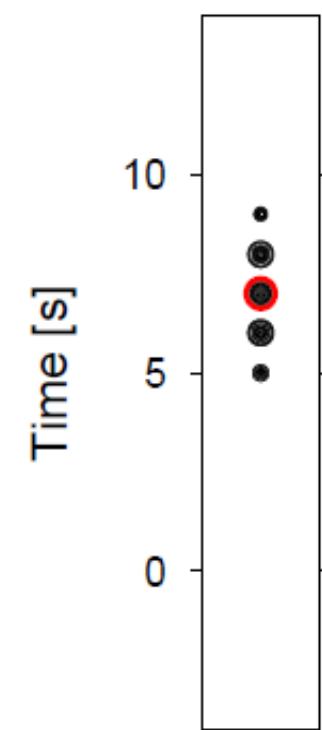
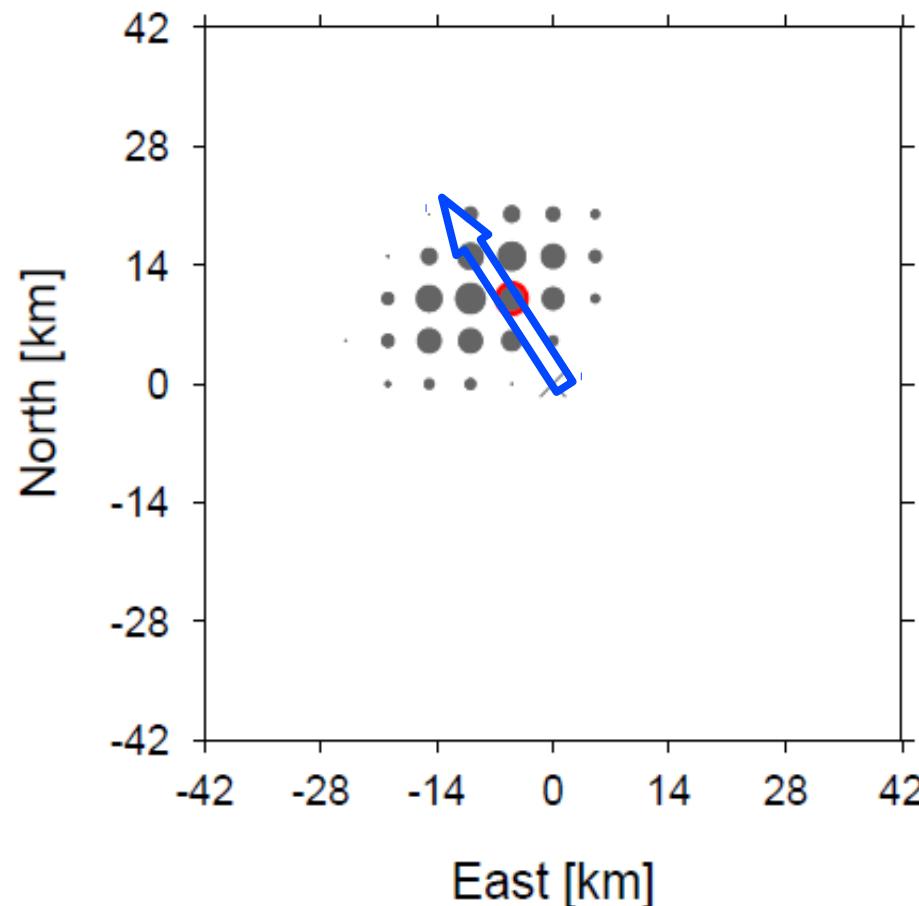
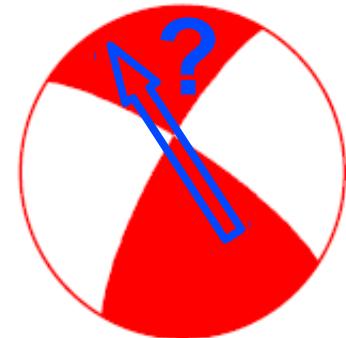
Whole trace

Bandpass

0.01 - 0.035 Hz

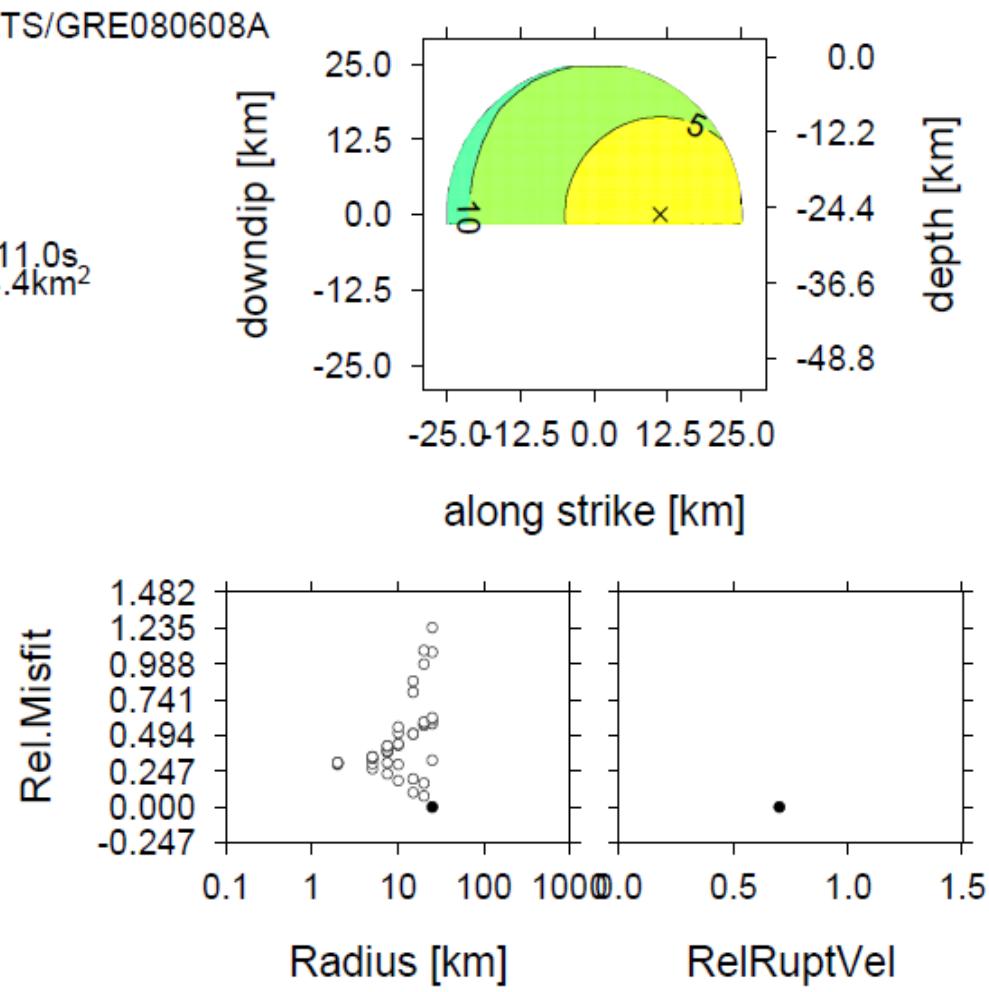
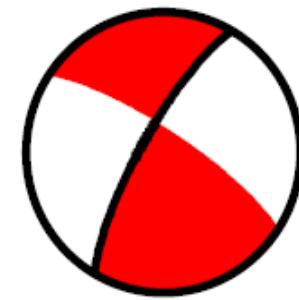
Traces

56 (20 stations)



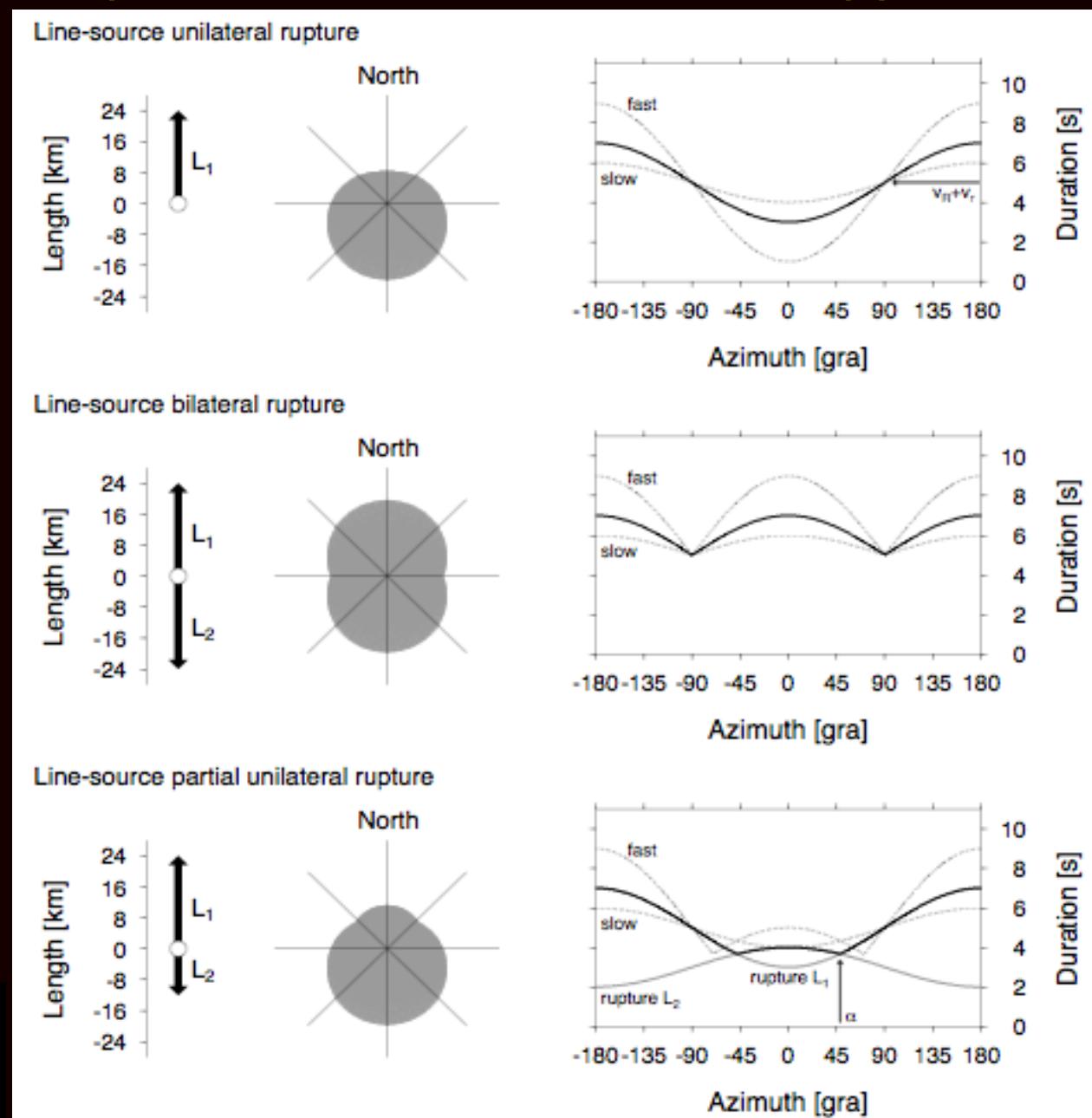
The Andravida earthquake – different inversion approaches

Event	andravida	..//RESULTS/GRE080608A	
Lat Lon	37.93 N 21.63 E		
Strike	210.0		
Dip	77.0		
Rake	167.0		
M_0	$4.36E+18\text{Nm}$		
M_w	6.3		
Depth	25.5km	Duration	3.3+11.0s
Radius	25.0km	Area	1054.4km ²
Average Slip	0.062m	RelRuptVel	0.7
Nucleation	x: 11.25km	y: 0.0km	
Misfit	0.291		
Method	Amplitude spectra		
Components	une		
Phases	Whole trace		
Bandpass	0.01 - 0.1 Hz		
Traces	56 (20 stations)		

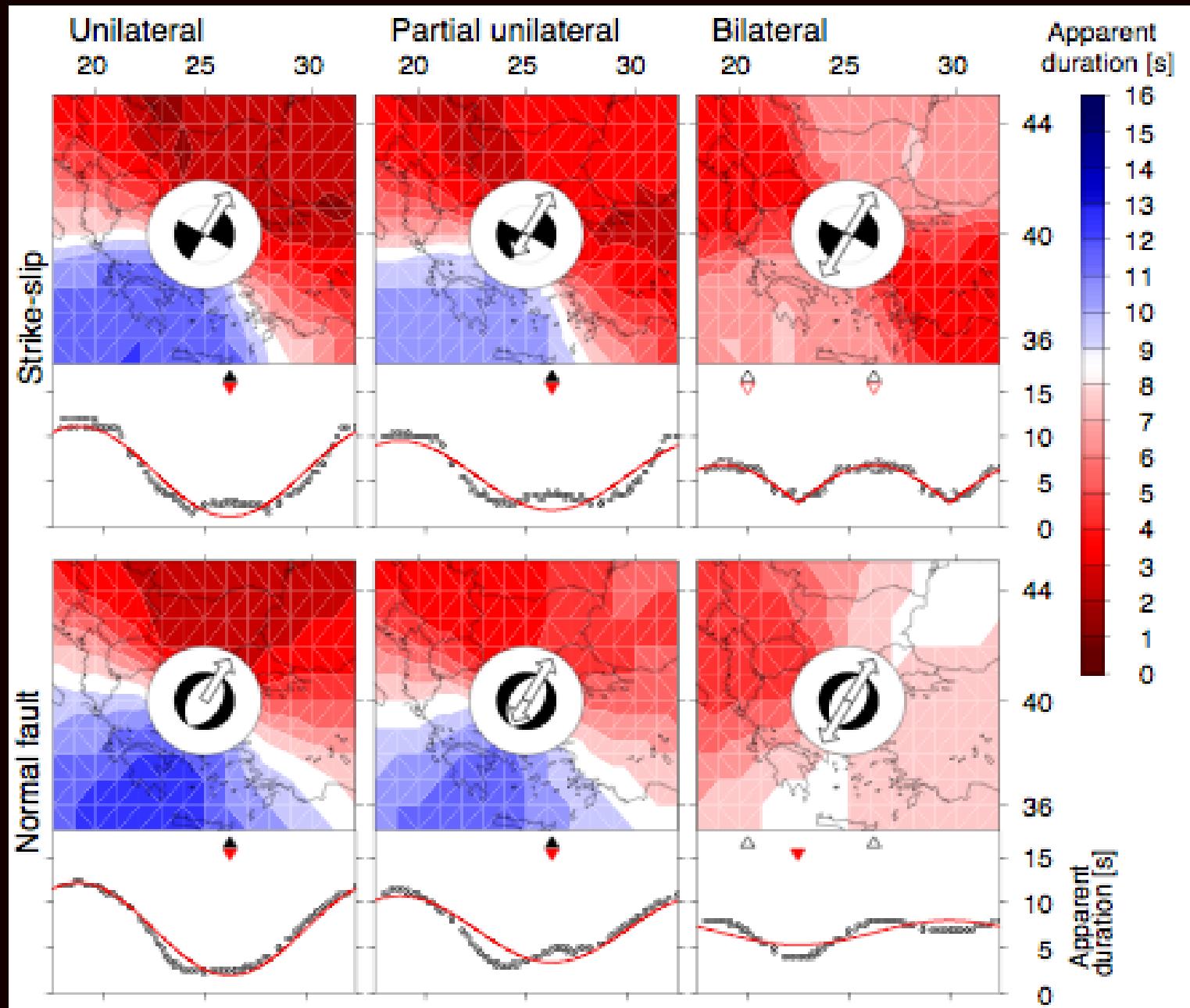


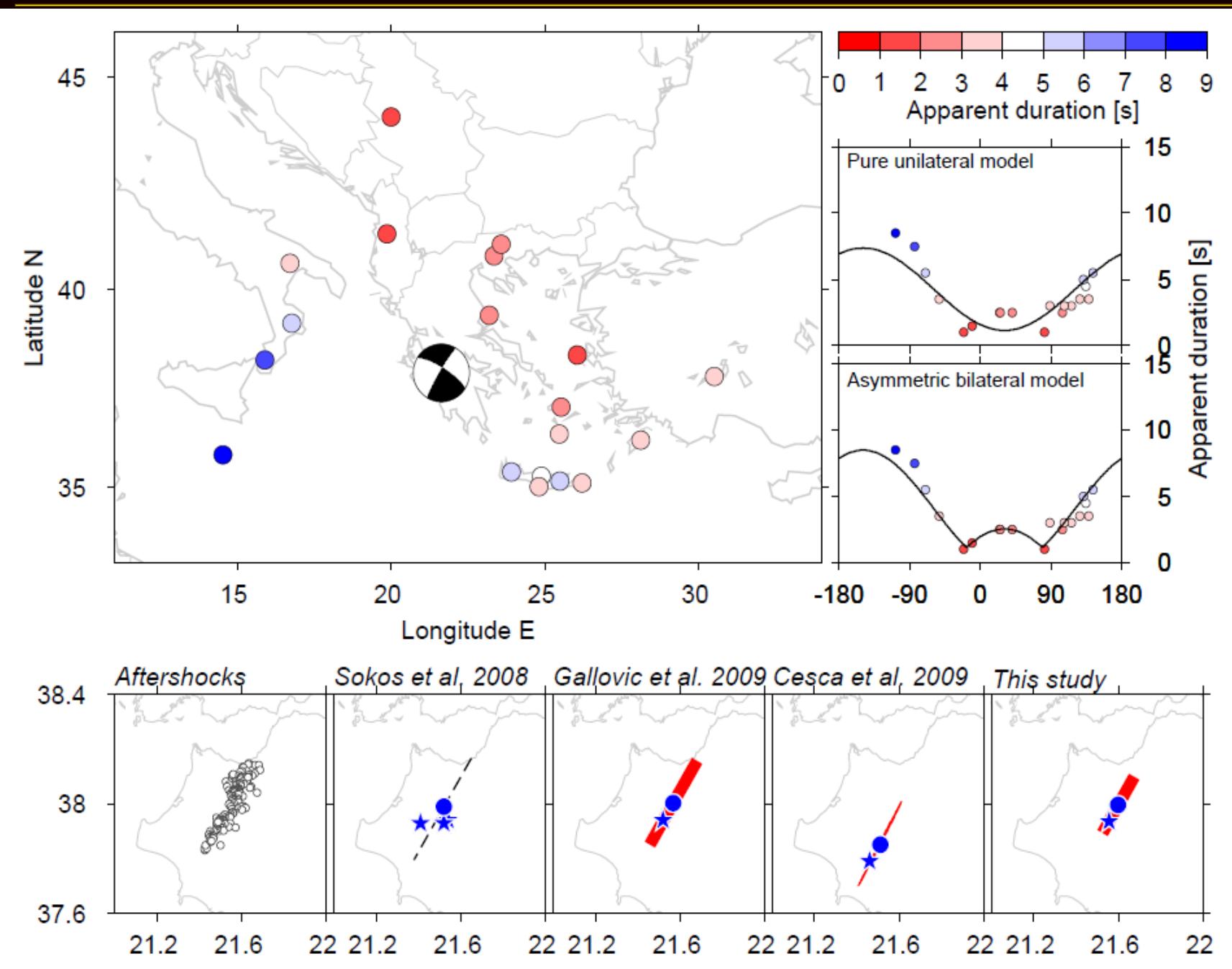
The Andravida earthquake – different inversion approaches

Fast directivity detection using apparent durations

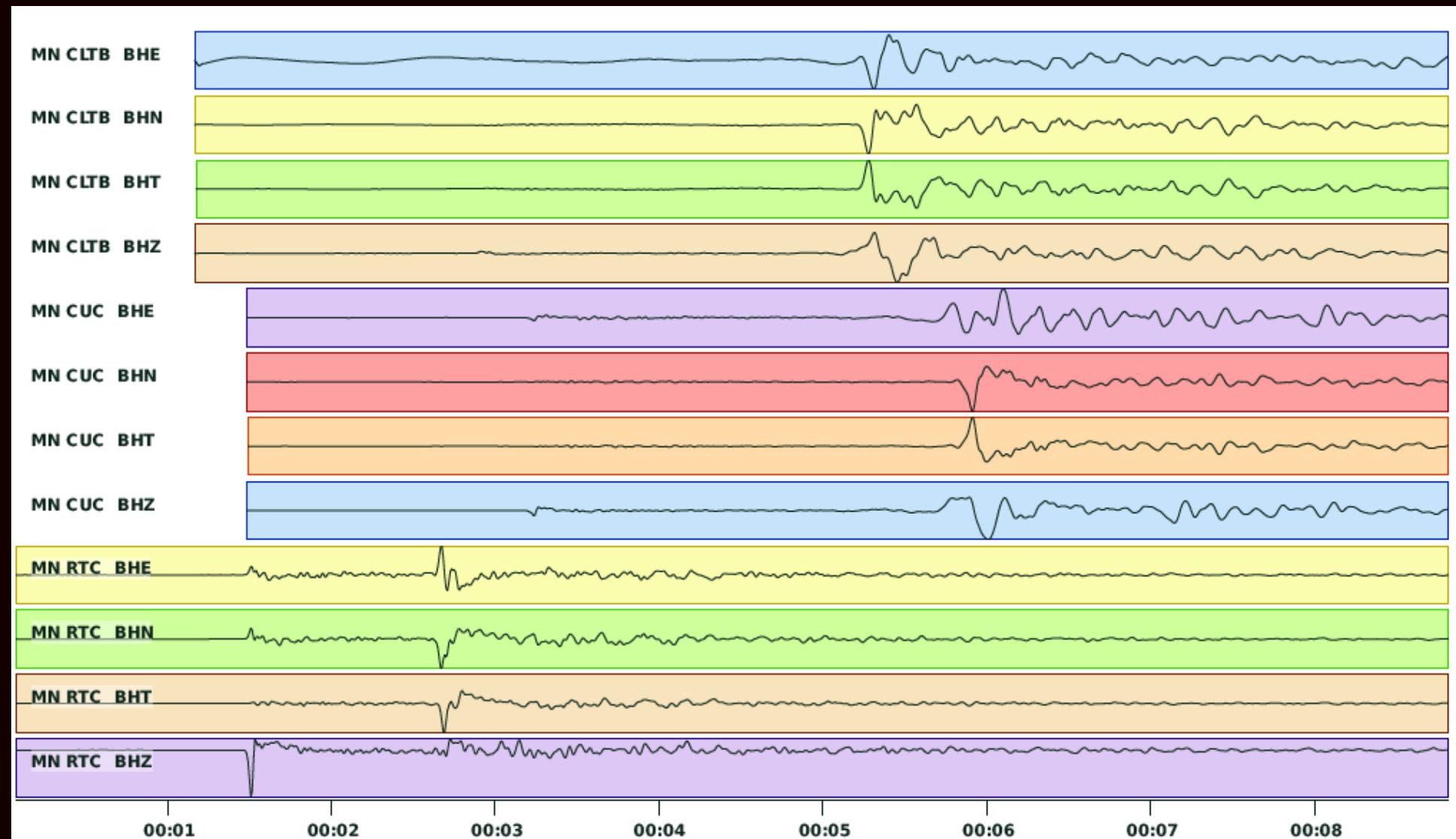


Cesca et al.
J. Seismol. 2011



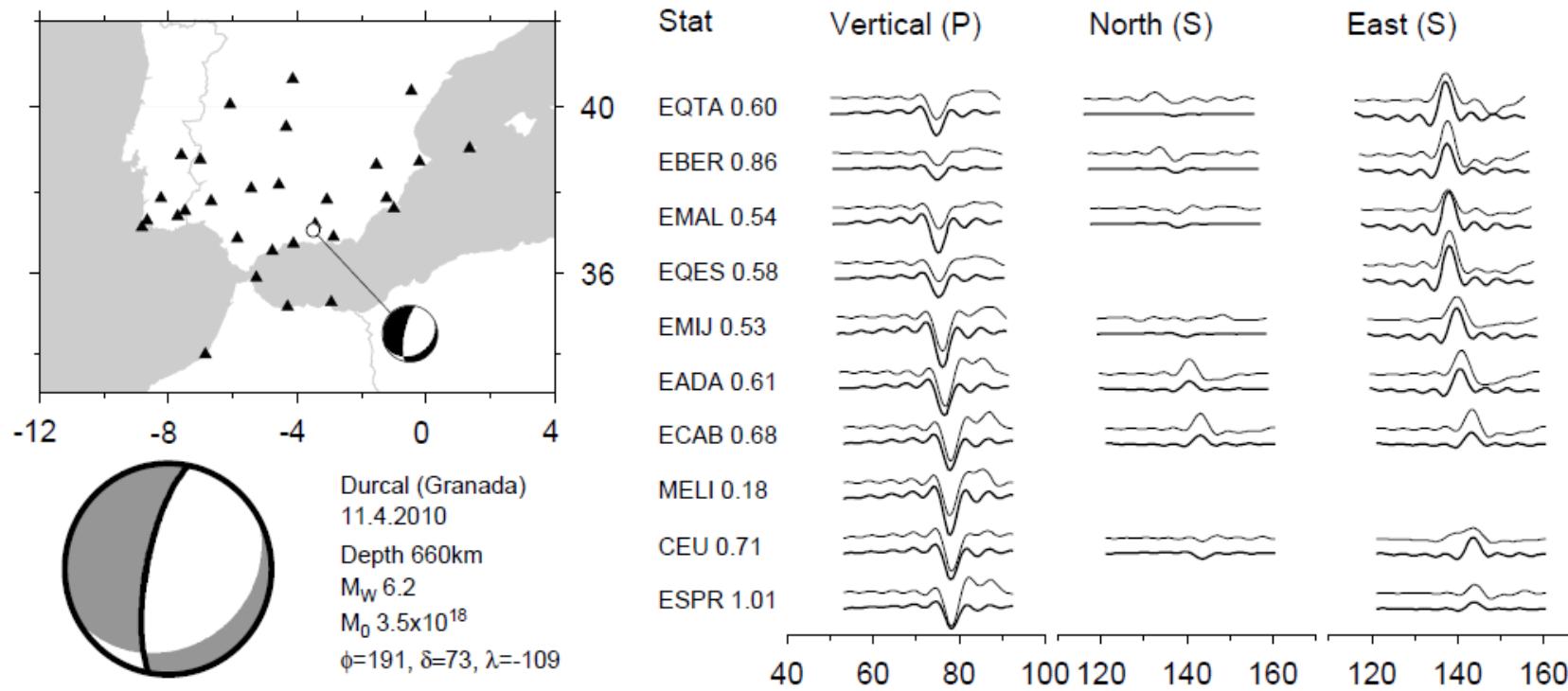


A deep earthquake beneath Southern Spain, the 11.4.2010 Granada earthquake

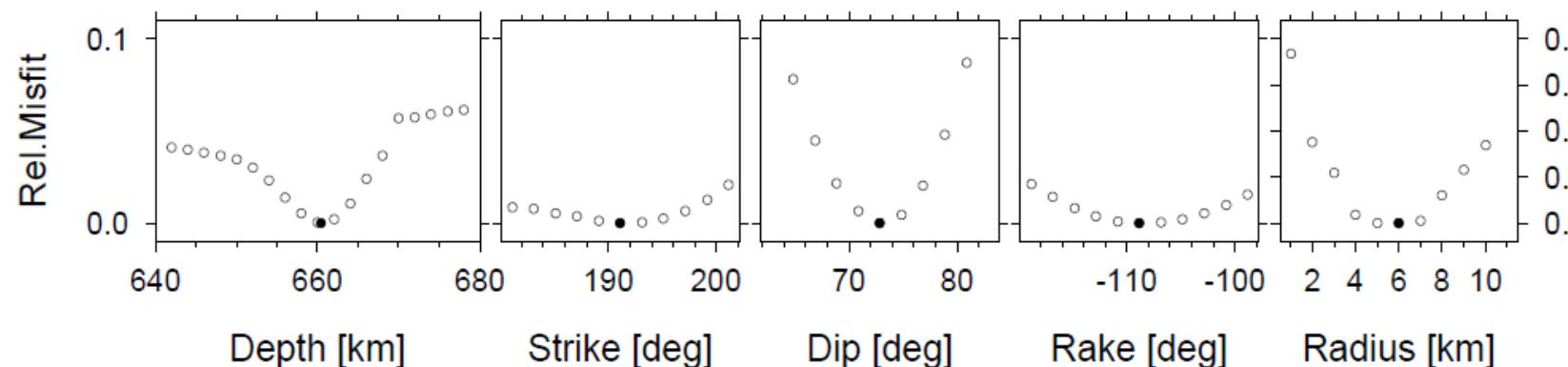


A deep earthquake beneath Southern Spain, the 11.4.2010 Granada earthquake

(a) Stations, source model and seismogram fit (closest 10 stations)

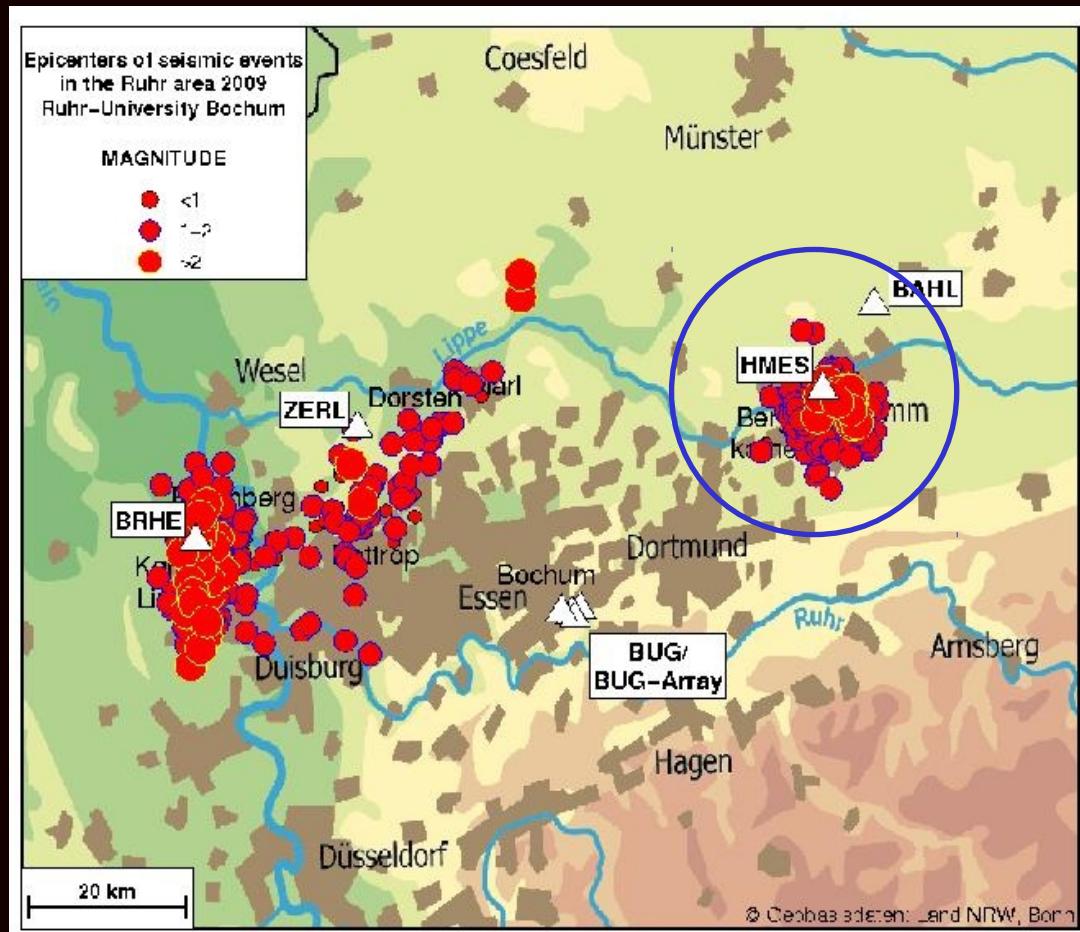


(b) Stability of earthquake source parameters



Buorn et al.
BSSA 2011

Microseismicity application, source inversion in mining environments



Bischoff et al. 2010

Coal mining induced seismicity
monitored by Ruhr University since
1983

About 1000 events are recorded
between $0.7 < \text{ML} < 3.3$ every year

Hamm region (blue circle)

>7000 events in 2006-2007 (14 months)

913 events $0.0 < \text{ML} < 2.0$

DC inversion

MT inversion

Kinematic inversion and rupture modeling





Seismicity follows longwall mining,
Epicenters are spreaded over an area of
about 2x2km

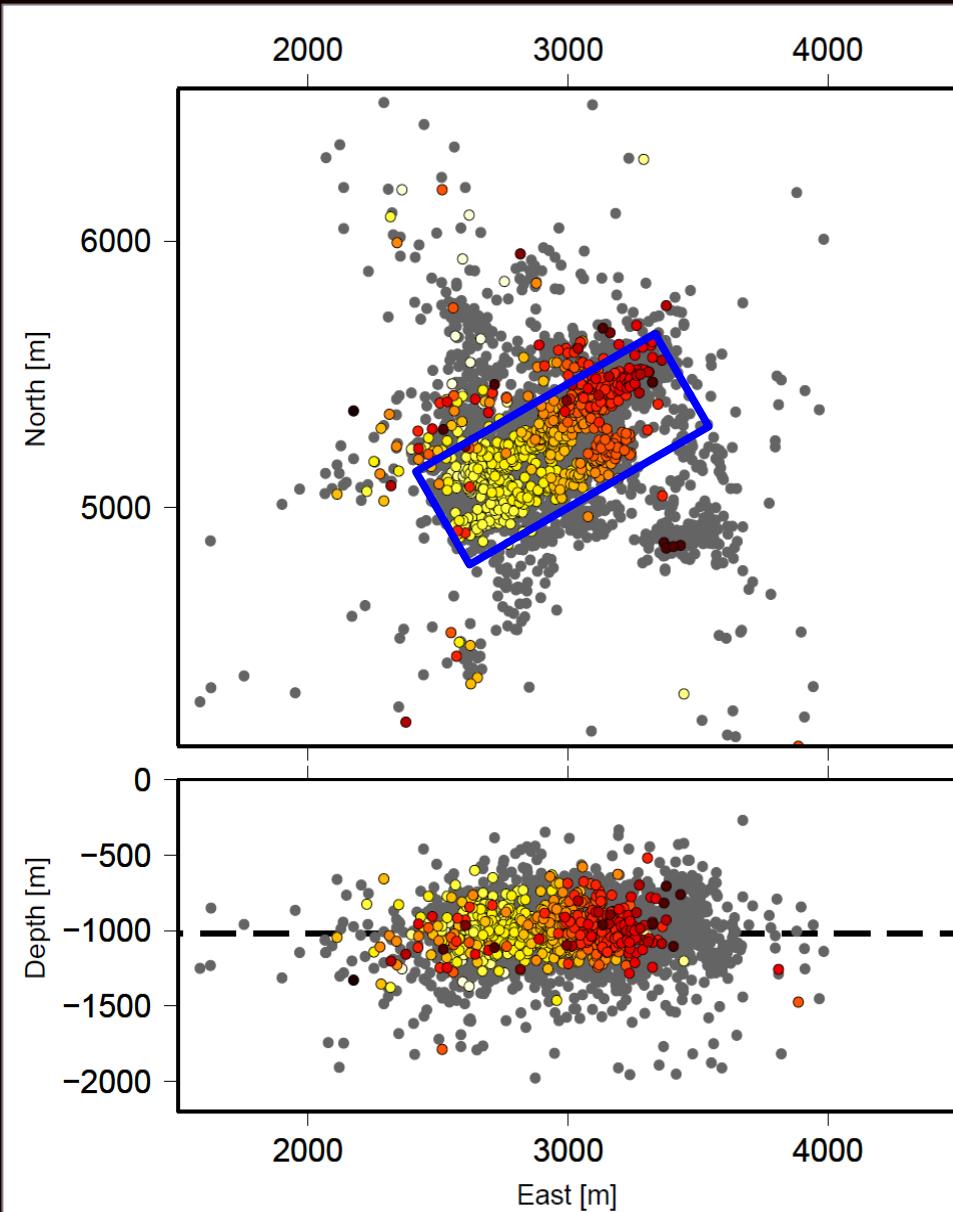
6 broadband stations (5 Guralp CMG,
pink; 1 Trillium 40, purple)

9 short-period (Mark L-4C-3D, orange)

3 subsurface stations (yellow)

We work here at 0.5-2Hz or 1-4Hz,
combine BB and SP stations



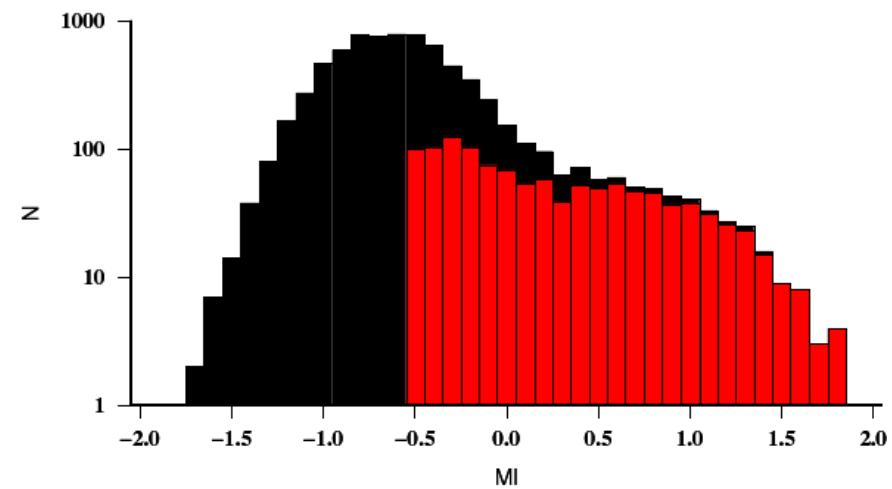


Spatiotemporal evolution of seismicity follows longwall mining

Additional clusters

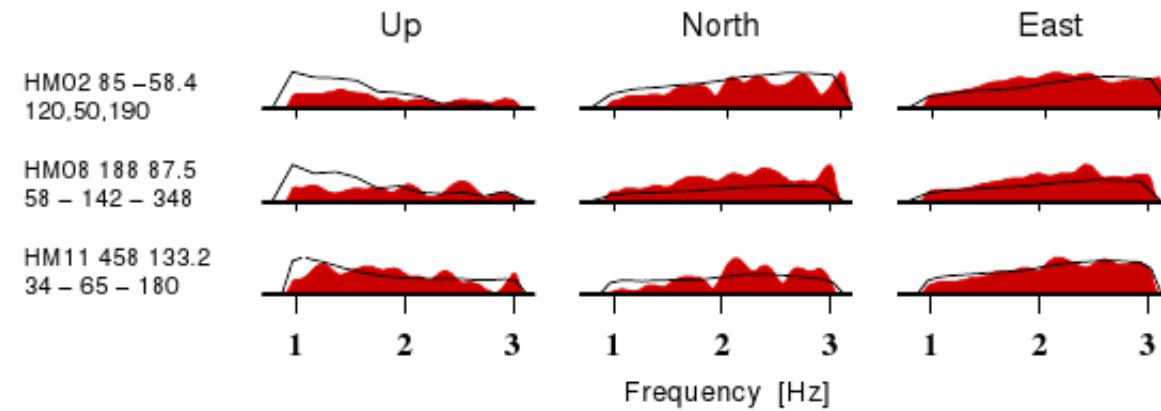
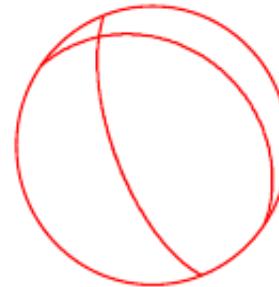
Average depth above the mining level

Bimodal frequency-magnitude distribution

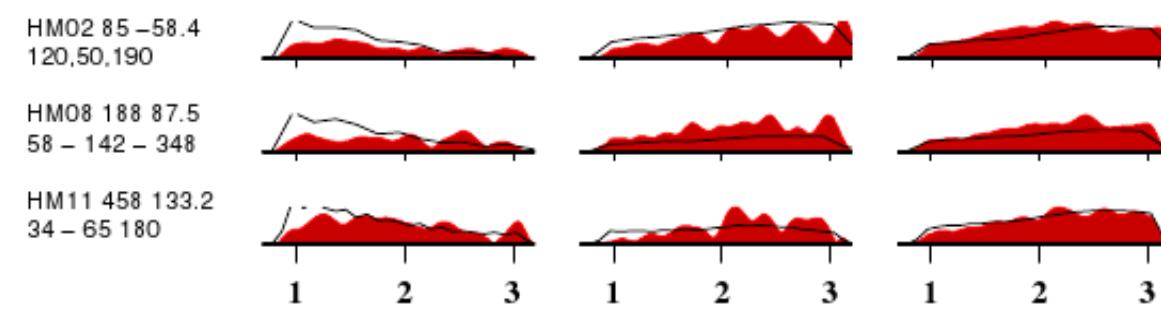


Step 1, 1b Point source inversion (amplitude spectra)

a) DC Amplitude Spectra

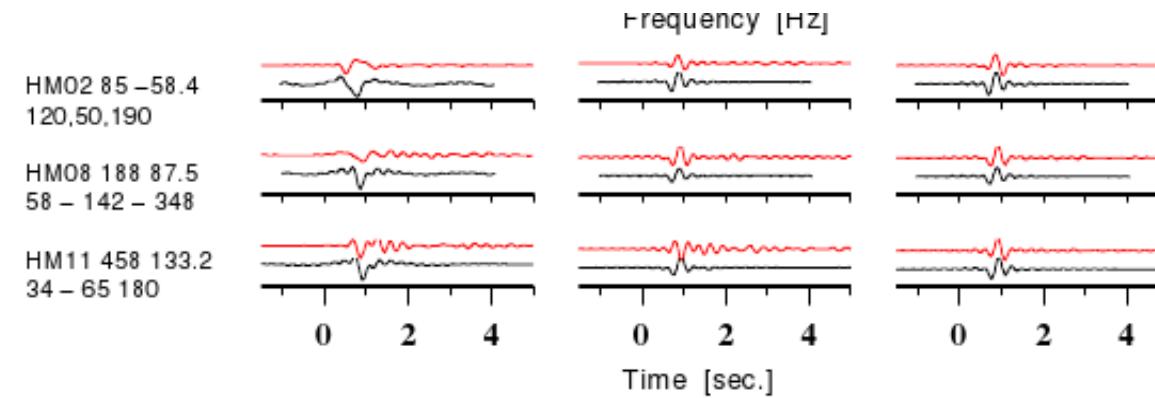
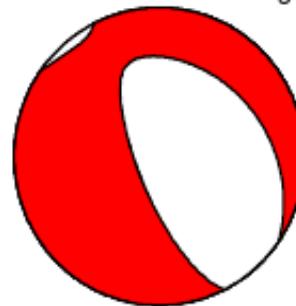


b) MT Amplitude Spectra



Step 2, 2b Point source inversion (time domain)

c) MT Waveform Fitting

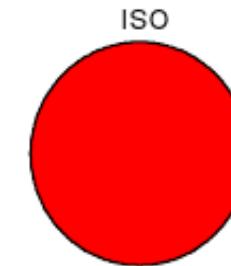
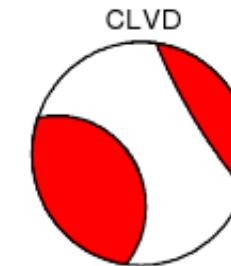
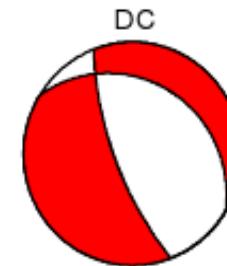


d) Decomposition of MT

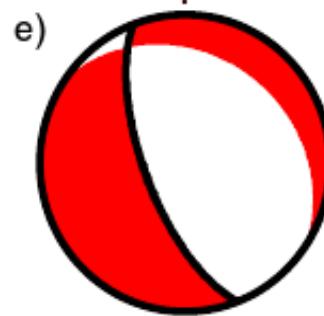
DC = %91

CLVD = %9

ISO = %21



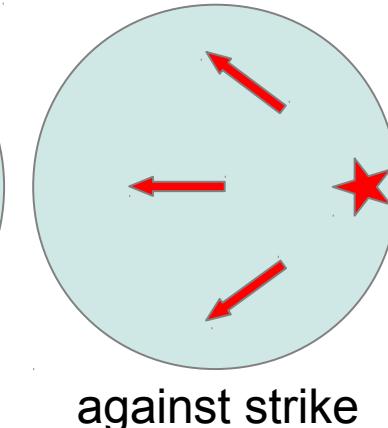
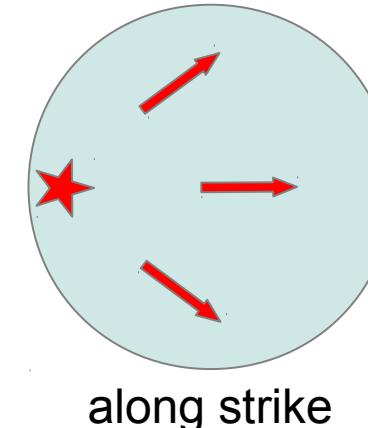
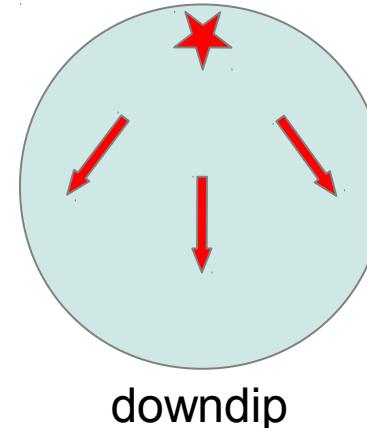
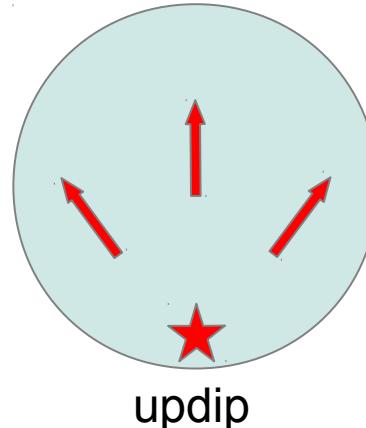
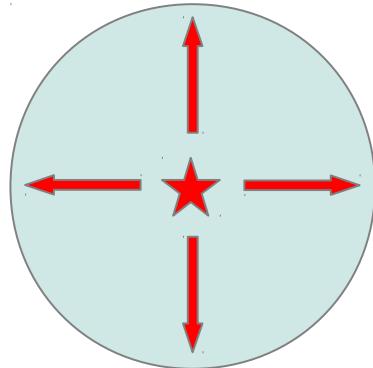
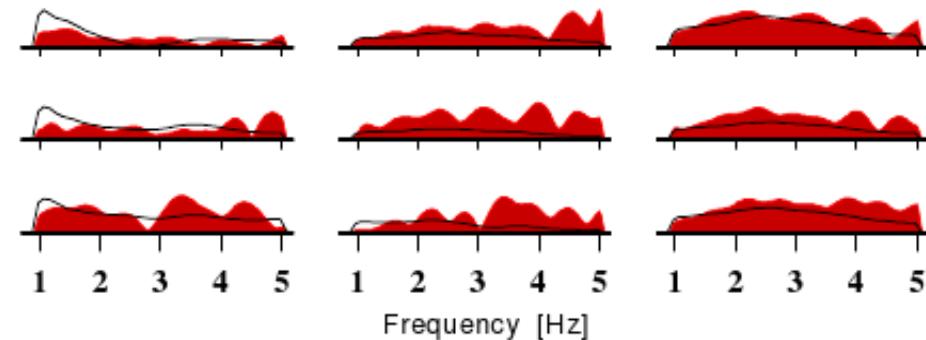
Step 3 Kinematic inversion (amplitude spectra)



HM02 85 - 58.4
120, 50, 190

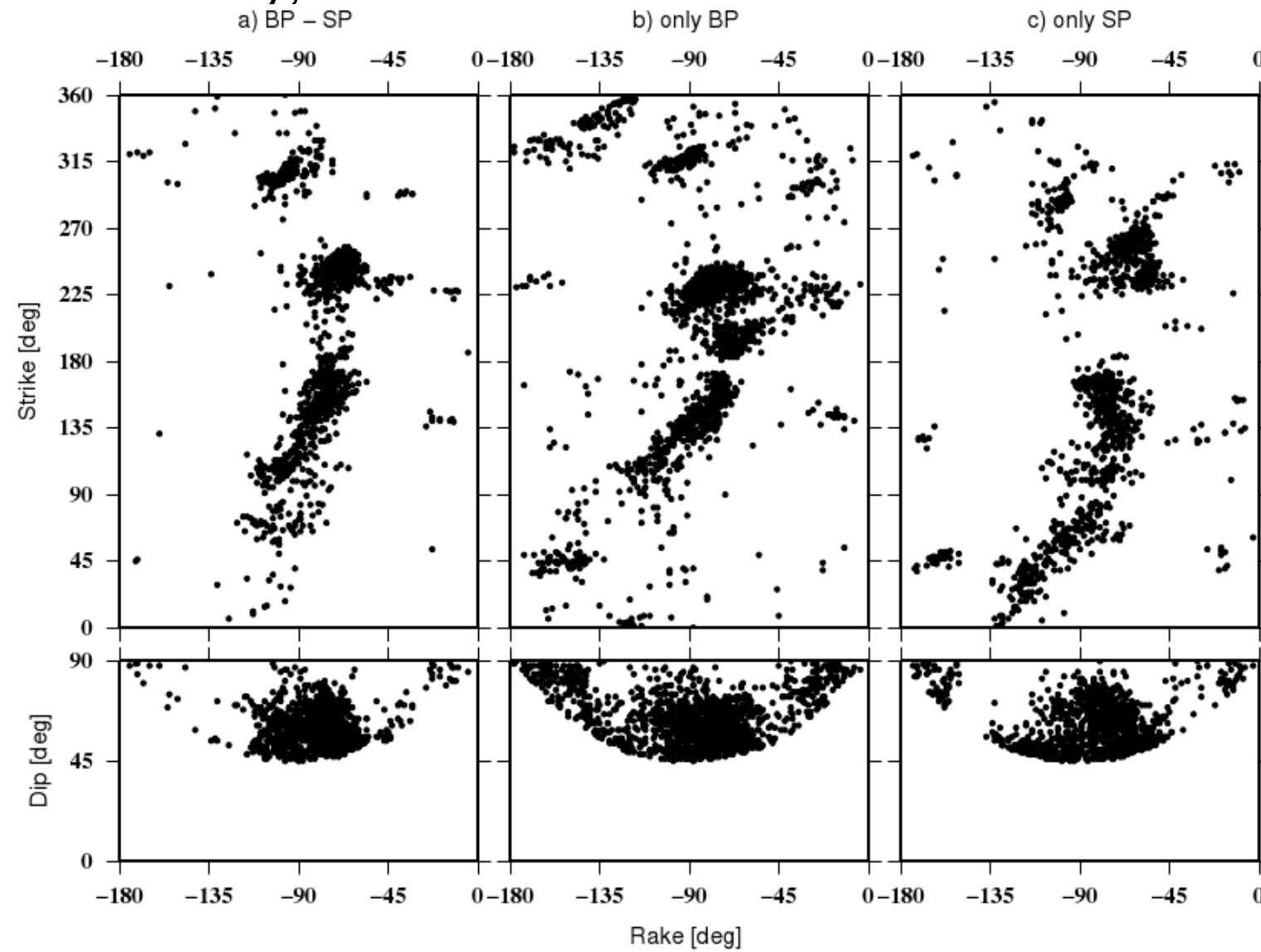
HM08 188 87.5
58 - 142 - 348

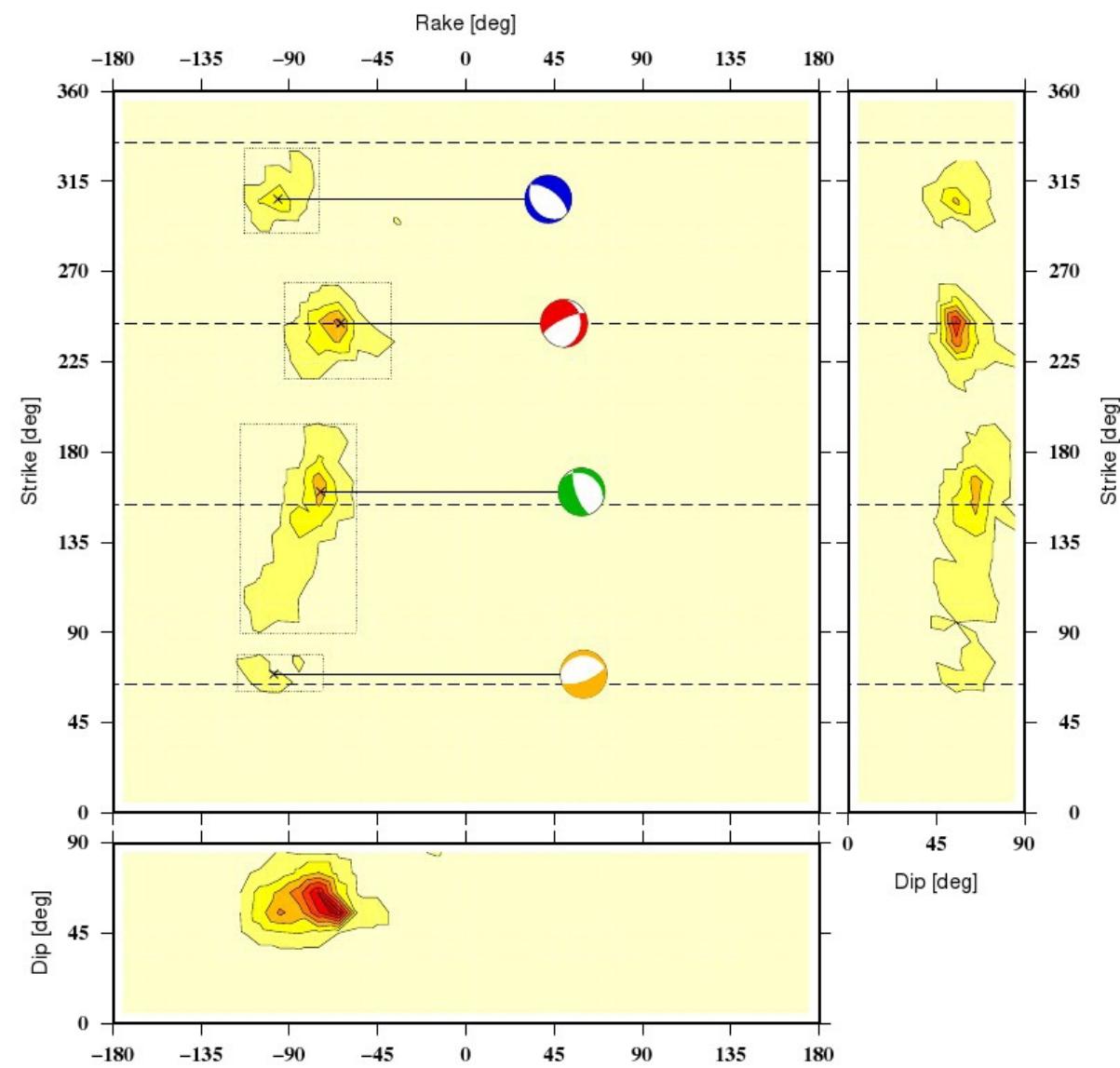
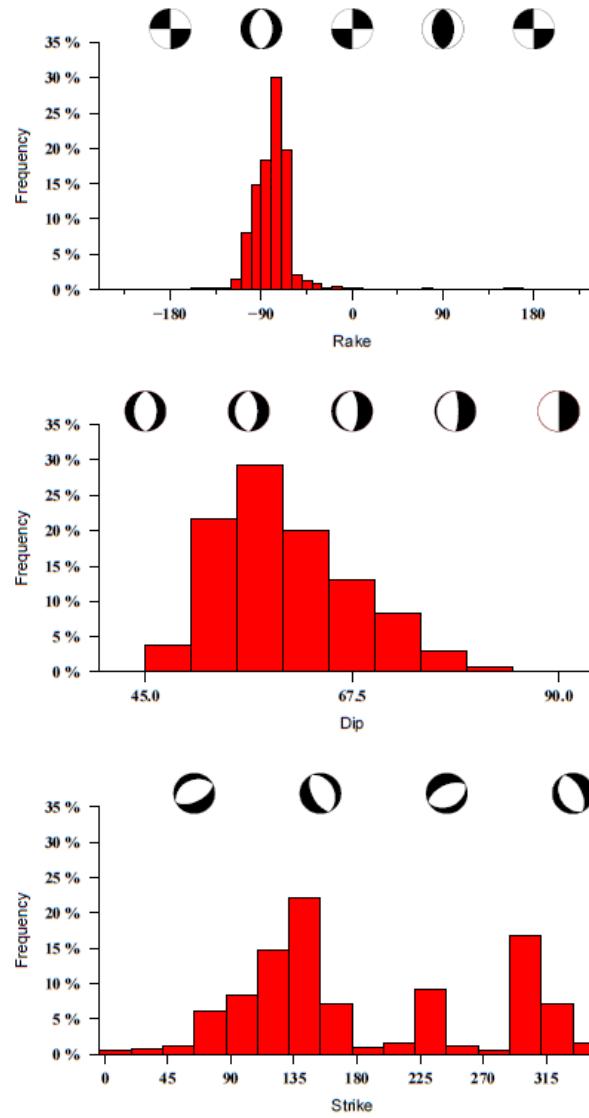
HM11 458 133.2
34 - 65 180

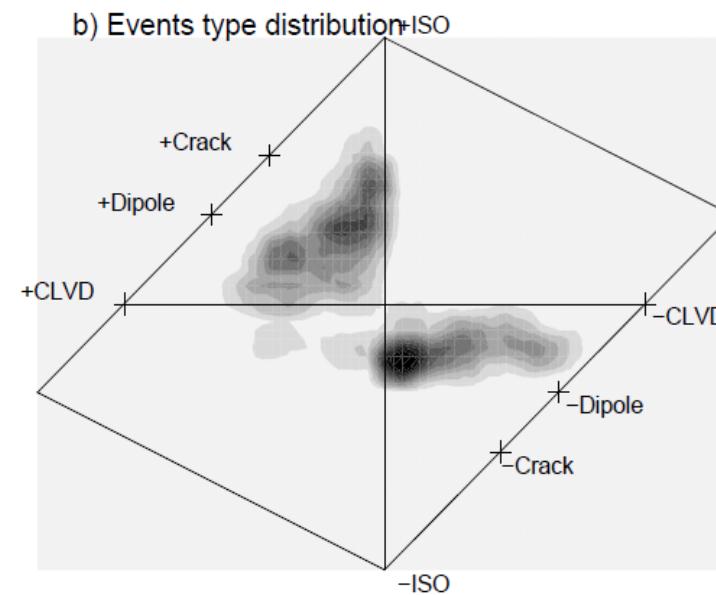
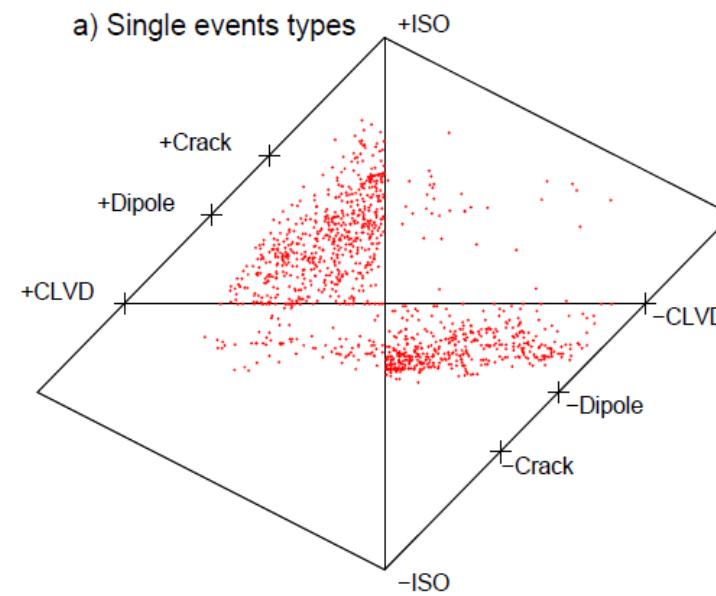
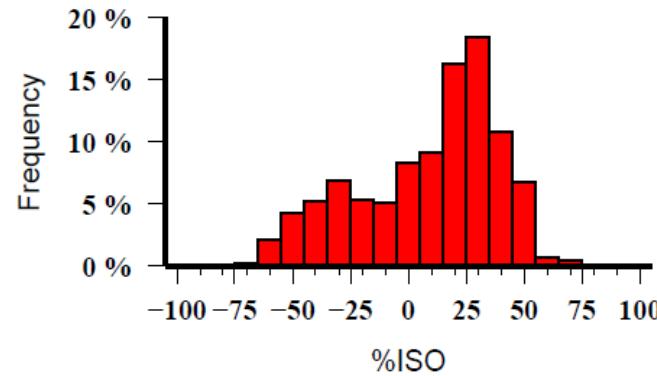
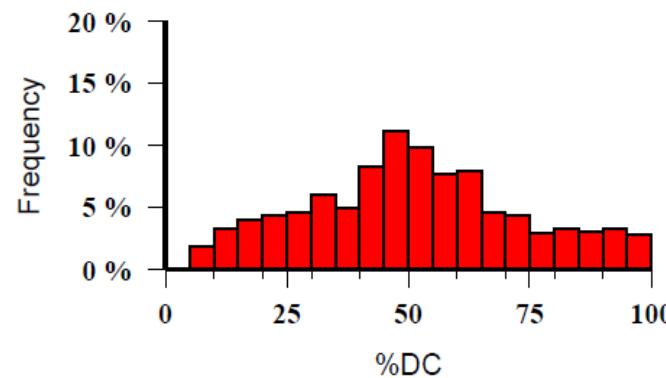
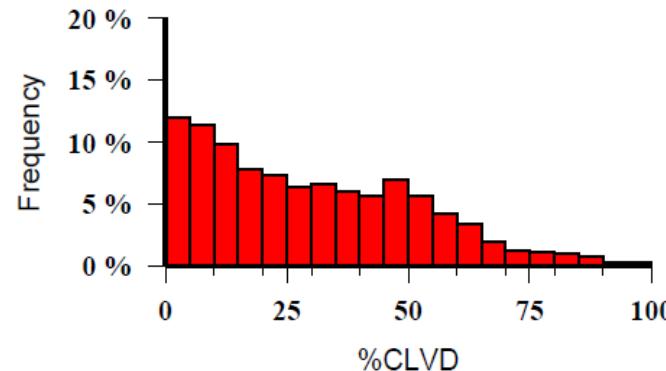


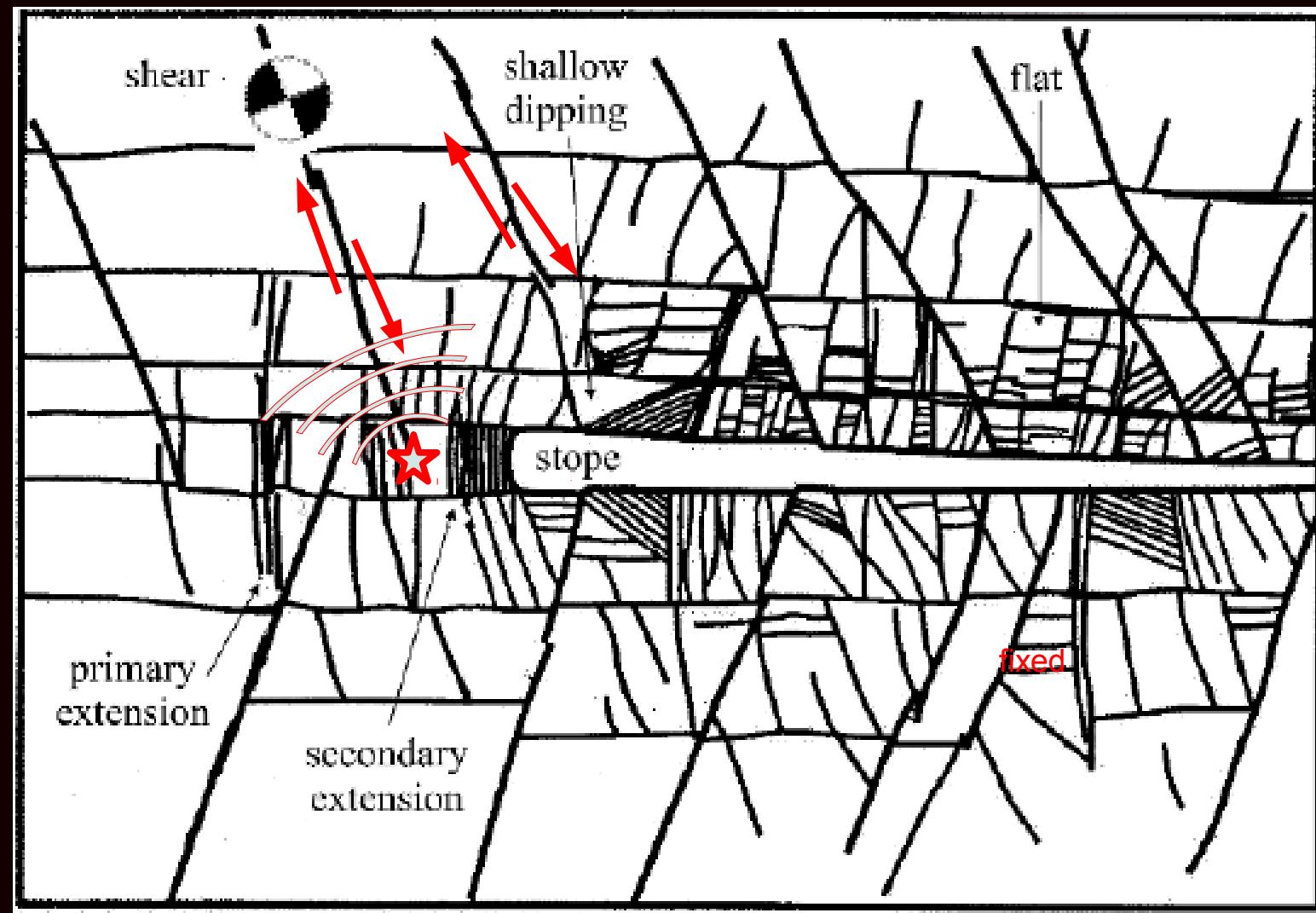
Results stability, different stations

con









Sen et al. DGG 2012, after Ryder and Jager (2002)

Thanks to:

A. T. Sen, Prof. Dr. T. Dahm, Dr. S. Heimann, A. Rohr

**DFG and BMBF project KINHERD, RAPID, MINE
GEOTECHNOLGIEN programme**

The Kiwi tools are currently used at:

**University of Hamburg, University of Potsdam, BGR Hannover, GFZ Potsdam,
University of Lisbon, University of Coimbra, Aristotle University of Thessaloniki,
Ruhr University Bochum**

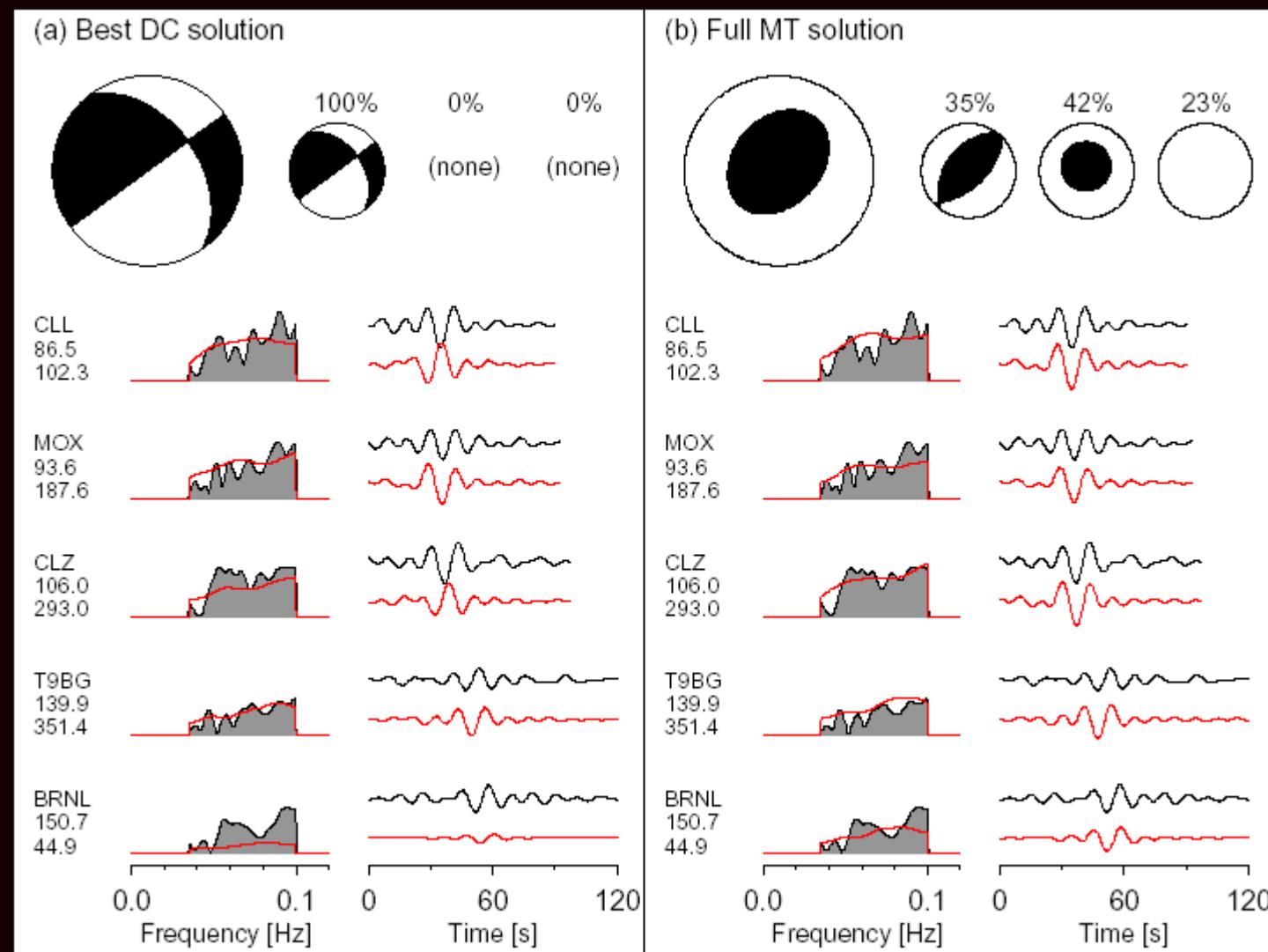
Further info on software and applications:

<http://mine.zma.de>

<http://kinherd.org>



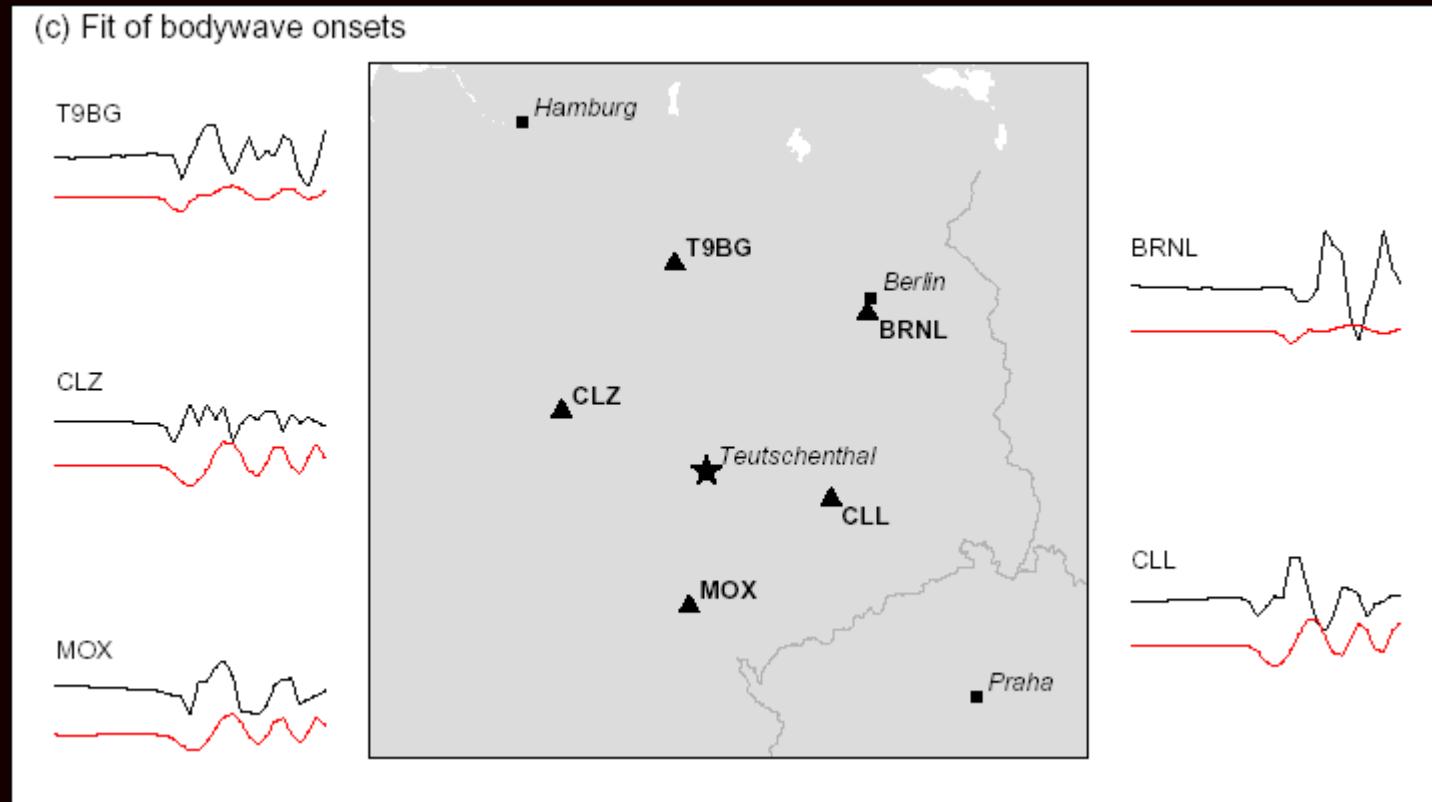
Source inversion, natural and induced seismicity



Cesca et
al.
submitte
d



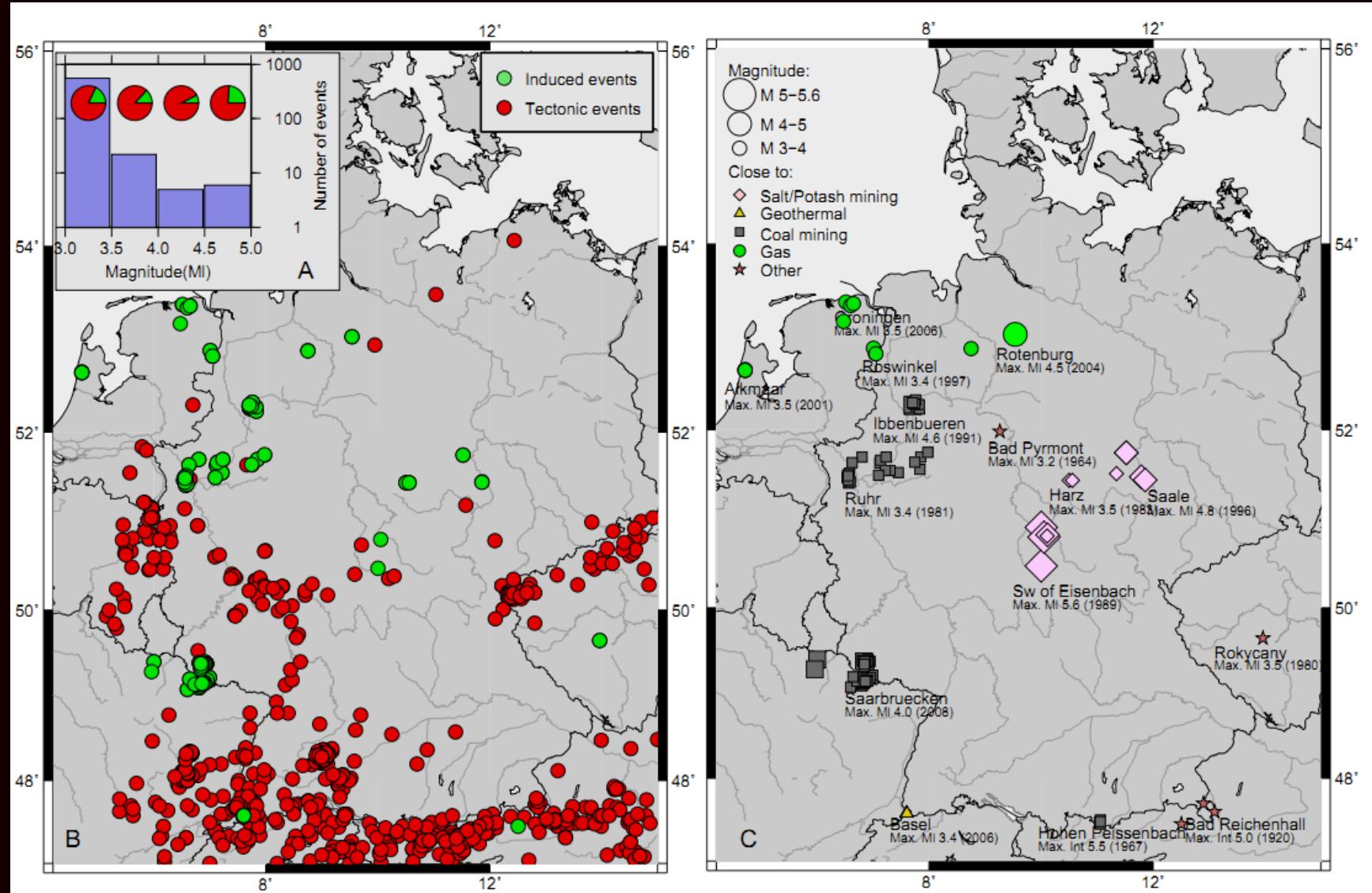
Source inversion, natural and induced seismicity



Cesca et
al.
submitte
d



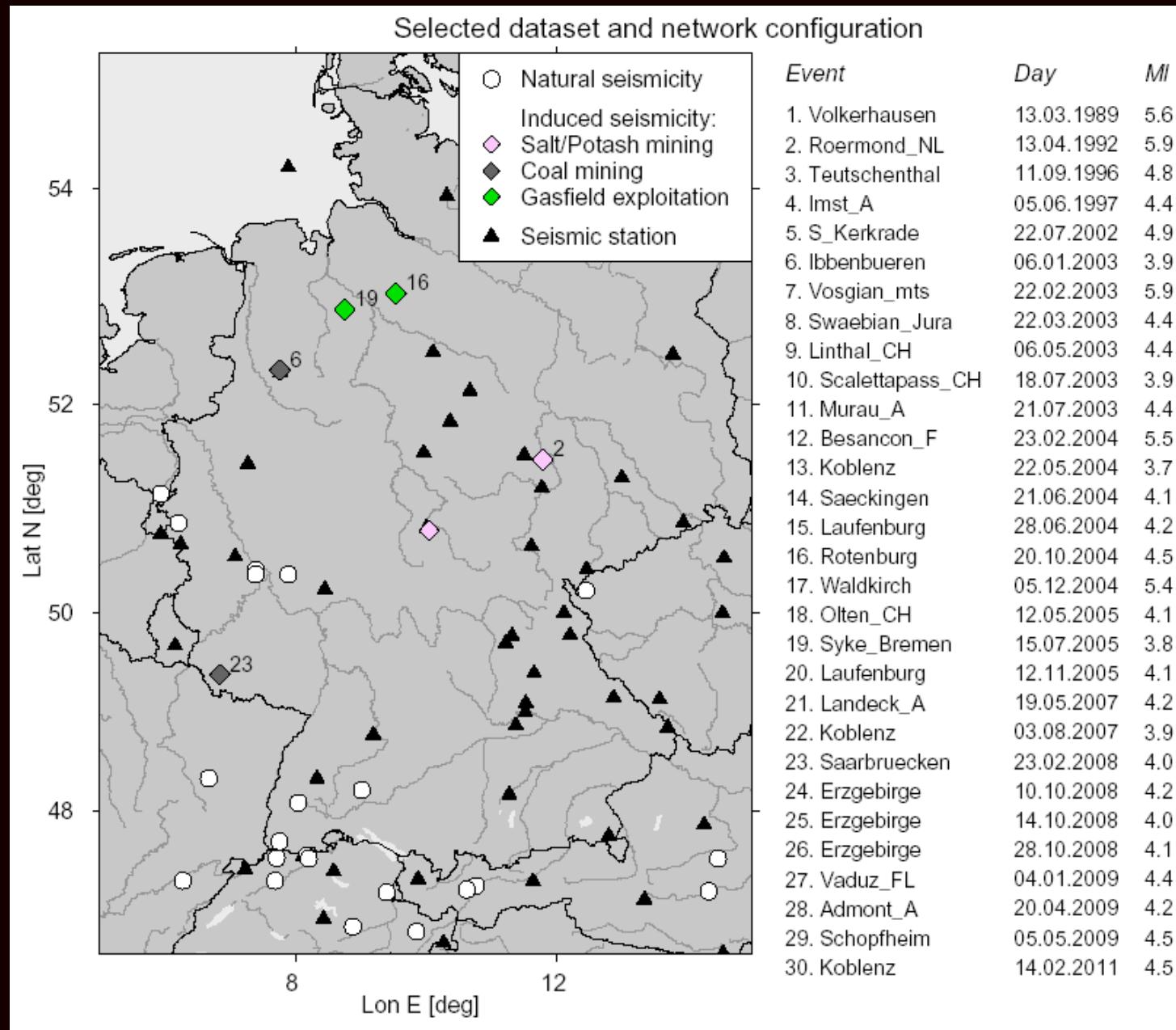
Source inversion, natural and induced seismicity



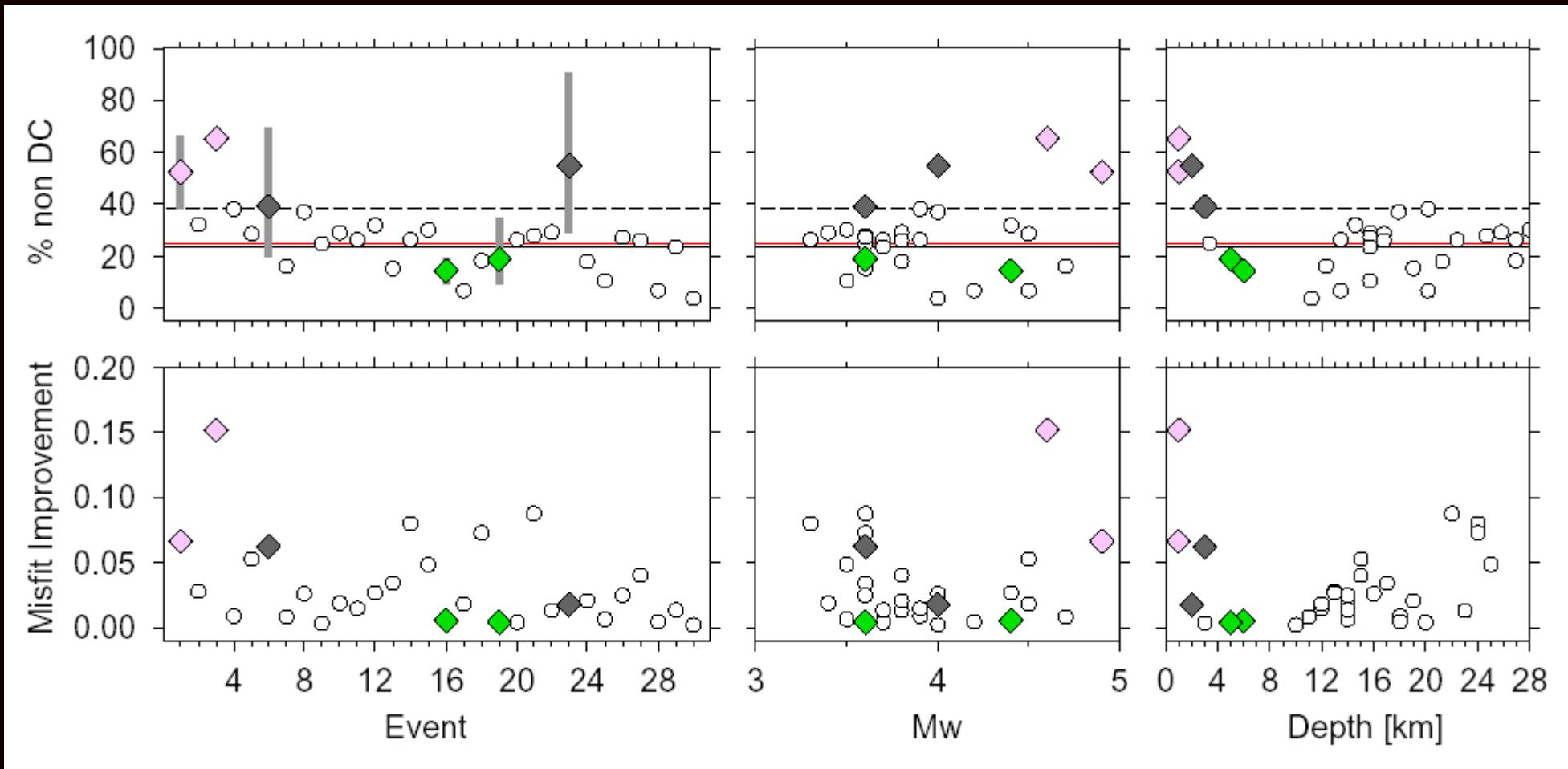
Cesca et al.
submitted



Source inversion, natural and induced seismicity



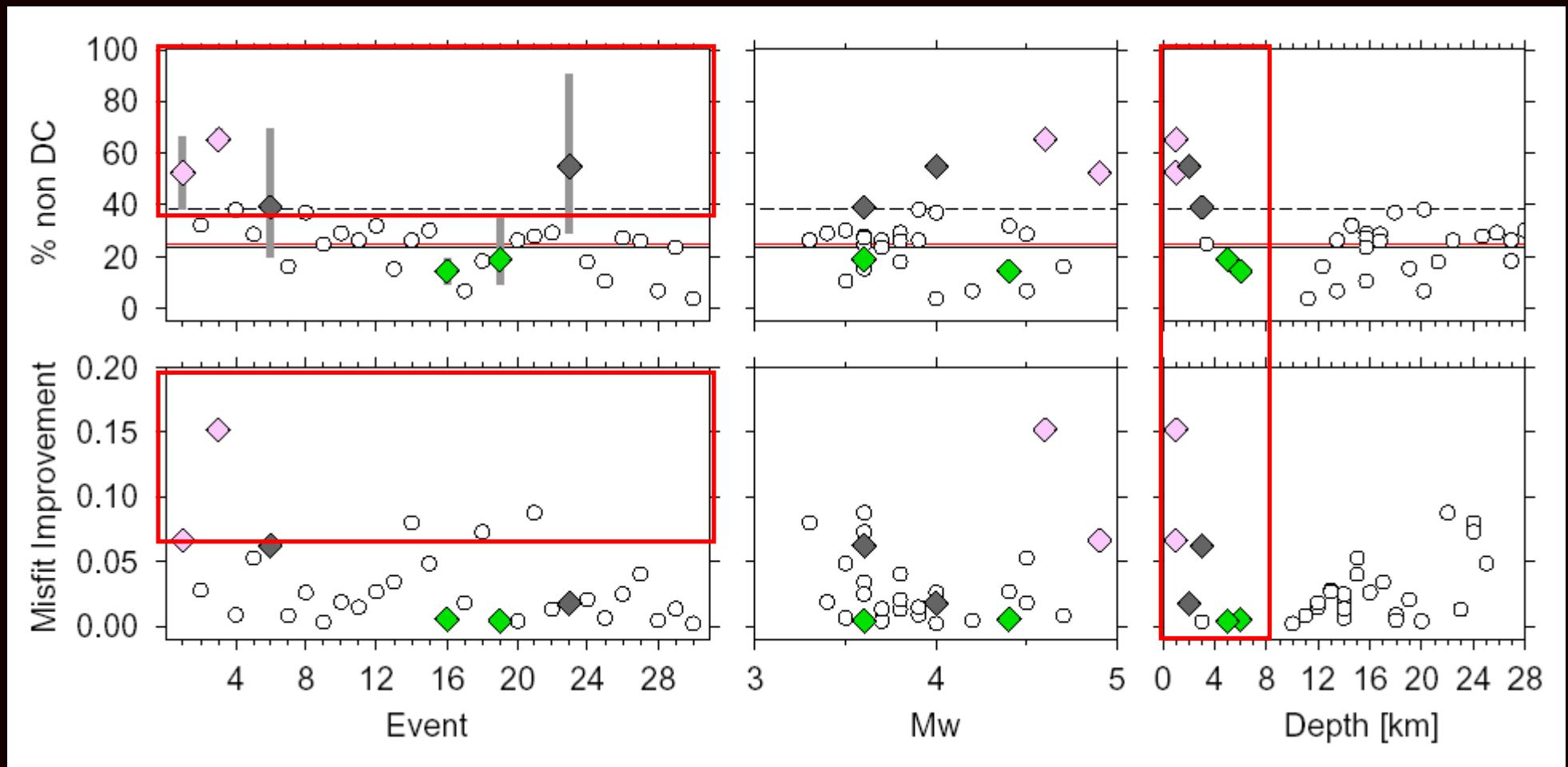
Source inversion, natural and induced seismicity



Cesca et al.,
submitted



Where to look for induced (collapses, rockbursts, pillar blasts, explosions) seismicity?



Cesca et al., J. Seismol., R1 submitted



Kiwi Green's function database

